

Theoretical study of "K-pp"



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1. *Introduction*
2. *Situation of theoretical studies of "K-pp"*
3. *"K-pp" investigated with ccCSM+Feshbach method*
4. *Further analysis of "K-pp"*
 - *SIDDHARTA constraint for K-p scattering length*
 - *Another way of $K^{\text{bar}}N$ energy self-consistency*
 - *Double pole of "K-pp"?*
5. *Summary and future plan*

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(Nihon univ.)
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(Osaka Inst. Tech.)

1. Introduction

 K^- $K^{\text{bar}}N$ two-body system**Proton**

Low energy scattering data, $1s$ level shift of kaonic hydrogen atom

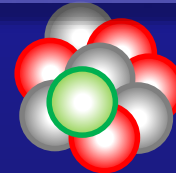
“Excited hyperon $\Lambda(1405) = K^-$ proton quasi-bound state”

Strongly attractive $K^{\text{bar}}N$ potential



- Doorway to **dense matter**[†]
→ Chiral symmetry restoration in dense matter
- Interesting structure[†]
- Neutron star

Kaonic nuclei



${}^3\text{He}K^-$, $pppK^-$,
 ${}^4\text{He}K^-$, $pppnK^-$,
..., ${}^8\text{Be}K^-$, ...

[†] A. D., H. Horiuchi, Y. Akaishi and T. Yamazaki, PRC70, 044313 (2004)

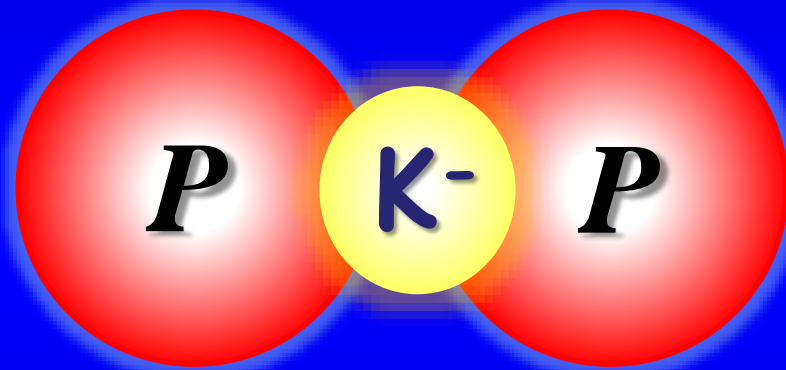


Proton

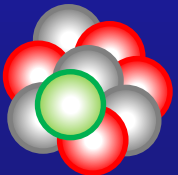


K^-

$K^{\text{bar}}N$ two-body system = $\Lambda(1405)$



Prototype system = $K^- pp$

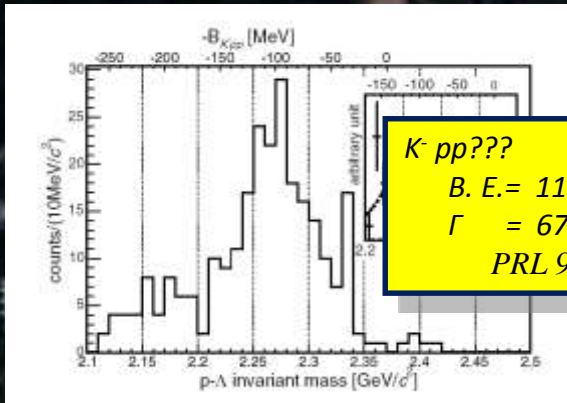


Kaonic nuclei

= Nuclear many-body system with antikaons

Experiments of K - pp search

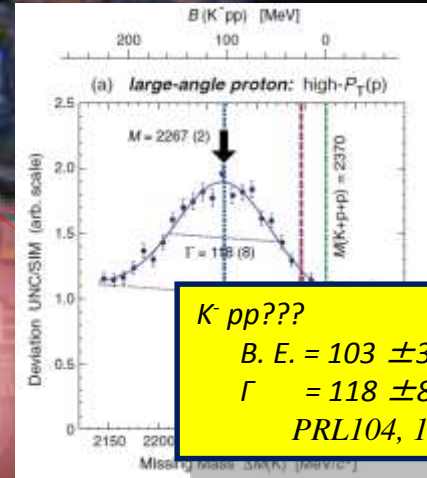
FINUDA



$K^- pp$???

$B. E. = 115 \text{ MeV}$
 $\Gamma = 67 \text{ MeV}$
 PRL 94, 212303 (2005)

DISTO

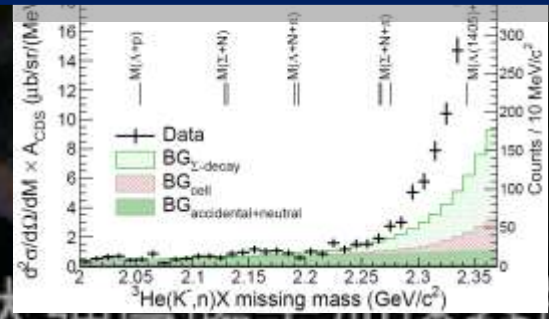


$K^- pp$???

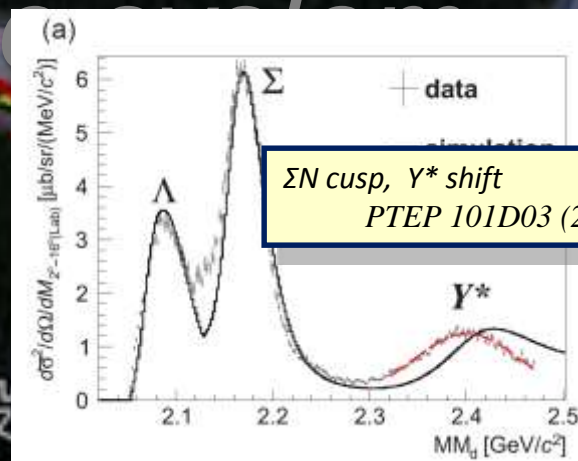
$B. E. = 103 \pm 3 \pm 5 \text{ MeV}$
 $\Gamma = 118 \pm 8 \pm 10 \text{ MeV}$
 PRL 104, 132502 (2010)

J-PARC E15

Attraction in K - pp subthreshold region
 arXiv:1408.5637 [nucl-ex]

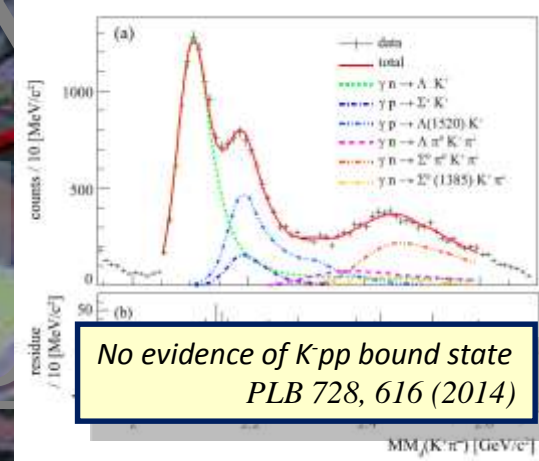


J-PARC E27



ΣN cusp, Y^* shift
 PTEP 101D03 (2014)

SPring8/LEPS



No evidence of $K^- pp$ bound state
 PLB 728, 616 (2014)

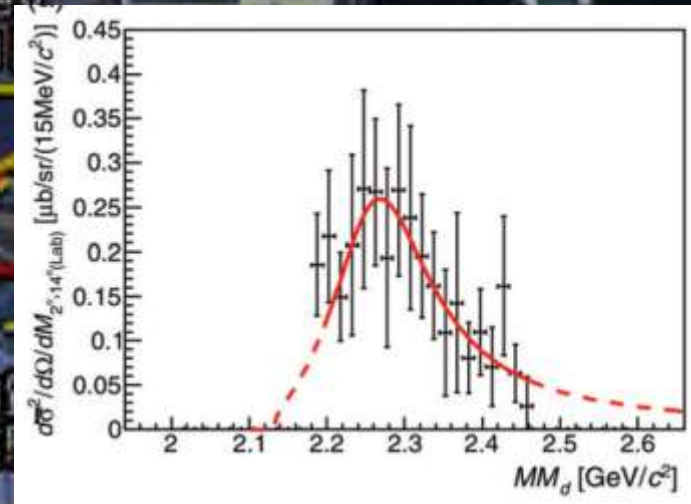
K^-pp at J-PARC

- J-PARC E27

$d(\pi^+, K^+) \quad P_{\pi^-} = 1.7 \text{ GeV}/c$

$Mass = 2275_{-18}^{+17+21} \text{ MeV}$
 $(B_{Kpp} \sim 95 \text{ MeV})$
 $\Gamma = 162_{-45}^{+87+66} \text{ MeV}$

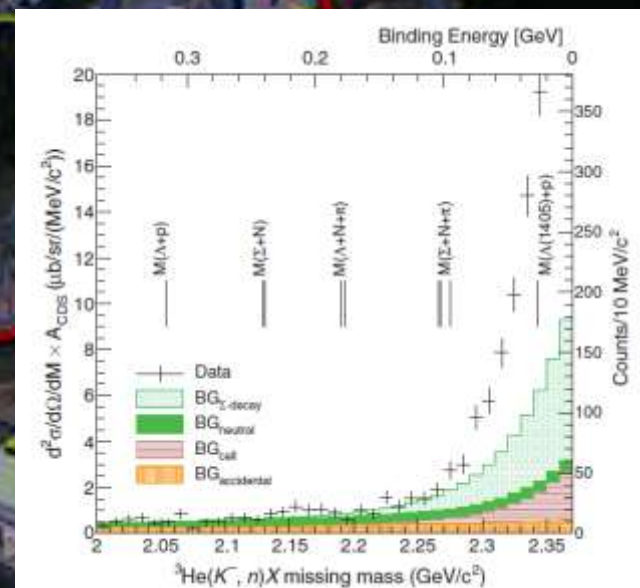
Y. Ichkawa et al. PTEP 2015, 021D01



- J-PARC E15 (1st run)

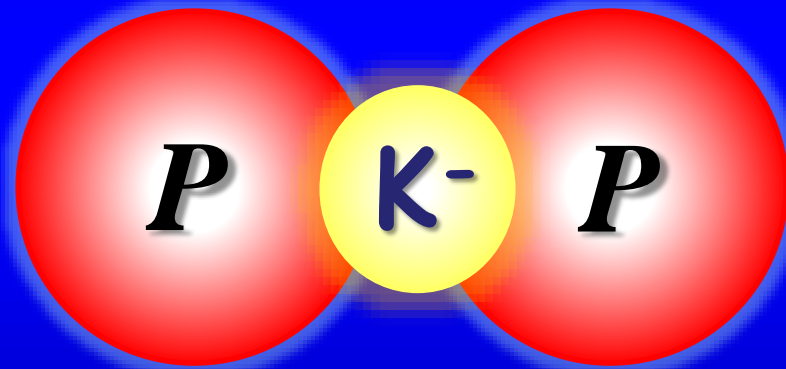
${}^3\text{He}(\text{inflight } K^-, n)X \quad P_K = 1.0 \text{ GeV}/c$
 $X \rightarrow \Lambda + p$

Attraction in K^-pp subthreshold region



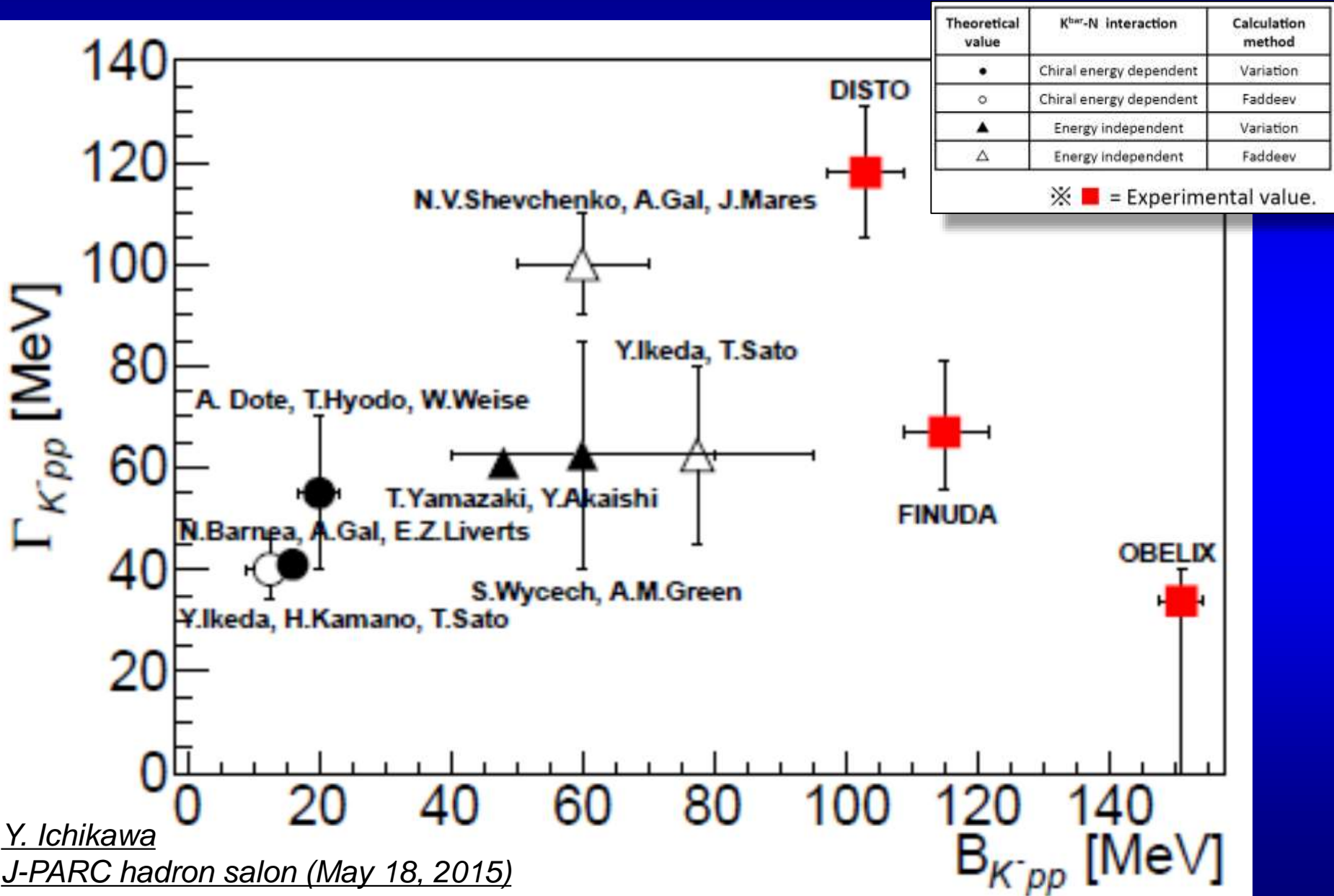
T. Hashimoto et al. PTEP 2015, 061D01

2. Situation of theoretical studies



“ K^-pp ” =
 $K^{\text{bar}}NN - \pi\Sigma N - \pi\Lambda N$ ($J^\pi = 0^-, T=1/2$)

Theoretical studies of “K⁻pp”



Y. Ichikawa

J-PARC hadron salon (May 18, 2015)

Theoretical studies of “K⁻pp”

	<i>Dote-Hyodo-Weise</i>	<i>Barnea-Gal-Liverts</i>	<i>Akaishi-Yamazaki</i>	<i>Ikeda-Kamano-Sato</i>	<i>Shevchenko-Gal-Mares</i>
	PRC79, 014003 (2009)	PLB712, 132 (2012)	PRC76, 045201 (2007)	PTP124, 533 (2010)	PRC76, 044004 (2007)
$B(K\text{-}pp)$	20 ± 3	16	47	9 ~ 16	50 ~ 70
Γ	40 ~ 70	41	61	34 ~ 46	90 ~ 110
Method	Variational (Gauss)	Variational (H. H.)	Variational (Gauss)	Faddeev-AGS	Faddeev-AGS
Potential	<i>Chiral</i> (<i>E</i> -dep.)	<i>Chiral</i> (<i>E</i> -dep.)	<i>Pheno.</i>	<i>Chiral</i> (<i>E</i> -dep.)	<i>Pheno.</i>

- **Chiral pot. (*E*-dep.)** → **Small *B. E.***
 ... $\Lambda(1405) \sim 1420 \text{ MeV}$ (*B. E.* $\sim 15 \text{ MeV}$)
- **Phenomenological pot. (*E*-indep.)** → **Large *B. E.***
 ... $\Lambda(1405) = 1405 \text{ MeV}$ (*B. E.* = 30 MeV)

$B(K\text{-}pp) < 100 \text{ MeV}$

***K⁻pp* should be a resonance between $K^{\text{bar}}NN$ and $\pi\Sigma N$ thresholds.**

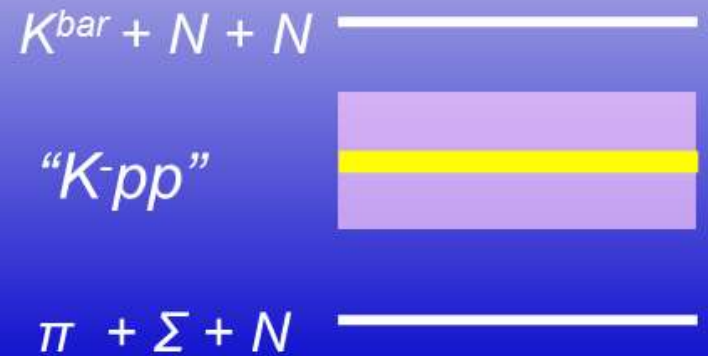
3. “K-pp” investigated with
ccCSM+Feshbach method

- $\Lambda(1405) = \text{Resonant state \& } K^{\text{bar}}N \text{ coupled with } \pi\Sigma$

- “K-pp” ... Resonant state of
 $K^{\text{bar}}NN\text{-}\pi YN$ coupled-channel system

*Doté, Hyodo, Weise, PRC79, 014003(2009). Akaishi, Yamazaki, PRC76, 045201(2007)
Ikeda, Sato, PRC76, 035203(2007). Shevchenko, Gal, Mares, PRC76, 044004(2007)
Barnea, Gal, Liverts, PLB712, 132(2012)*

- Resonant state
- Coupled-channel system



⇒ “coupled-channel
Complex Scaling Method”

Complex Scaling Method

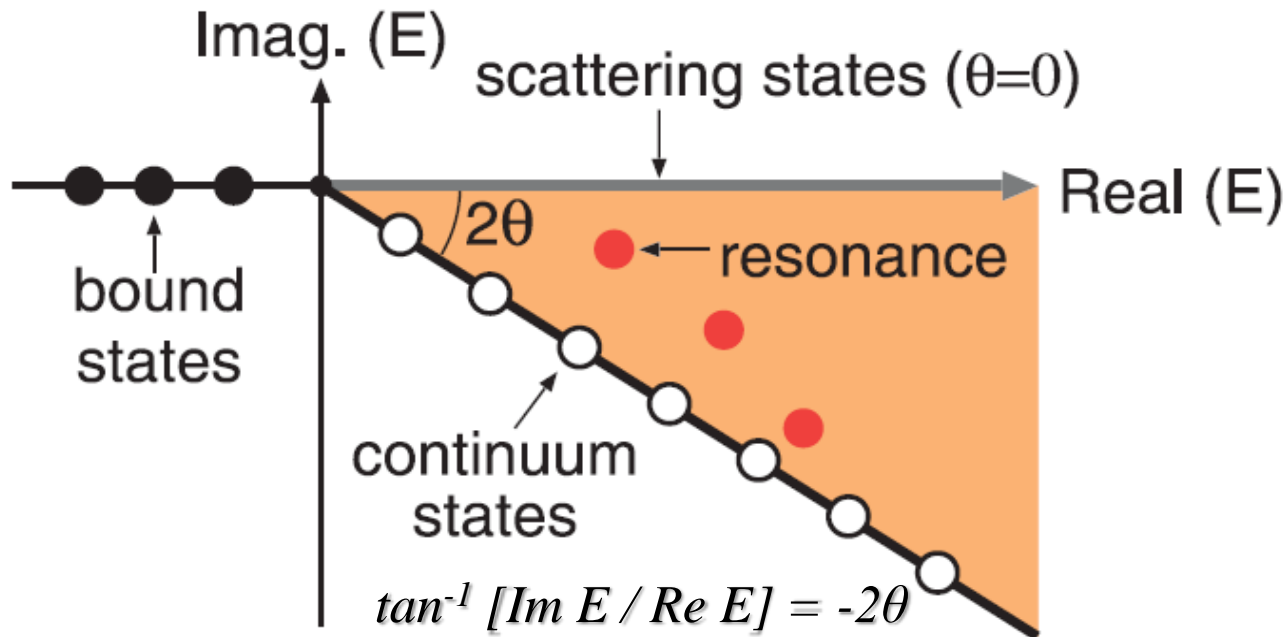
... Powerful tool for resonance study of many-body system

Complex rotation (Complex scaling) of coordinate

Resonance wave function $\rightarrow L^2$ integrable

$$U(\theta): \mathbf{r} \rightarrow \mathbf{r} e^{i\theta}, \quad \mathbf{k} \rightarrow \mathbf{k} e^{-i\theta}$$

Diagonalize $H_\theta = U(\theta) H U^{-1}(\theta)$ with Gaussian base,



- Continuum state appears on 2ϑ line.
- Resonance pole is off from 2ϑ line, and independent of ϑ . (ABC theorem)

Chiral SU(3) potential with a Gaussian form

A. D., T. Inoue, T. Myo, Nucl. Phys. A 912, 66 (2013)

• **Anti-kaon = Nambu-Goldstone boson**

⇒ Chiral SU(3)-based $K^{\text{bar}}N$ potential

- Weinberg-Tomozawa term of effective chiral Lagrangian
- Gaussian form in r -space
- Semi-rela. / Non-rela.
- Based on Chiral SU(3) theory
→ **Energy dependence**

A non-relativistic potential (NRv2c)

$$V_{ij}^{(I=0,1)}(r) = -\frac{C_{ij}^{(I=0,1)}}{8f_{\pi}^2} (\omega_i + \omega_j) \sqrt{\frac{1}{m_i m_j}} g_{ij}(r)$$

$$g_{ij}(r) = \frac{1}{\pi^{3/2} d_{ij}^3} \exp\left[-(r/d_{ij})^2\right] : \text{Gaussian form}$$

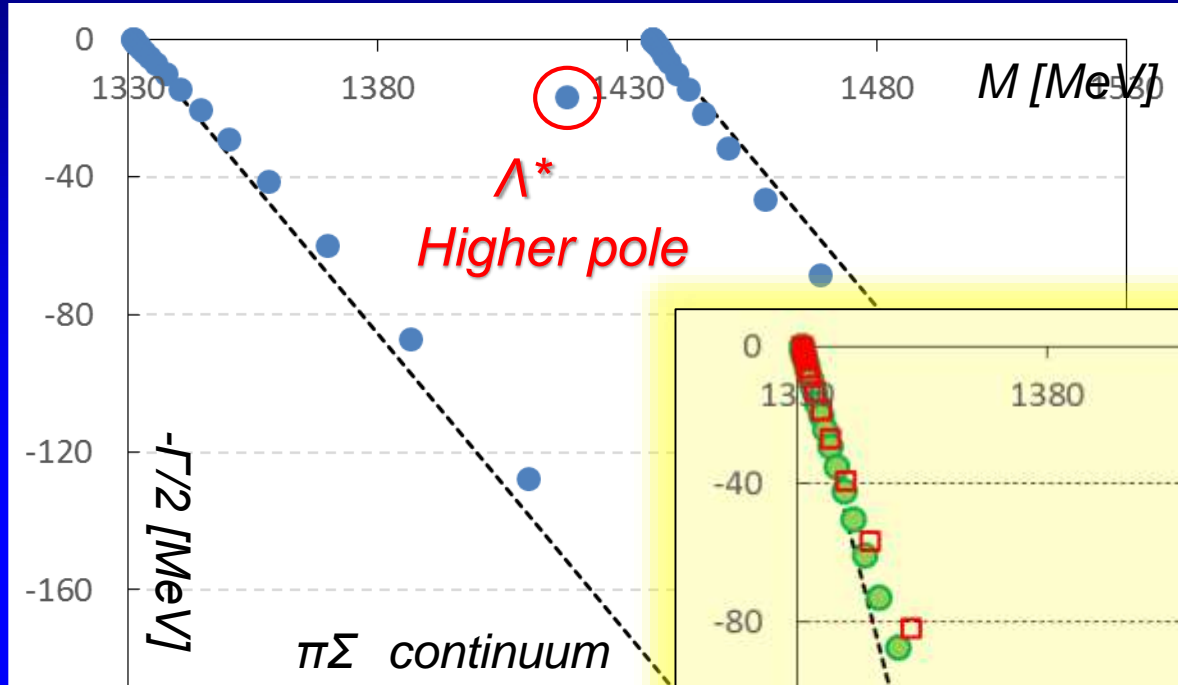
ω_i : meson energy

Constrained by $K^{\text{bar}}N$ scattering length

$$a_{KN(I=0)} = -1.70 + i0.67 \text{ fm}, \quad a_{KN(I=1)} = 0.37 + i0.60 \text{ fm}$$

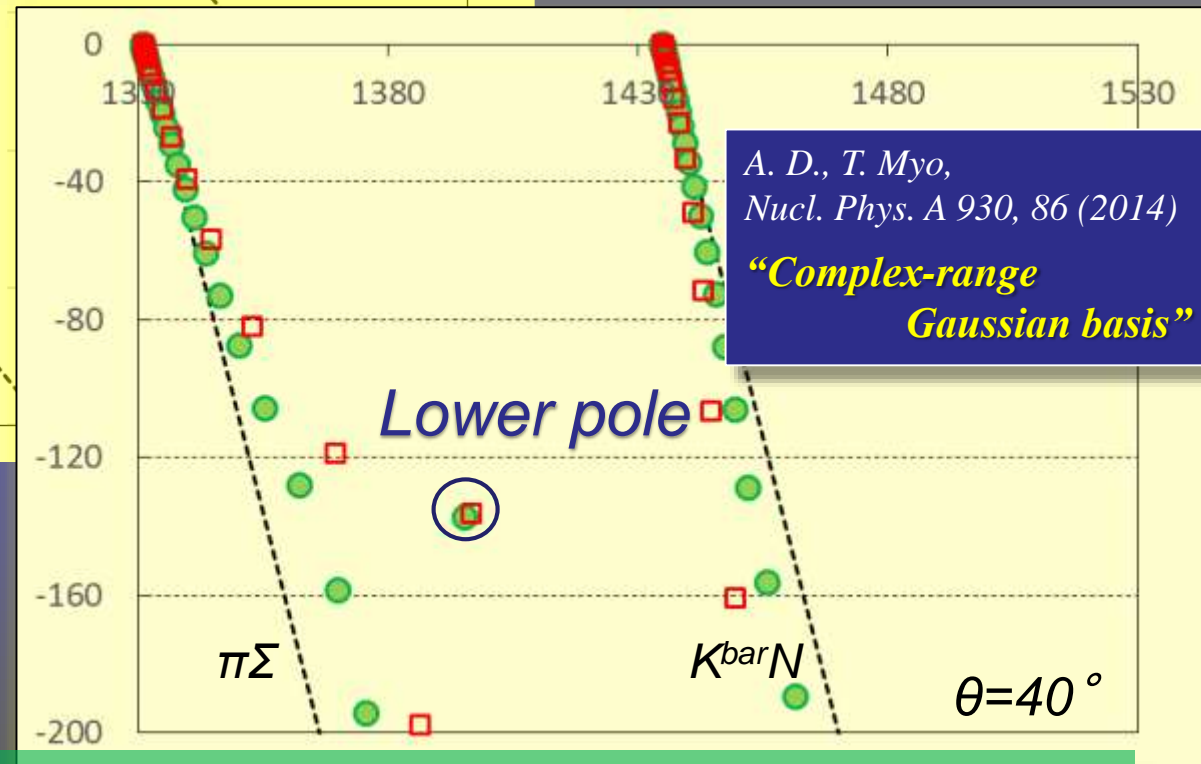
A. D. Martin, NPB179, 33(1979)

$\Lambda(1405)$ on coupled-channel Complex Scaling Method



$K^{\text{bar}}N$ potential:
a chiral $SU(3)$ potential
(NRv2, $f_\pi=110$)

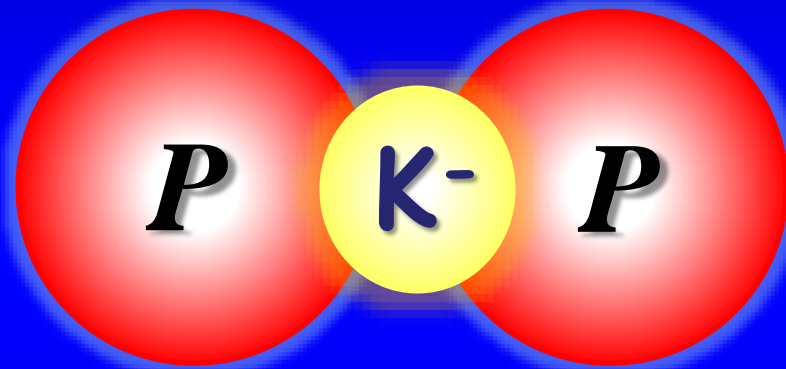
A. D., T. Inoue, T. Myo,
Nucl. Phys. A 912, 66 (2013)



A. D., T. Myo,
Nucl. Phys. A 930, 86 (2014)
“Complex-range
Gaussian basis”

Double-pole structure of $\Lambda(1405)$

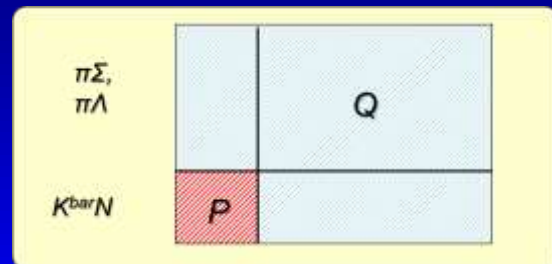
$$\text{“}K^-pp\text{”} = K^{\text{bar}}NN - \pi\Sigma N - \pi\Lambda N \quad (J^\pi = 0^-, T=1/2)$$



*Feshbach projection on
coupled-channel Complex Scaling Method
“ccCSM+Feshbach method”*

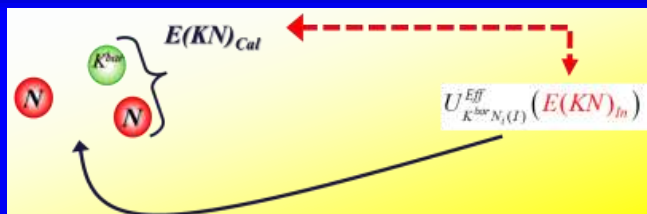
Remarks on “K^{bar}pp” calculation

1. For economical treatment of a three-body system of “K^{bar}pp”, an **effective K^{bar}N single-channel potential** is derived by means of **Feshbach projection on CSM**.



$$\begin{matrix} V(K^{\bar{b}ar}N - \pi Y; I=0,1) \\ V(\pi Y - \pi Y'; I=0,1) \end{matrix} \longrightarrow U_{K^{\bar{b}ar}N(I=0,1)}^{Eff}(E)$$

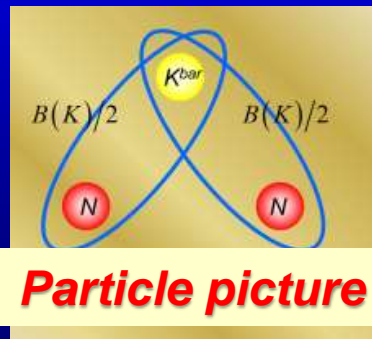
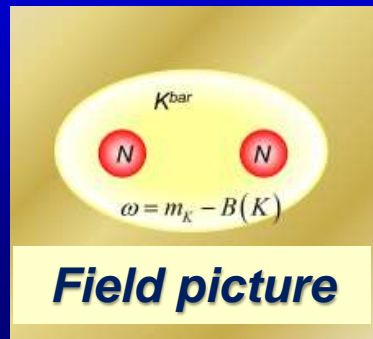
2. **Self-consistency for complex K^{bar}N energy** is taken into account.



- $E(KN)_{In}$: assumed in the $K^{\bar{b}ar}N$ potential
- $E(KN)_{Cal}$: calculated with the obtained $K\text{-}pp$

$$E(KN)_{In} = E(KN)_{Cal}$$

3. The energy of a K^{bar}N pair in K^{bar}pp is estimated in two ways.

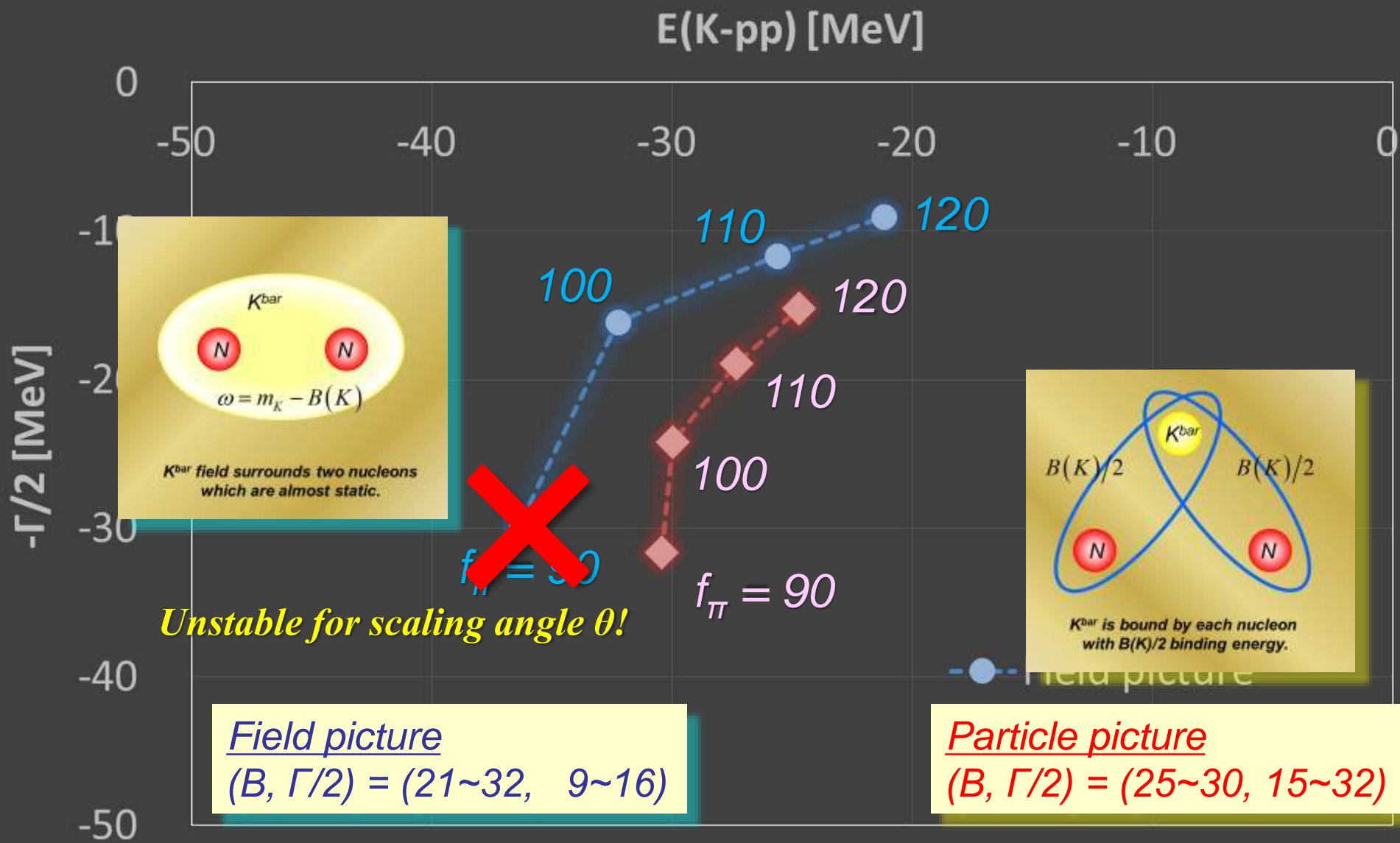


$$E(KN) = M_N + \omega = \begin{cases} M_N + m_K - B(K) & : \text{Field pict.} \\ M_N + m_K - B(K)/2 & : \text{Particle pict.} \end{cases}$$

Self-consistent results

$f_\pi = 90 \sim 120 \text{ MeV}$

NN pot. : Av18 (Central)
 K^{bar} N pot. : NRv2c potential
 ($f_\pi = 90 - 120 \text{ MeV}$)



Field picture
 ($B, \Gamma/2$) = (21~32, 9~16)

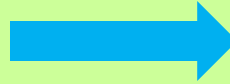
Particle picture
 ($B, \Gamma/2$) = (25~30, 15~32)

NN correlation density

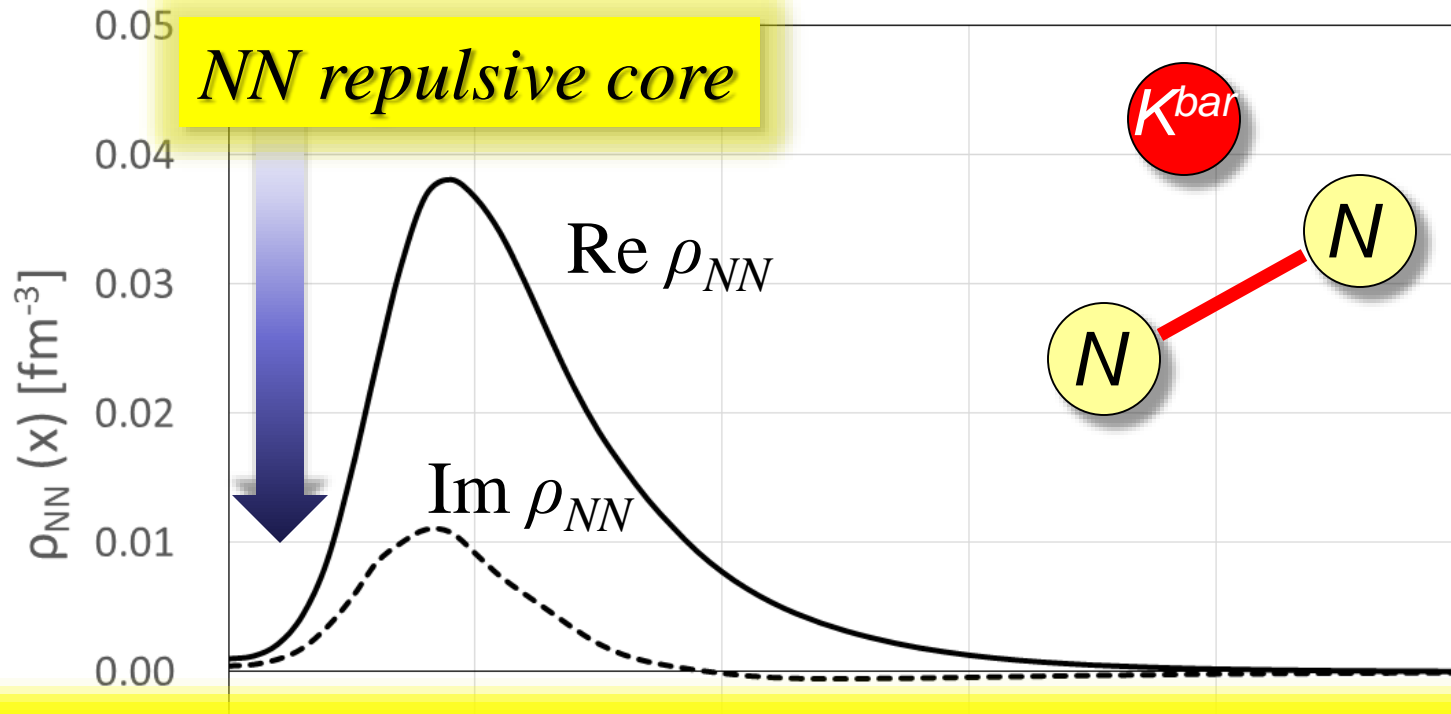
NN pot. : Av18 (Central)
 $K^{\text{bar}}N$ pot. : NRv2c potential
 $f_{\pi}=110$, Particle pict.

Correlation density in Complex Scaling Method

$$\rho_{NN,\theta}(\mathbf{x}) = \delta^3(\hat{\mathbf{r}}_{NN,\theta} - \mathbf{x})$$
$$\hat{\mathbf{r}}_{NN,\theta} = \hat{\mathbf{r}}_{NN} e^{i\theta}$$



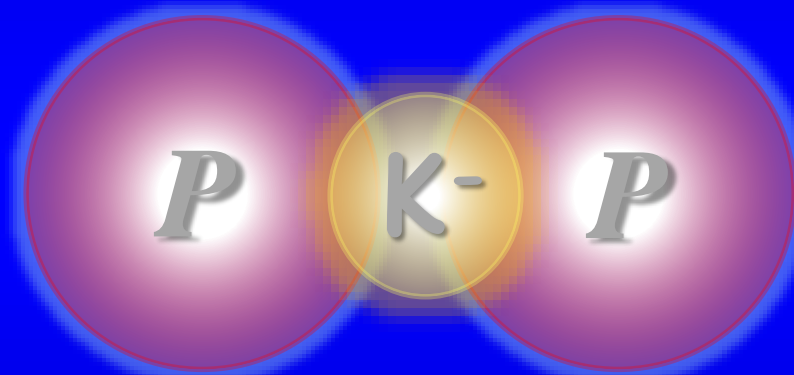
$$\rho_{NN}(\mathbf{x}) \equiv \langle \Phi_{\theta} | \rho_{NN,\theta}(\mathbf{x}) | \Phi_{\theta} \rangle$$
$$= e^{-3i\theta} \int d^3\mathbf{R} \Phi_{\theta}^2(\mathbf{x}e^{-i\theta}, \mathbf{R})$$



NN distance = 2.1 - i 0.3 fm

*~ Mean distance of 2N in nuclear matter at **normal density!***

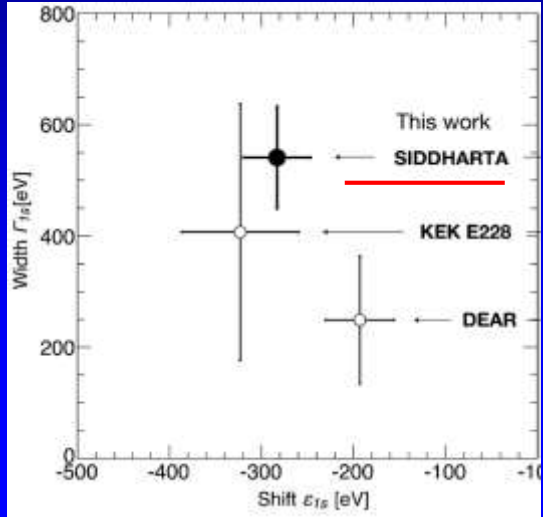
4. Further analysis of “K-pp”



- *SIDDHARTA* constraint for K-p scattering length
- Another way of $K^{\text{bar}}N$ energy self-consistency

K-pp with SIDDHARTA data

Precise measurement of 1s level shift of kaonic hydrogen



Strong constraint for the $K^{bar}N$ interaction!

$$\epsilon_{1s} = -283 \pm 36(\text{stat}) \pm 6(\text{syst}) \text{ eV}$$

$$\Gamma_{1s} = 541 \pm 89(\text{stat}) \pm 22(\text{syst}) \text{ eV}$$

M. Bazzi et al. (SIDDHARTA collaboration),
NPA 881, 88 (2012)

- Kp scattering length (with improved Deser-Truman formula)

U. -G. Meissner, U. Raha and A. Rusetsky, Eur. Phys. J. C 35, 349 (2004)

$$\text{Re} a(K^- p) = -0.65 \pm 0.10 \text{ fm}, \quad \text{Im} a(K^- p) = 0.81 \pm 0.15 \text{ fm}$$

- Kn scattering length (with coupled-channel chiral dynamics)

$$a(K^- n) = 0.57^{+0.04}_{-0.21} + i0.72^{+0.26}_{-0.41} \text{ fm.}$$

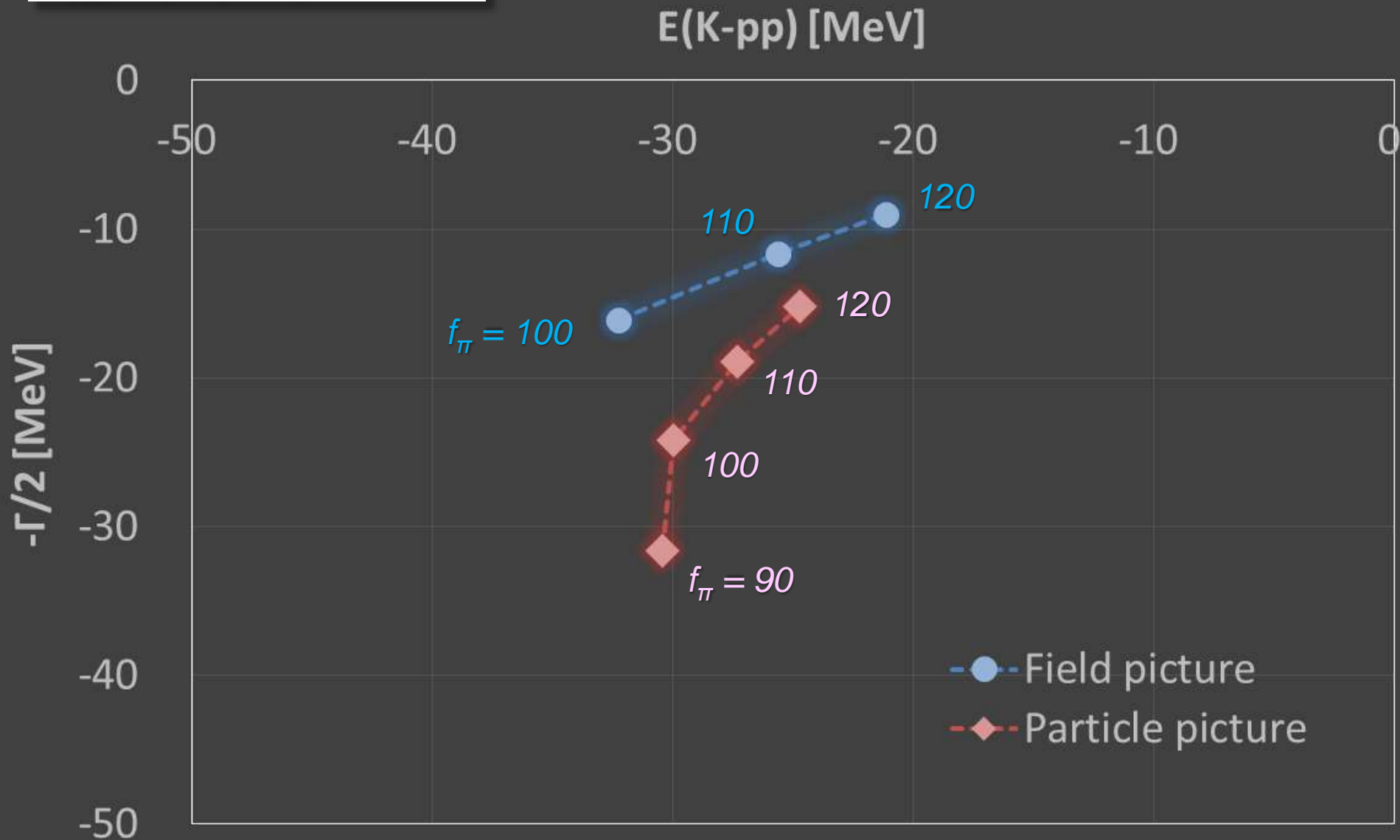
Y. Ikeda, T. Hyodo and W. Weise, NPA 881, 98 (2012)

"K-pp" with Martine value

$$a_{KN}(l=0) = -1.7 + i0.68 \text{ fm}$$

$$a_{KN}(l=1) = (0.37) + i0.60 \text{ fm}$$

NN pot. : Av18 (Central)
 $K^{\text{bar}}N$ pot. : NRv2c potential
($f_{\pi}=90 - 120\text{MeV}$)

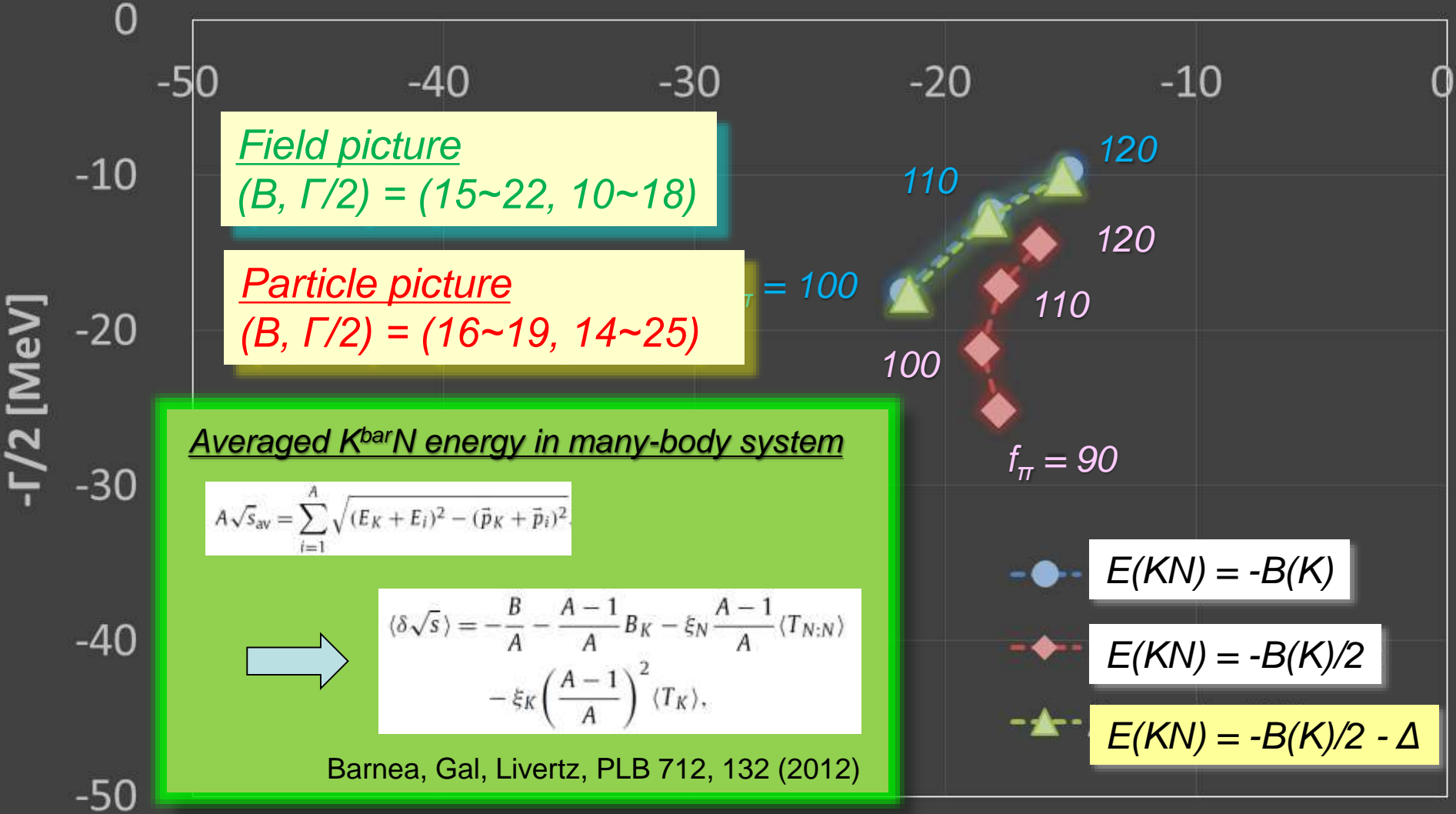


"K-pp" with SIDDHARTA value

NN pot. : Av18 (Central)
 $K^{\text{bar}}N$ pot. : NRv2a-IHW pot.
 ($f_{\pi}=90 - 120\text{MeV}$)

$a_{KN}(l=0) = -1.97 + i1.05 \text{ fm}$
 $a_{KN}(l=1) = 0.57 + i0.73 \text{ fm}$

$E(K\text{-pp}) [\text{MeV}]$



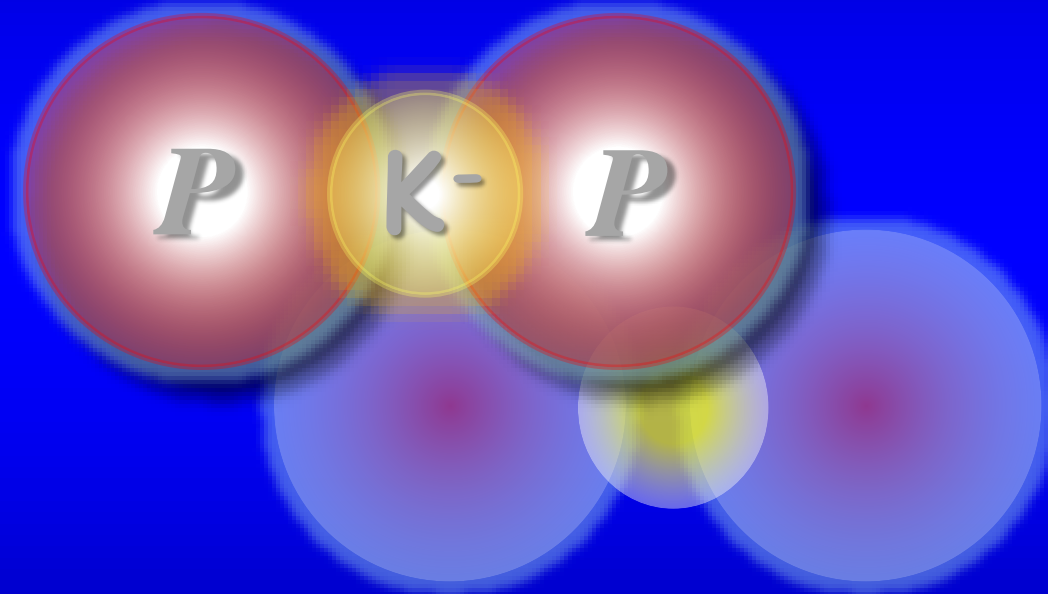
Averaged $K^{\text{bar}}N$ energy in many-body system

$$A\sqrt{s}_{\text{av}} = \sum_{i=1}^A \sqrt{(E_K + E_i)^2 - (\vec{p}_K + \vec{p}_i)^2}$$

$\delta\sqrt{s} = -\frac{B}{A} - \frac{A-1}{A} B_K - \xi_N \frac{A-1}{A} \langle T_{N:N} \rangle - \xi_K \left(\frac{A-1}{A}\right)^2 \langle T_K \rangle$

Barnea, Gal, Livertz, PLB 712, 132 (2012)

4. Further analysis of “K-pp”

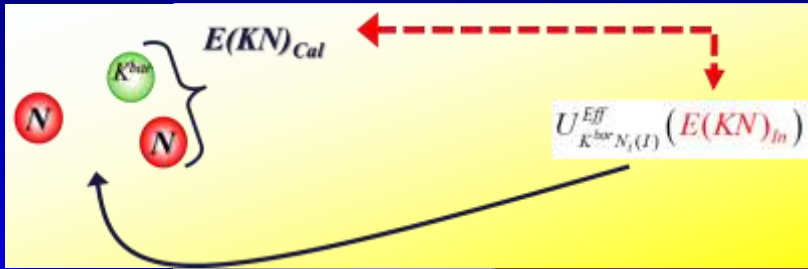


- Double pole of “K-pp”?

Quasi self-consistent solution

NRv2c ($f_\pi = 110$ MeV)

Particle picture



Indicator of self-consistency

$$\Delta = |E(KN)_{Cal} - E(KN)_{In}|$$

$\Delta=0$ at $E(KN)=(29, 14)$

Self-consistent solution:

$$B(KNN) = 27.3$$

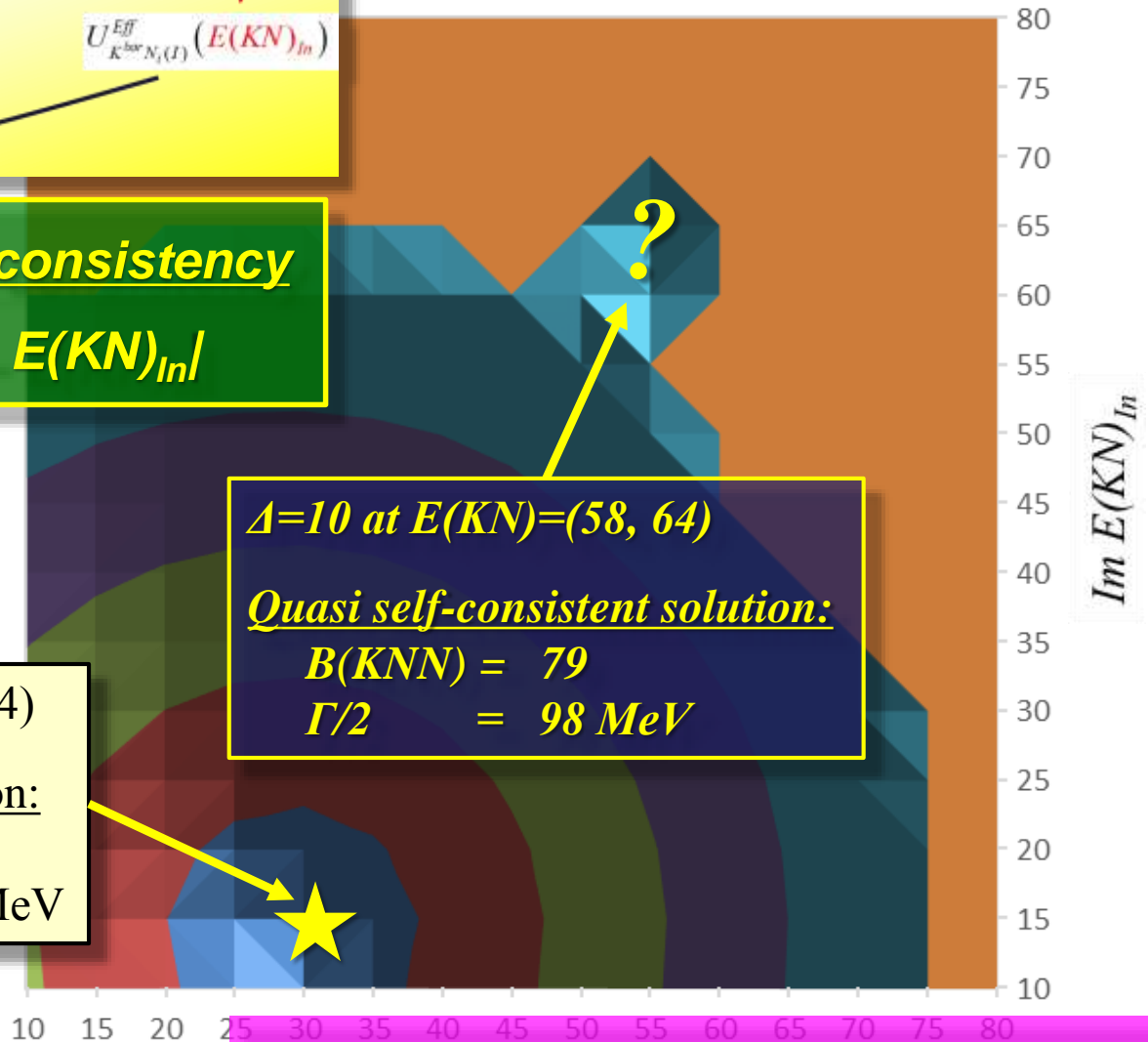
$$\Gamma/2 = 18.9 \text{ MeV}$$

$\Delta=10$ at $E(KN)=(58, 64)$

Quasi self-consistent solution:

$$B(KNN) = 79$$

$$\Gamma/2 = 98 \text{ MeV}$$



“Double pole of K -pp” ?

Double-pole structure in “K-pp”?

- ✓ Quasi self-consistent solution is obtained ...
 $(B(KNN), \Gamma/2) = (62 \sim 79, 74 \sim 104)$ MeV for $f_\pi = 90 \sim 120$ MeV
with Particle picture
- ✓ Such solutions are not obtained with Field picture.

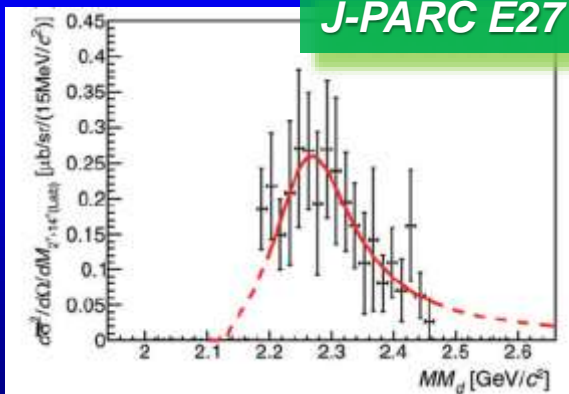
- A Faddeev-AGS calc. has predicted the double-pole structure of “K-pp”.

Lower pole : $(B(KNN), \Gamma/2) = (67 \sim 89, 122 \sim 160)$ MeV

Higher pole : $(B(KNN), \Gamma/2) = (9 \sim 16, 17 \sim 23)$ MeV

Y. Ikeda, H. Kamano, and T. Sato, PTP 124, 533 (2010)

- Relation to signals observed by J-PARC E27, DISTO?



Lower pole of “K-pp” ($J^\pi=0^-, l=1/2$)
... “K-pp” has two poles similarly to $\Lambda(1405)$.
The lower pole appears.

Partial restoration of chiral symmetry

... $K^{\text{bar}}N$ potential is enhanced by 17%.

S. Maeda, Y. Akaishi, T. Yamazaki, Proc. Jpn. Acad., Ser. B 89, 418 (2013)

Pion assisted dibaryon “ $Y = \pi\Sigma N - \pi\Lambda N$ ($J^\pi=2^+, l=3/2$)”

A. Gal, arXiv:1412.0198 (Proceeding of EXA2014)

Signal at ~ 100 MeV below $K^{\text{bar}}NN$ thr.

***5. Summary
and future plans***

5. Summary

A prototype of K^{bar} nuclei “ K^-pp ” = Resonance state of $K^{\text{bar}}NN-\pi YN$ coupled system

“ K^-pp ” is theoretically investigated in various ways:

Chiral SU(3)-based potential (E-dep.)	→ Shallow binding ... $B(K^-pp) = 10\sim 25$ MeV
Phenomenological potential (E-indep.)	→ Deep binding ... $B(K^-pp) = 50\sim 90$ MeV

All theoretical studies predict $B(K^-pp) < 100$ MeV.

K^-pp studied with “coupled-channel Complex Scaling Method + Feshbach projection”

- Used a Chiral SU(3)-based potential (Gaussian form in r -space)
- Self-consistency for $K^{\text{bar}}N$ **complex** energy (Field and Particle pictures)

K^-pp ($J^\pi=0^-, T=1/2$) ... $(B, \Gamma/2) = (20\sim 30, 10\sim 30)$ MeV (Martin constraint)
(15~22, 10~25) MeV (SIDDHATA constraint)

- Quasi self-consistent solution with Particle picture
... Deeper binding and larger decay width

K^-pp ($J^\pi=0^-, T=1/2$) $(B, \Gamma/2) = (60\sim 80, 75\sim 105)$ MeV (Martin constraint)

“ K^-pp ” has a double-pole structure similarly to $\Lambda(1405)$?

- Relation to the K^-pp search experiments

The signal observed in J-PARC E27 is considered to correspond to the lower pole of “ K^-pp ”??
J-PARC E15 may pick up the higher pole of “ K^-pp ”???

5. Future plans

- Full-coupled channel calculation of $K\bar{p}p$
... Detailed study for the double pole structure of $K\bar{p}p$
- Application to resonances of other hadronic systems



Thank you for your attention!

References:

1. A. D., T. Inoue, T. Myo,
NPA 912, 66 (2013)
2. A. D., T. Myo, NPA 930, 86 (2014)
3. A. D., T. Inoue, T. Myo,
PTEP 2015, 043D02 (2015)

Cats in KEK