

2016/08/09

The 34st Reimei Workshop

Heavy flavor measurements at PHENIX

K.Nagashima

Hiroshima Univ./RIKEN

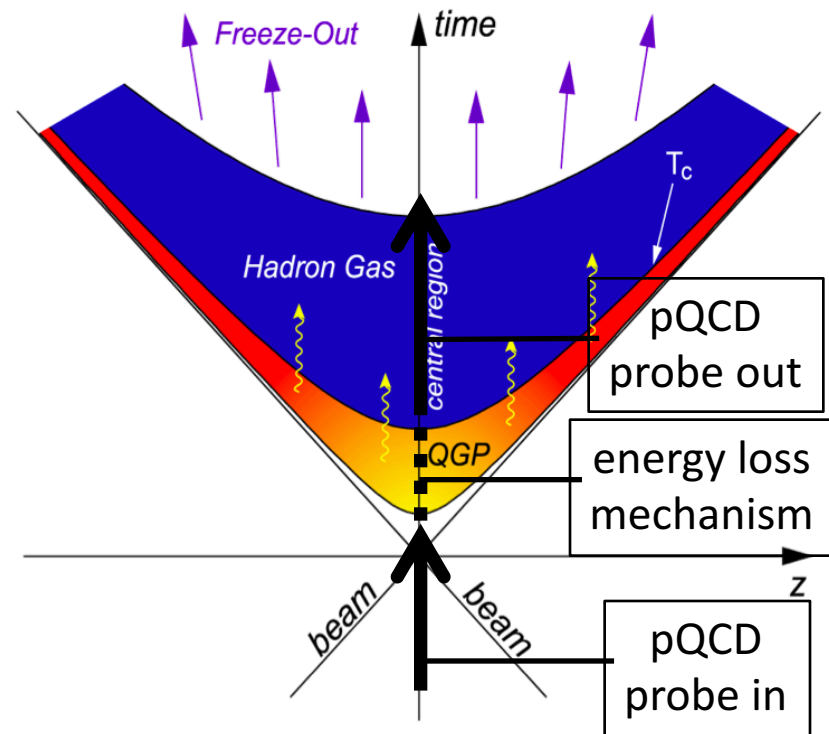
✓ Introduction of heavy flavor measurements

Heavy flavor probe

- > large mass
 - $m_{c,b} \gg \Lambda_{\text{QCD}} (\gg T_{\text{QGP}})$
 - $1/2 m_{c,b} \ll \tau_{\text{form}}$
 - hardly generated in QGP
 - thorough time evolution
- > allows some pQCD calculation
model = pQCD + energy loss model

QGP physical property

- > HF momentum and space variation \rightarrow QGP property
- > model parameters
 - Diffusion constant
 - Gluon density



✓ Quark energy loss mechanism in QGP

collisional energy loss

- parton elastic scattering
- Brownian motion via Langevin equation

$$\frac{d\vec{p}}{dt} = -\eta_D(p)\vec{p} + \vec{\xi} \quad \begin{array}{l} \eta_D: \text{friction coefficient} \\ \xi: \text{drift force} \end{array}$$

radiative energy loss

- Bathe-Heitler for gluon radiation

$$dP_0 \approx \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{dk_{\perp}^2}{k_{\perp}^2}$$

> Dead-Cone effect

- strong suppression of HF in small-angle radiation

$$\propto \frac{k_{\perp}^2 dk_{\perp}^2}{(k_{\perp}^2 + \omega^2 \theta_0^2)^2}, \quad (\theta_0 \equiv \frac{M}{E})$$

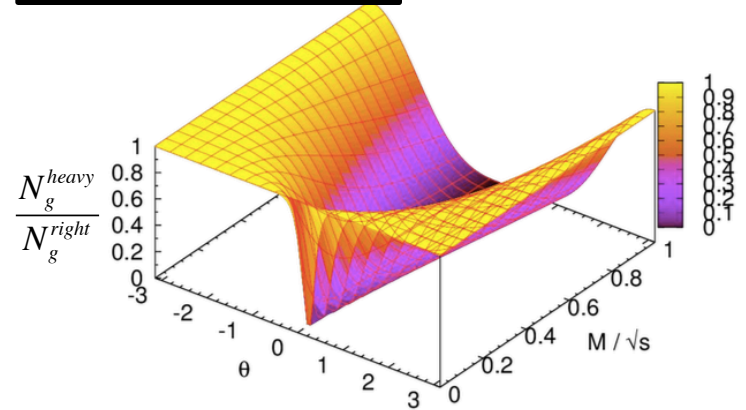
> Landau-Pomeranchuk-Migdal effect

- suppression in high density $\propto \frac{\lambda_{\text{path}}}{L_{\text{form}}}$

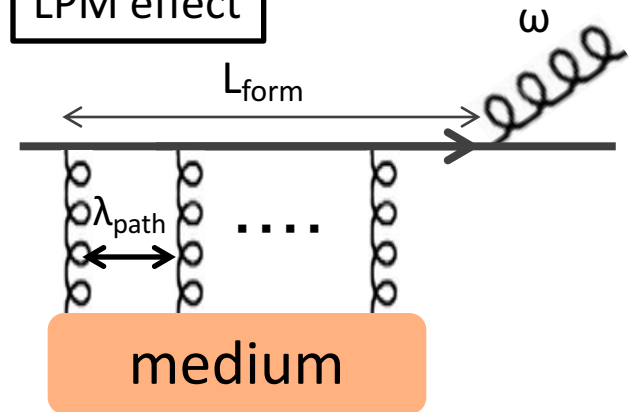
mass ordering

$$\Delta E_g > \Delta E_{u,d,s} > (?) \Delta E_c > (?) \Delta E_b$$

Dead-Cone effect

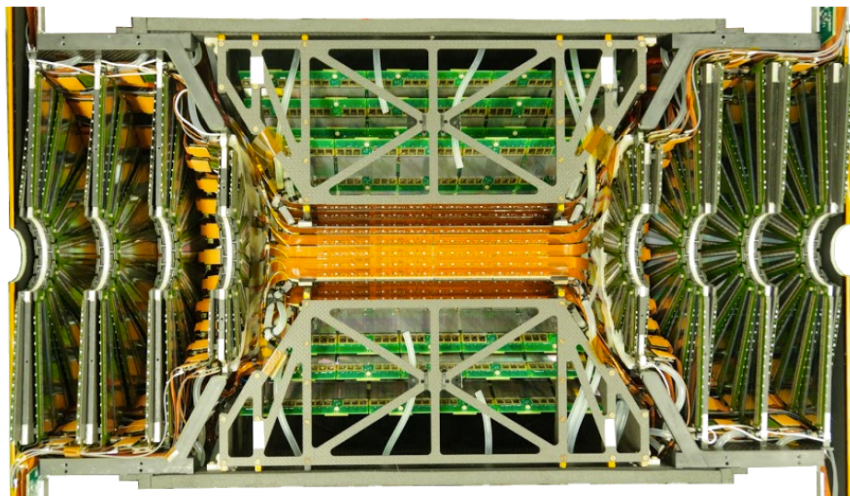


LPM effect



λ_{path} : mean free path
 L_{form} : formation length

✓ PHENIX Silicon Vertex Detector (VTX)

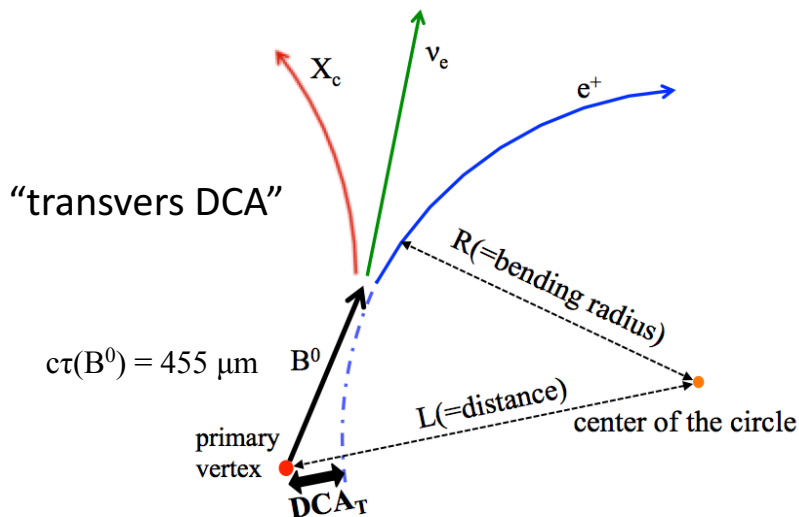


Silicon Vertex Detector (VTX)

- installed in 2011
- 2 pixel layers + 2 strip layers
($\sigma_\phi = 14.4 \mu\text{m}$) ($\sigma_\phi = 23 \mu\text{m}$)
- reconstruct precise collision vertex

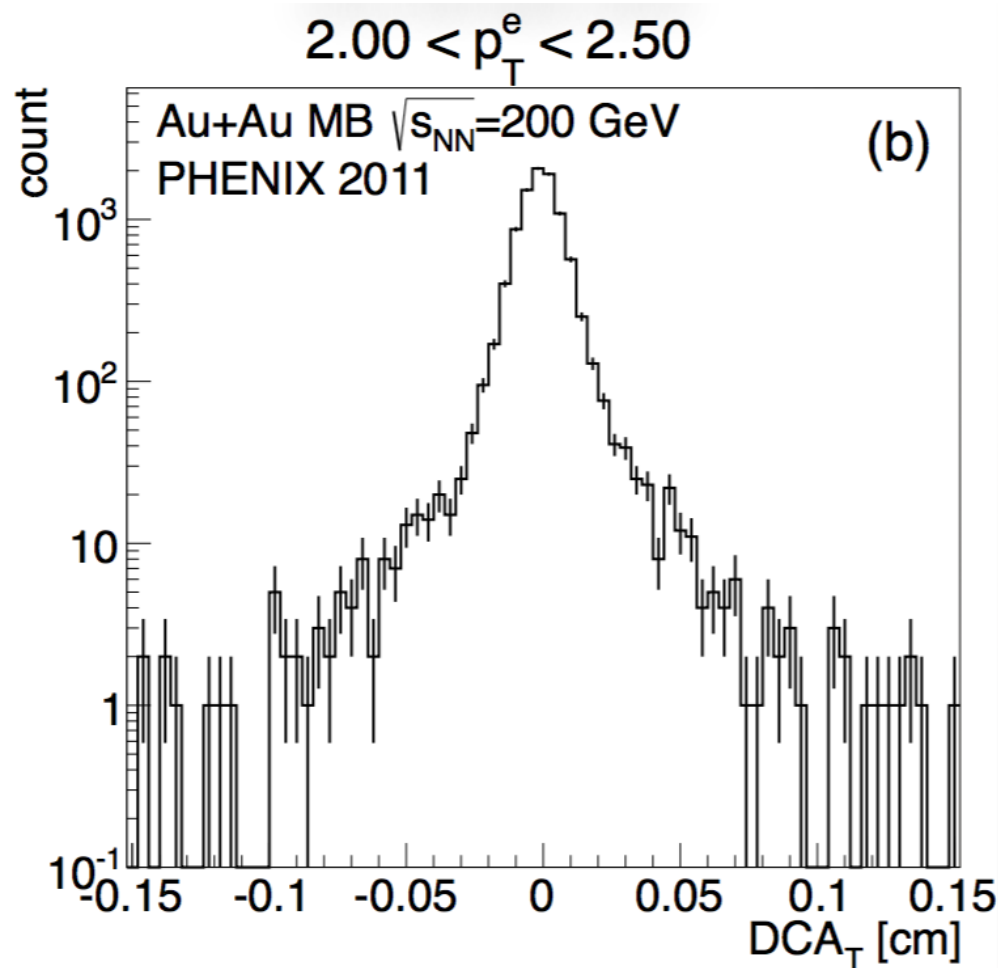
Precise displaced tracking

- Distance of Closest Approach (DCA)
- Transverse DCA of a track is defined as
$$\text{DCA}_T = L - R$$
- depends on parent particle life time and mass
- DCA resolution = $60 \mu\text{m}$ @ 2.5 GeV
- DCA analysis allows separated measurement of bottom and charm



-> focus on single electron tracks
from smi-leptonic decay channels

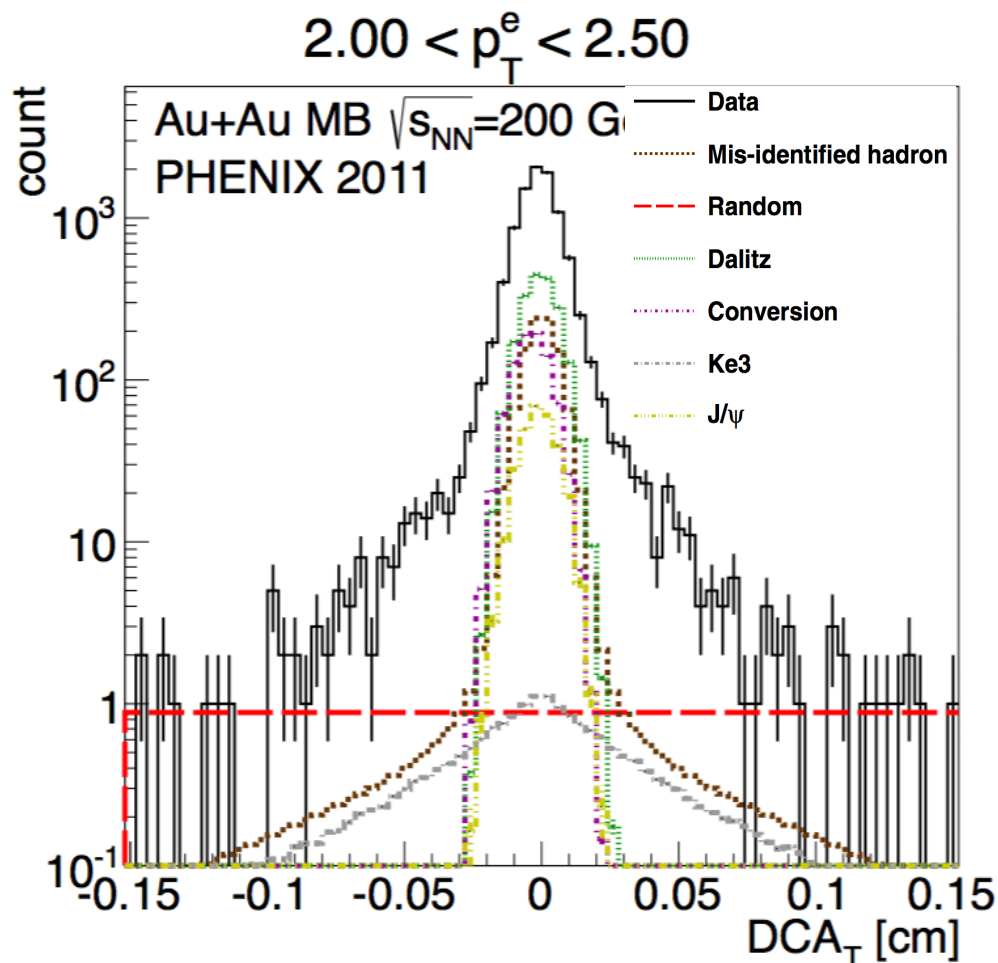
✓ DCA distribution of electrons



DCA distribution of electrons

- $1.5 < p_T < 5.0$
- no efficiency correction

✓ DCA distribution of electrons



DCA distribution of electrons

- $1.5 < p_T < 5.0$
- no efficiency correction

BG normalization and shape

- data driven
 - > Mis-hadron, Random
- measured yield + Monte Carlo
 - > Photonic, k_{e3} , J/ψ

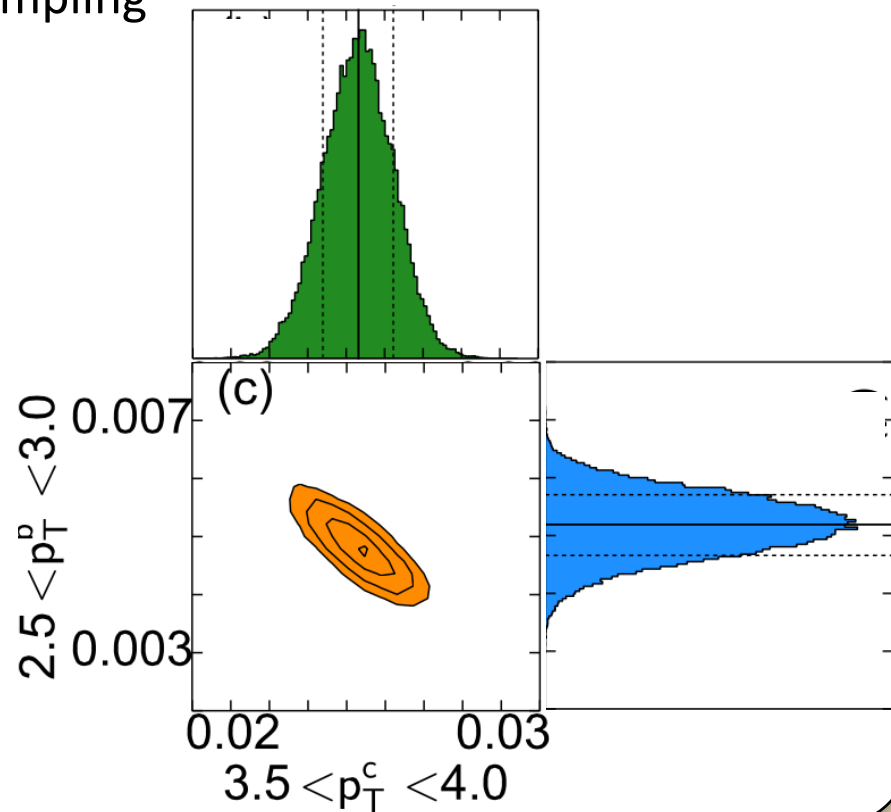
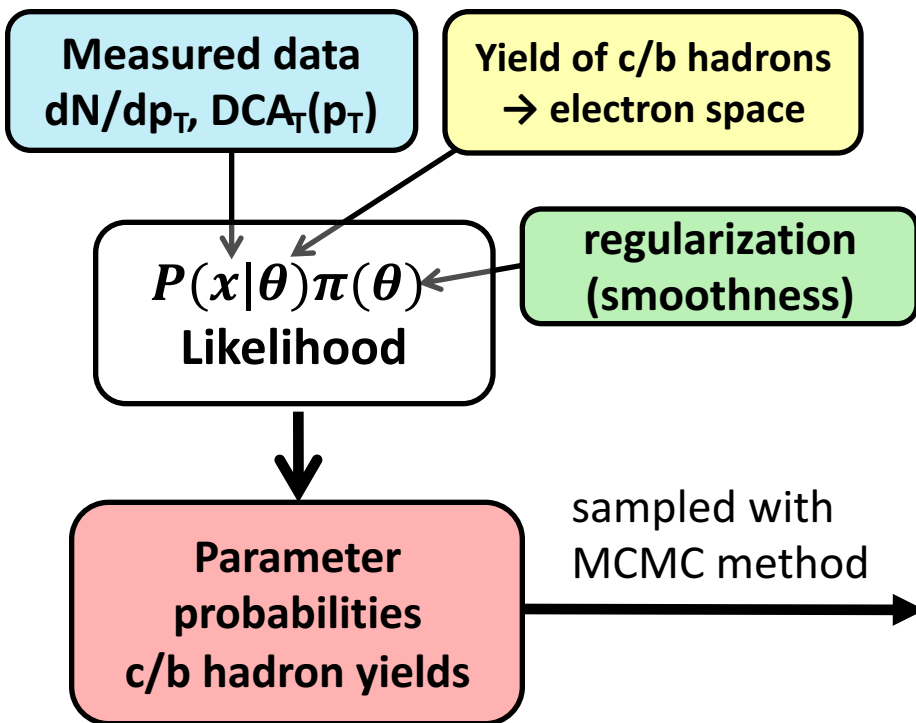
Heavy flavor decay electron

- dominates at $|0.04| < DCA_T < |0.1|$

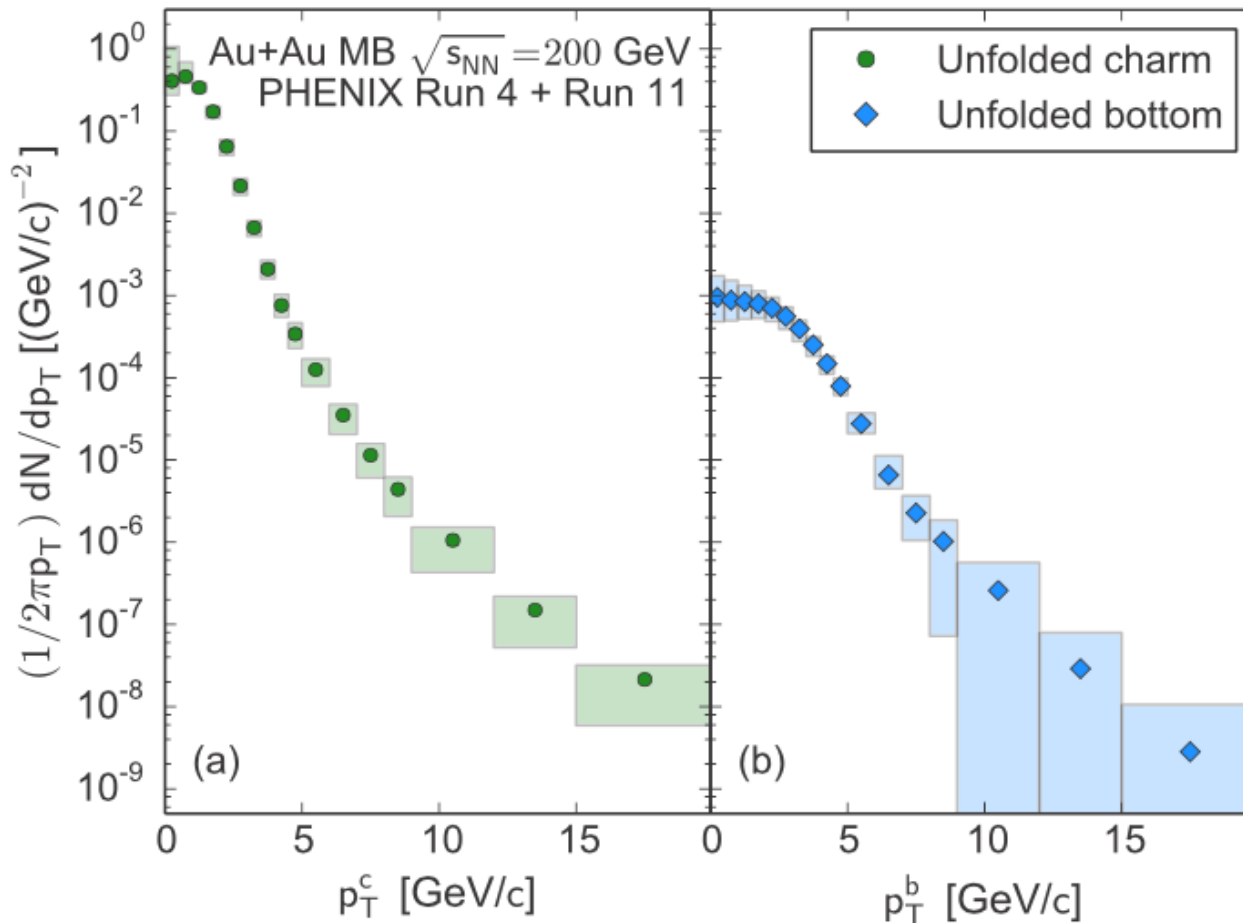
✓ Bayesian Inference

Bayesian Inference technique

- Bayes' theory $P(\theta|x) = \frac{P(x|\theta)\pi(\theta)}{P(x)}$
- c/b decay electron dN/dp_T , $DCA_T(p_T)$ from PHYTIA decay matrix
- employ Markov Chain Monte Carlo for sampling

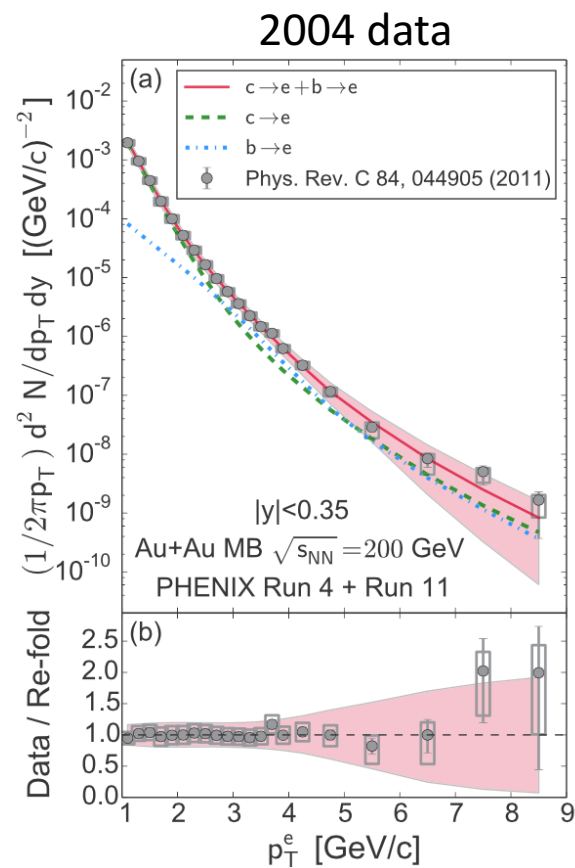
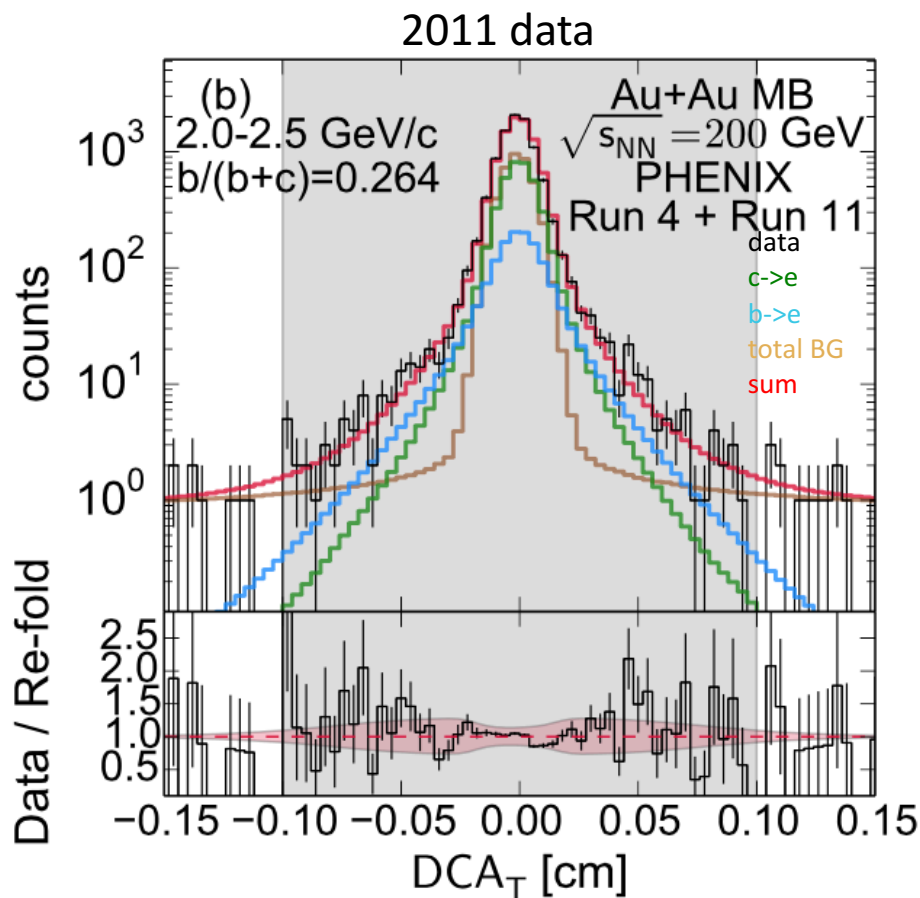


✓ Invariant yield of charm and bottom



Unfolded invariant yield of charm and bottom

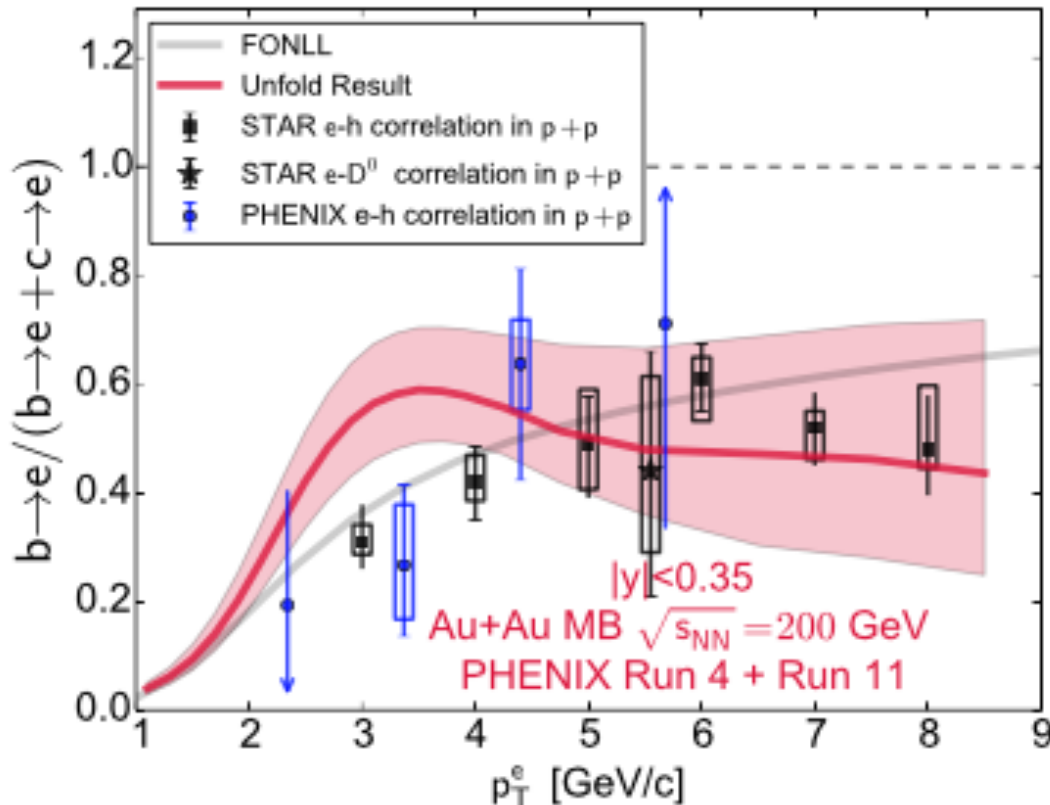
✓ Comparison between data and unfolding



Unfolding results agree with measured data well

✓ Bottom electron fraction

Bottom electron fraction



Fraction of bottom electrons

$$F = (b \rightarrow e) / (b \rightarrow e + c \rightarrow e)$$

p+p data

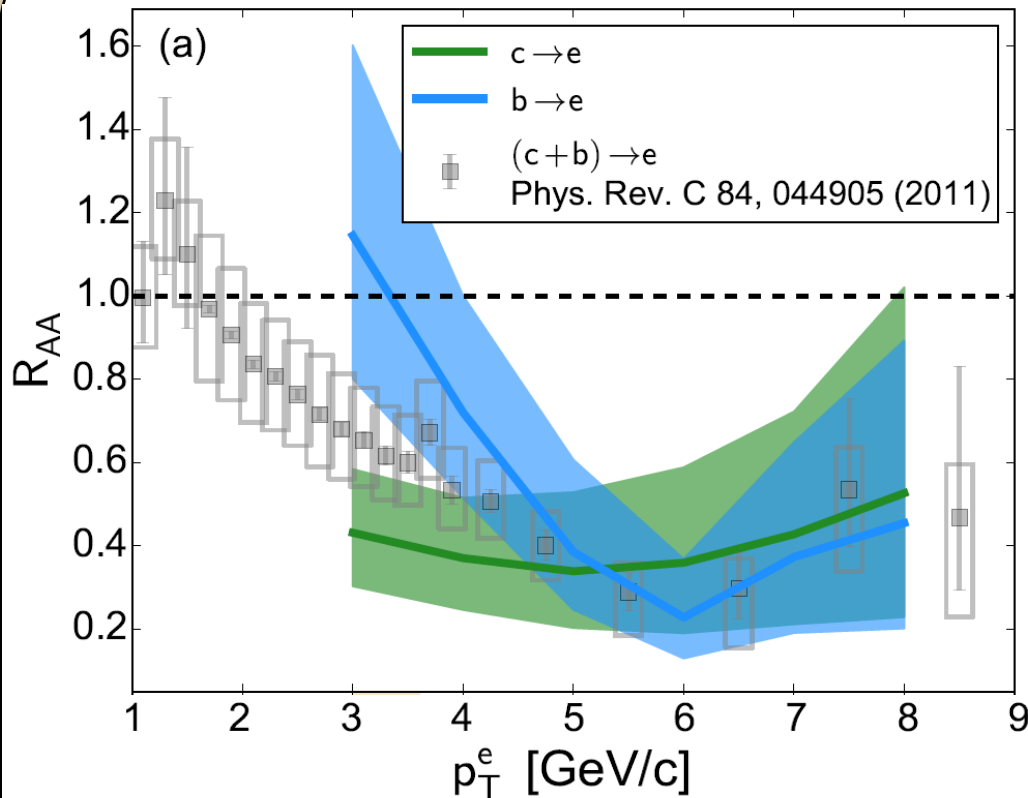
- not generate QGP
- agree with FONLL

Au+Au data (= unfolding)

- difference shape compared to p+p
- significant enhancement at 3 GeV/c
- consistent with p+p for high p_T

✓ Nuclear Modification Factor R_{AA}

Physical Review C93, 034904 (2016)



“Calculation of bottom and charm R_{AA} ”

- published inclusive HF R_{AA} (Run4)
- b-fraction of AuAu and pp(STAR e-h)

$$R_{AA}^{b \rightarrow e} = \frac{F_{AuAu}}{F_{pp}} R_{AA}^{HF}$$

$$R_{AA}^{c \rightarrow e} = \frac{(1-F_{AuAu})}{(1-F_{pp})} R_{AA}^{HF}$$

[$p_T < 4$ GeV/c]

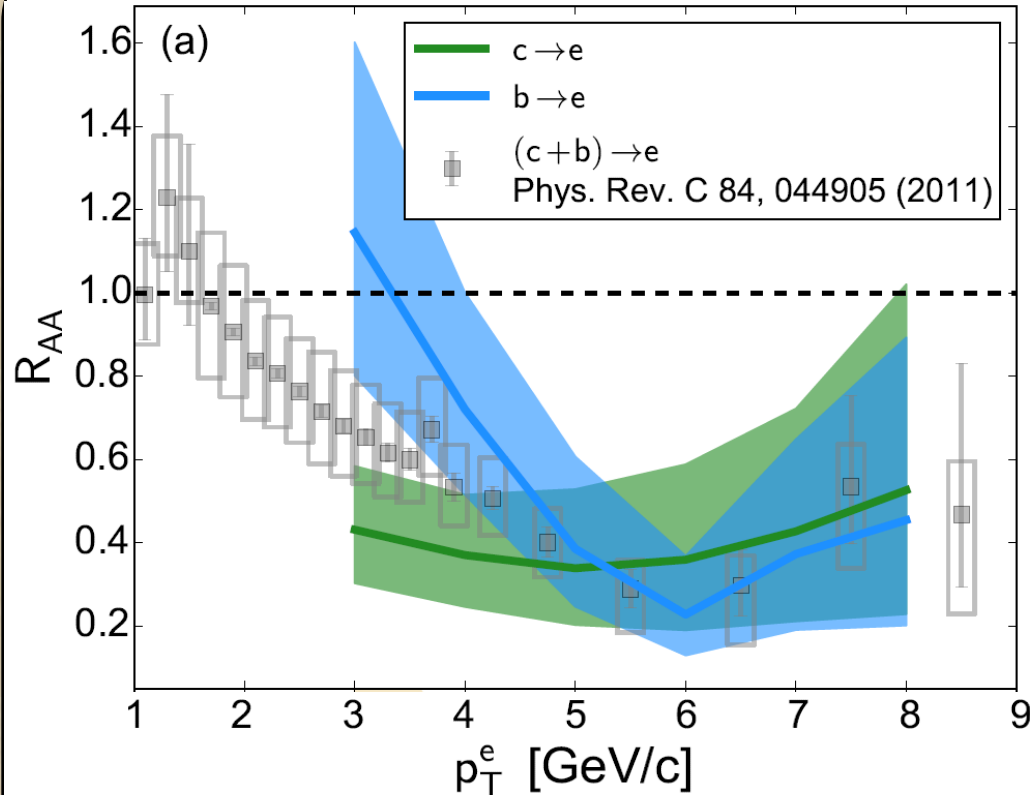
- bottom less suppressed than charm

[4 GeV/c $< p_T$]

- similarly suppressed

✓ Nuclear Modification Factor R_{AA}

Physical Review C93, 034904 (2016)



“Calculation of bottom and charm R_{AA} ”

- published inclusive HF R_{AA} (Run4)
- b-fraction of AuAu and pp(STAR e-h)

$$R_{AA}^{b \rightarrow e} = \frac{F_{AuAu}}{F_{pp}} R_{AA}^{HF}$$

$$R_{AA}^{c \rightarrow e} = \frac{(1-F_{AuAu})}{(1-F_{pp})} R_{AA}^{HF}$$

$[p_T < 4 \text{ GeV}/c]$

- bottom less suppressed than charm

$[4 \text{ GeV}/c < p_T]$

- similarly suppressed

- first measurements at RHIC

- > uncertainty is large

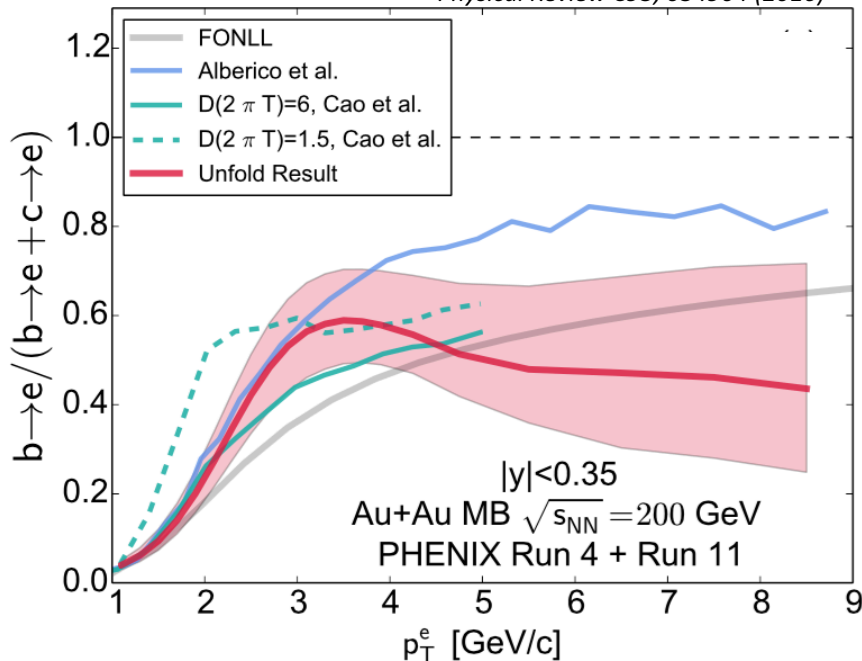
- need precise measurements to confirm mass ordering of c/b energy loss

- > we are analyzing high statistics and quality data (2014~2016)

✓ Comparison between data and models

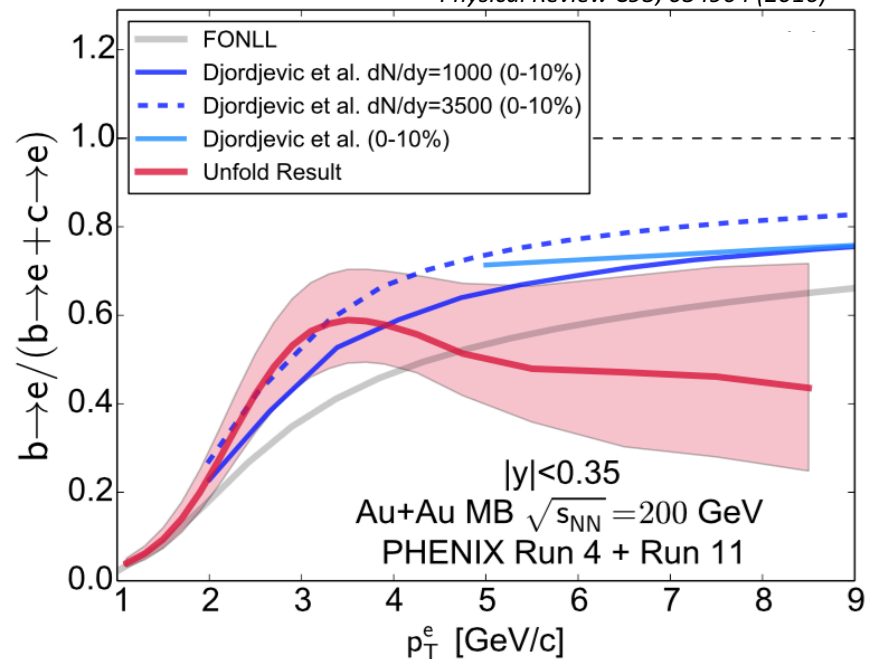
“Collisional energy loss”

Physical Review C93, 034904 (2016)



“Radiative energy loss”

Physical Review C93, 034904 (2016)



“Langevin equation”

- depend on diffusion constant D
- $D(2\pi T) = 6$ agree with data
- > strong coupling

“DGLV model (radiative only)”

- depend on gluon density in QGP
- $dN_g/dy = 1000 \sim 3500(?)$
- need more precise measurement...

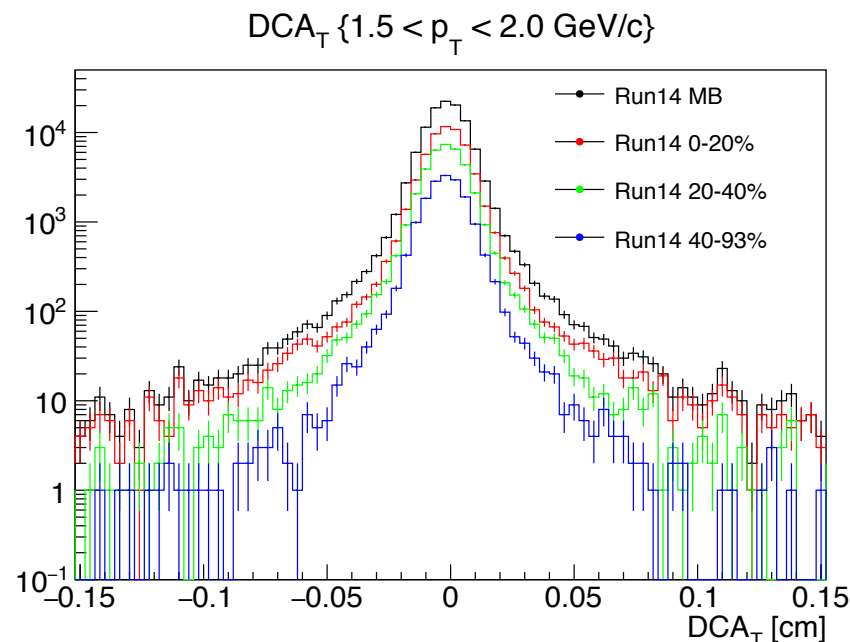
✓ Future Prospects

“High statics and quality data in 2014-2016”

- 2014 Au+Au data x10 statistics compared to 2011
 - > broader p_T range (1.0 – 9.0 GeV/c)
 - > update invariant yields of HF with centrality and angle
 - > suppress sys. uncertainty with new BG normalization
- 2015 p+p data
 - > new base line (same method)

“Analysis goal”

- centrality dependence of R_{AA}
- v_n measurements
 - > strong constraint to QGP physical property, $D(2\pi T)$, $dN_g/d\eta$

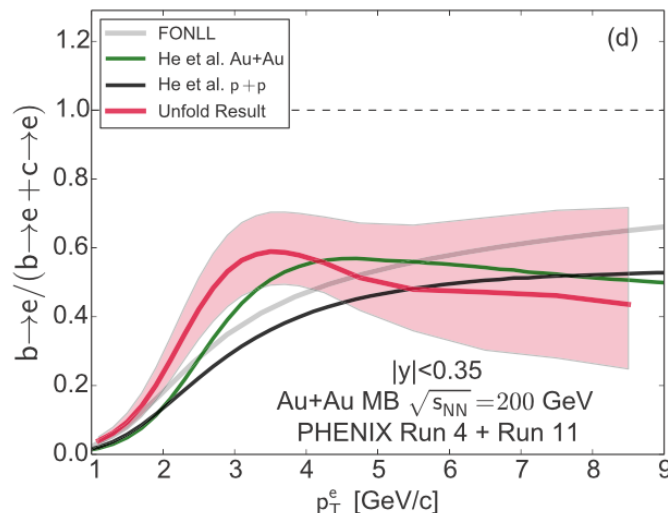
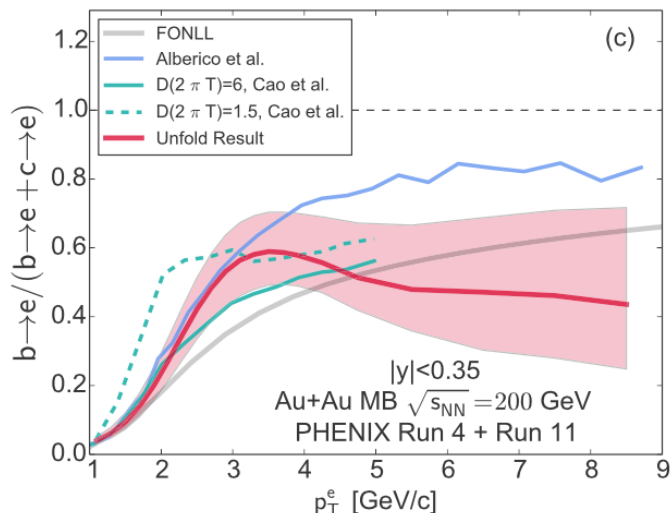
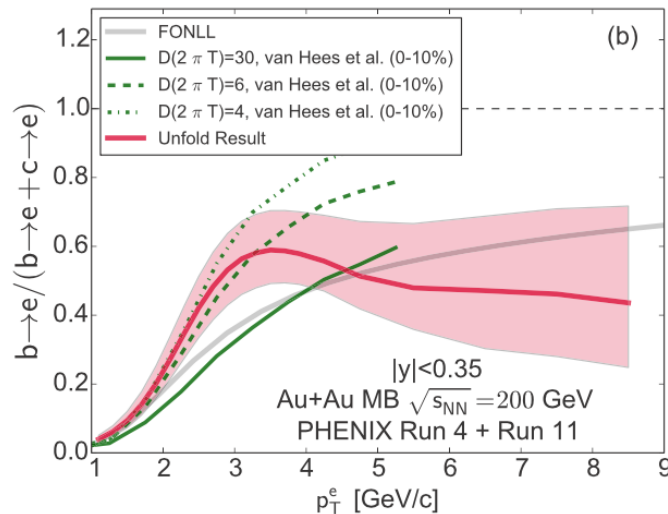
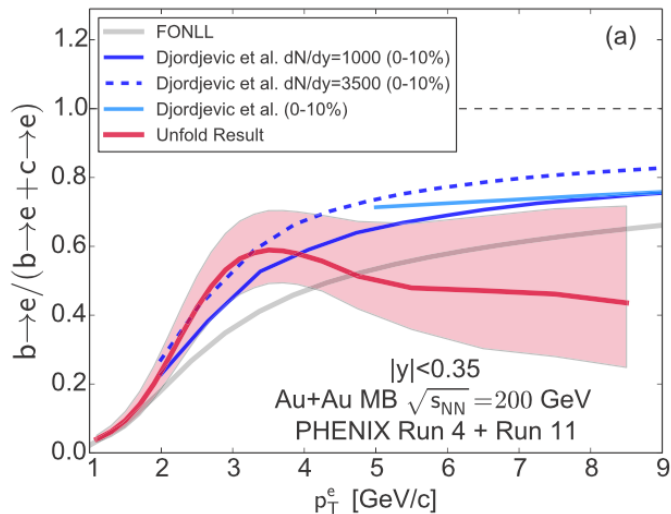


✓ Summary

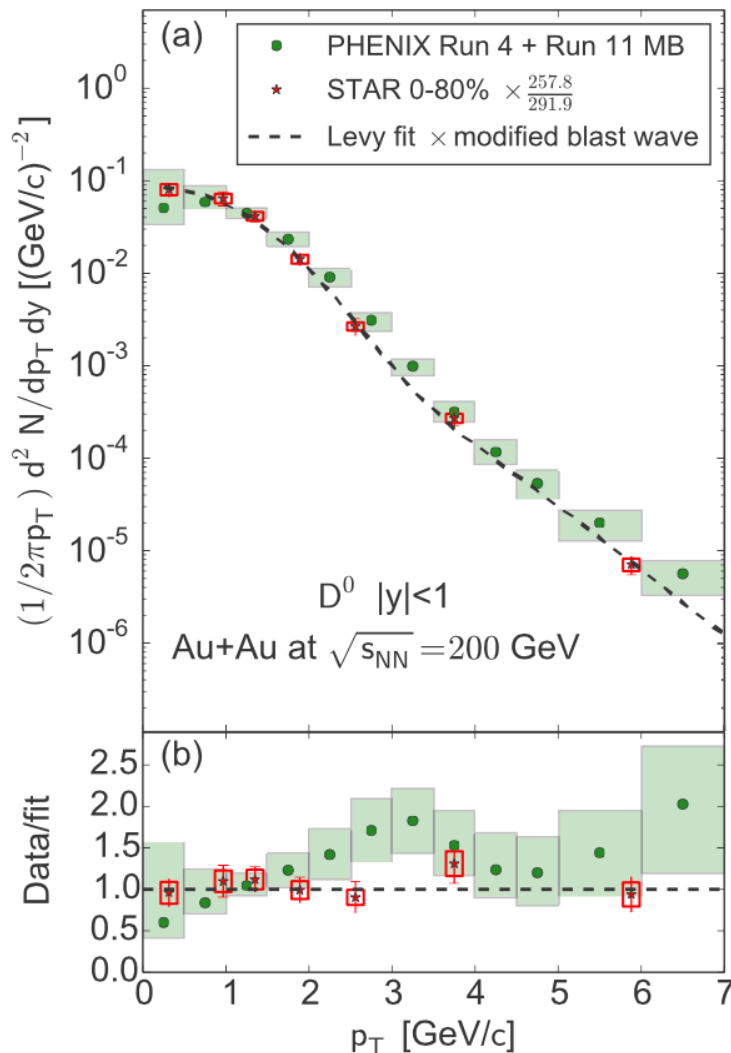
- Heavy flavor is important probe for Quark-Gluon Plasma
- Quark energy loss mechanism
 - Langevin equation → collisional energy loss
 - Bathe Heitler → radiative energy loss
- Measurement of single electrons from charm and bottom
 - used distance of closest approach and Bayesian inference
 - **bottom suppression is similar to charm at high p_T , but smaller than charm at low p_T**
 - compare between data and energy loss models
 - > **$D(2\pi T) \sim 6$** , gluon density = 1000~3500
- Future prospects
 - high statistics data (~10 times) in 2014

✓ backup

✓ Comparison between data and models



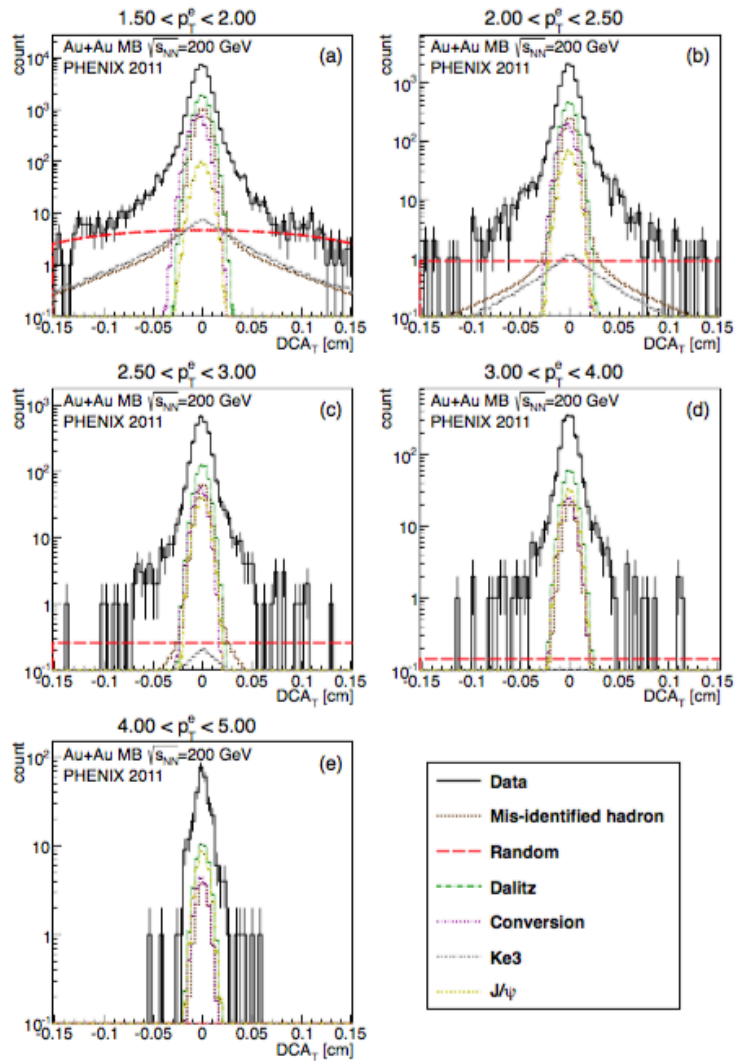
✓ Agreement with measured data



- Yields of D^0 can be calculated by unfolding charm yields + PYTHIA
- Unfolding result agree with STAR D^0 measurement > fit Levy function

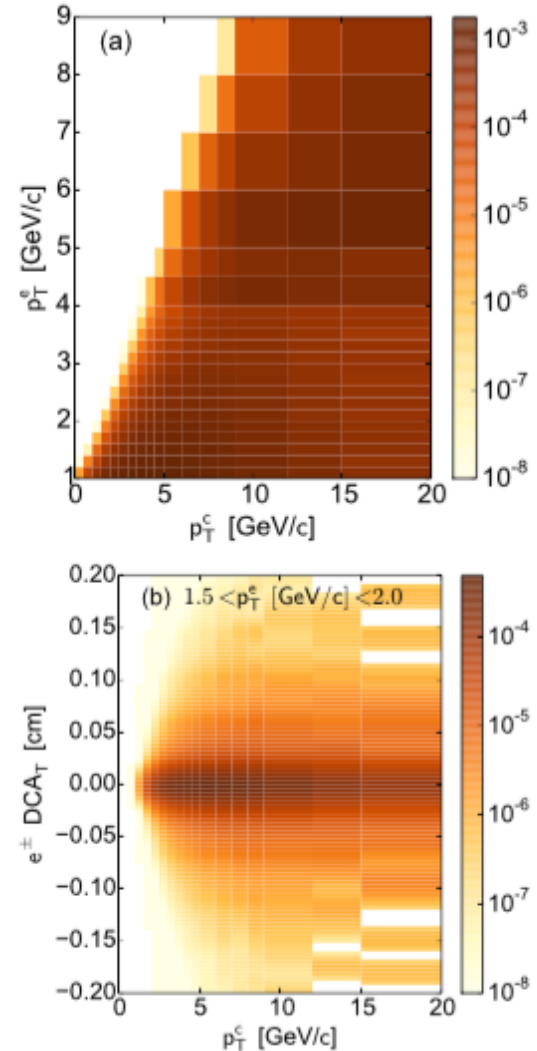
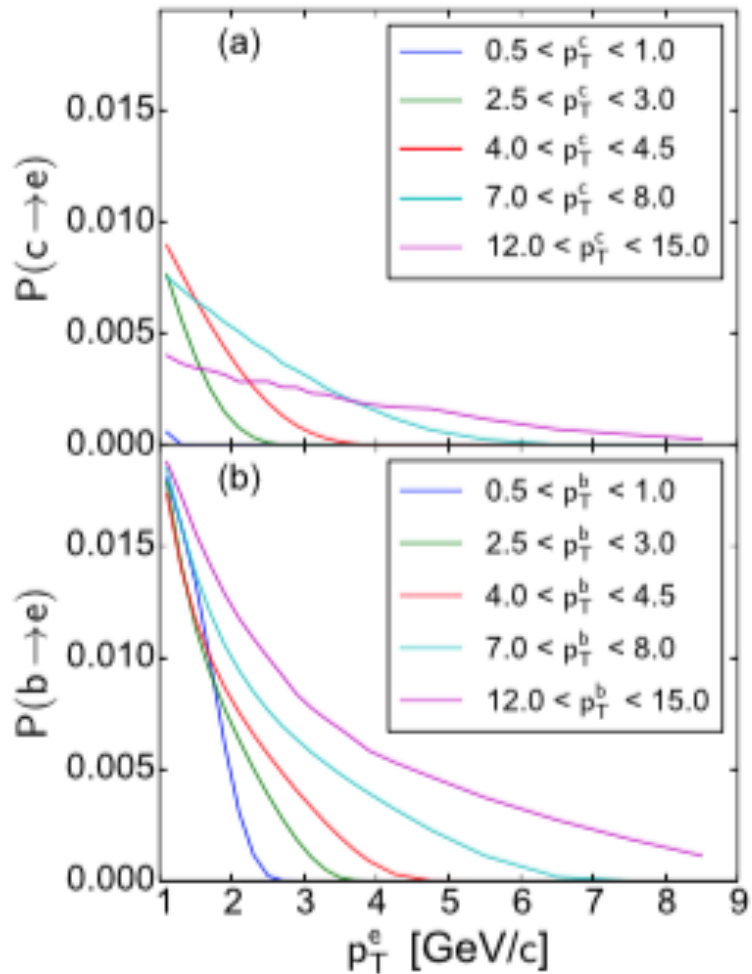
$$f(p_T) = p_0 \left[1 - \frac{(1 - p_1)p_T}{p_2} \right]^{1/(1-p_1)} \times \left[1.3\sqrt{2\pi p_4^2} G(p_T, p_3, p_4) + \frac{p_5}{1 + e^{-p_T+3}} \right],$$

✓ DCA distribution



✓ Decay matrix

decay electron pT matrix



✓ Bayesian Inference

[Bayes' theory]

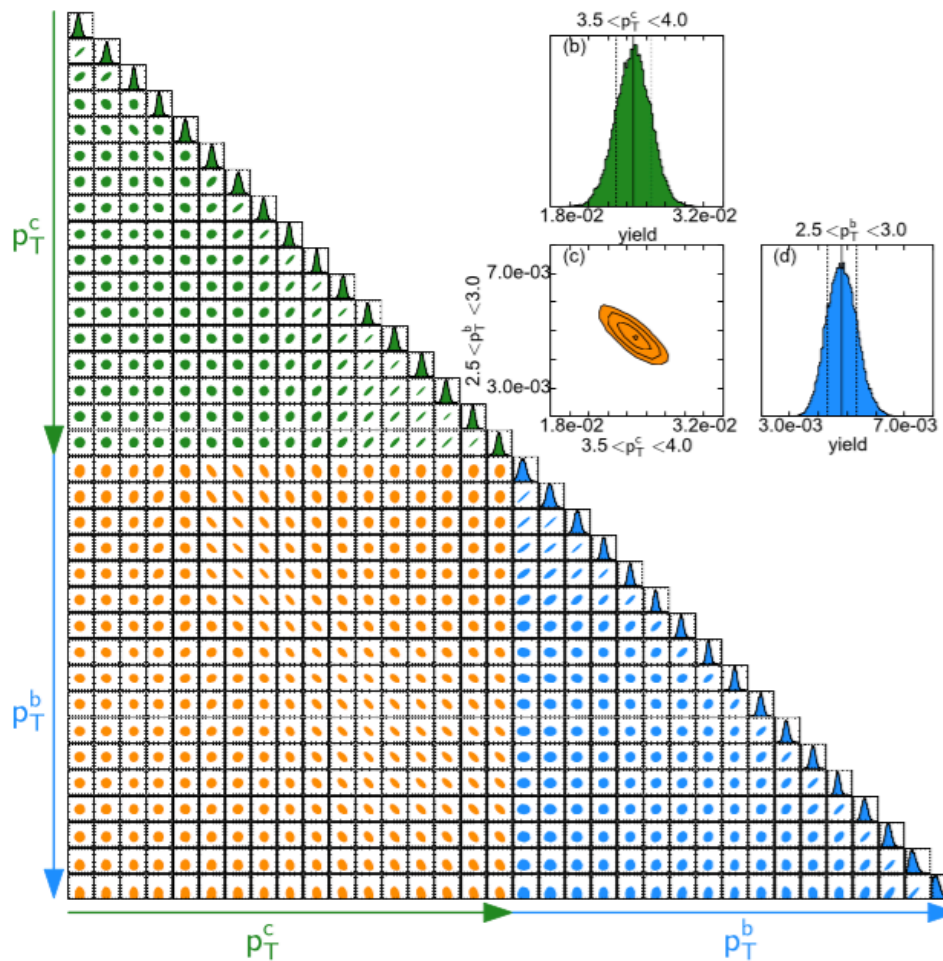
$$P(\theta | x) = \frac{P(x | \theta) P(\theta)}{P(x)}$$

- $P(\theta | x)$: posterior probability
- $P(x | \theta)$: likelihood
- $P(\theta)$: prior probability
- $P(x)$: normalization factor

Prior, $P(\theta)$

$$L = \frac{17}{2} \begin{pmatrix} -1 & 1 & & & & & & & & & \\ & 1 & -2 & 1 & & & & & & & \\ & & 1 & -2 & 1 & & & & & & \\ & & & \dots & \dots & \dots & & & & & \\ & & & & & \dots & \dots & \dots & & & \\ & & & & & & 1 & -2 & 1 & & \\ & & & & & & & 1 & -2 & 1 & \\ & & & & & & & & 1 & -1 & \end{pmatrix}$$

likelihood, $P(x | \theta)$



✓ Dead-Cone effect

light quark radiation

$$dP_0 \simeq \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{dk_{\perp}^2}{k_{\perp}^2} = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{d\theta^2}{\theta^2}$$

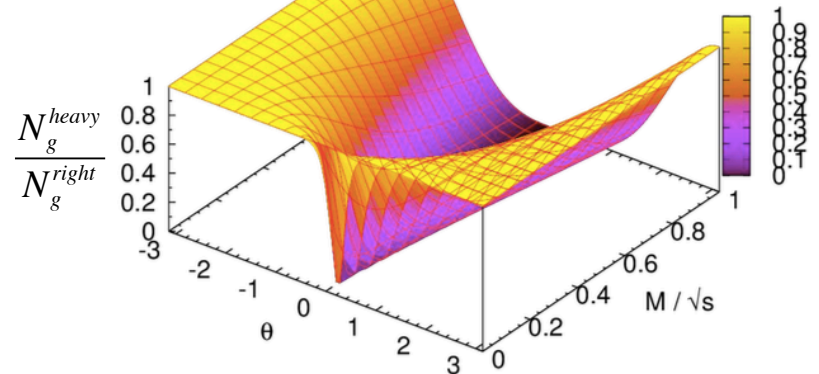
radiation including mass effect

$$dP = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{k_{\perp}^2 dk_{\perp}^2}{(k_{\perp}^2 + \omega^2 \theta_0^2)^2}, \quad \theta_0 \equiv \frac{M}{E}$$

heavy quark radiation

$$dP_{\text{HQ}} = dP_0 \cdot \left(1 + \frac{\theta_0^2}{\theta^2} \right)^{-2}$$

Dead-Cone effect



✓ Collisional energy loss

Brownian motion

- Langevin equation

$$\frac{d\vec{p}}{dt} = -\eta_D(p)\vec{p} + \vec{\xi}$$

η_D : coefficient of friction, ξ : drift force

- diffusion coefficient

$$D = \frac{T}{M\eta_D(0)} = \frac{2T^2}{k}$$

✓ Markov Chain Monte Carlo

Markov Chain

- Markov process = present status depend on previous status only

Algorithm

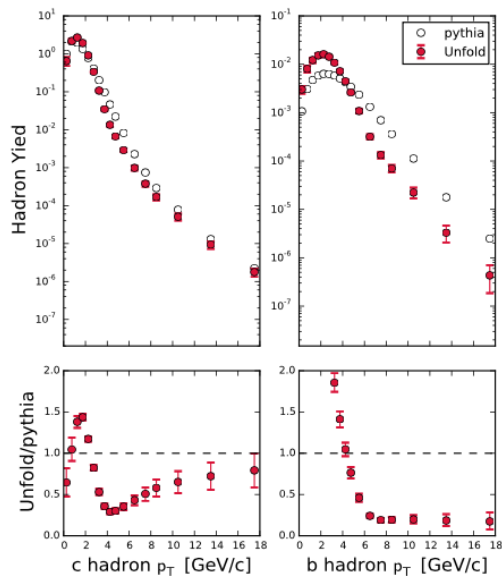
- make a initial input (c/b invariant yields) with PYHIA

- calculate Log likelihood

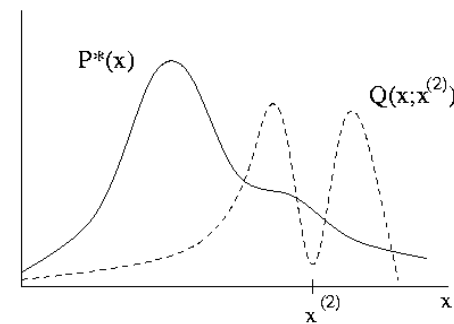
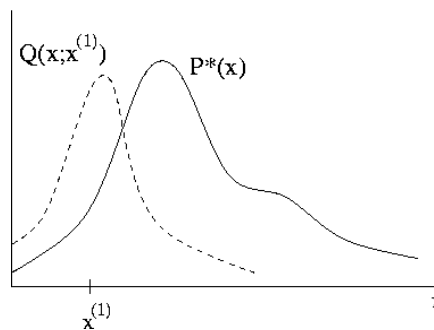
- compare between present Log likelihood and previous log likelihood

present > previous -> employ present parameters

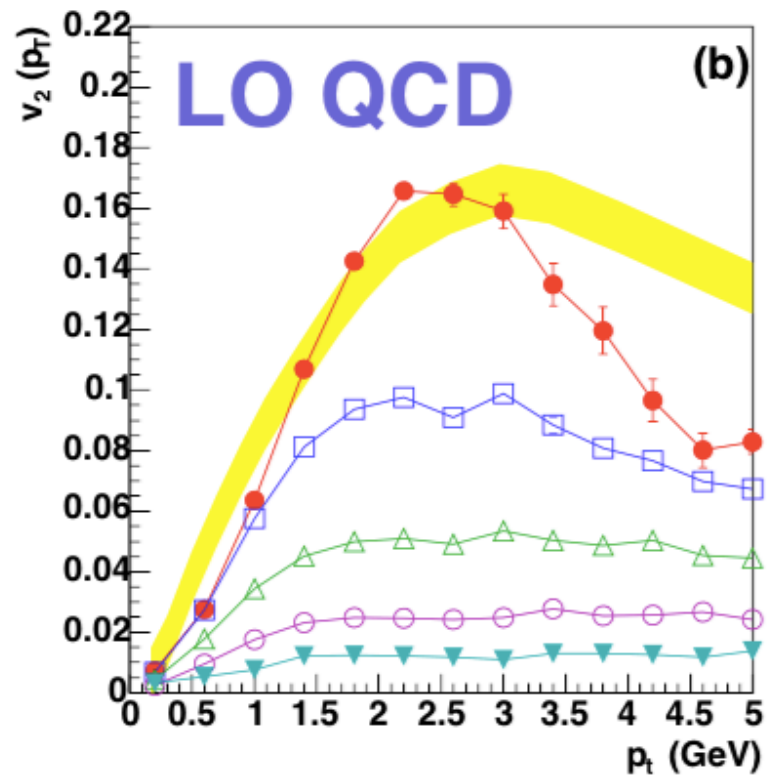
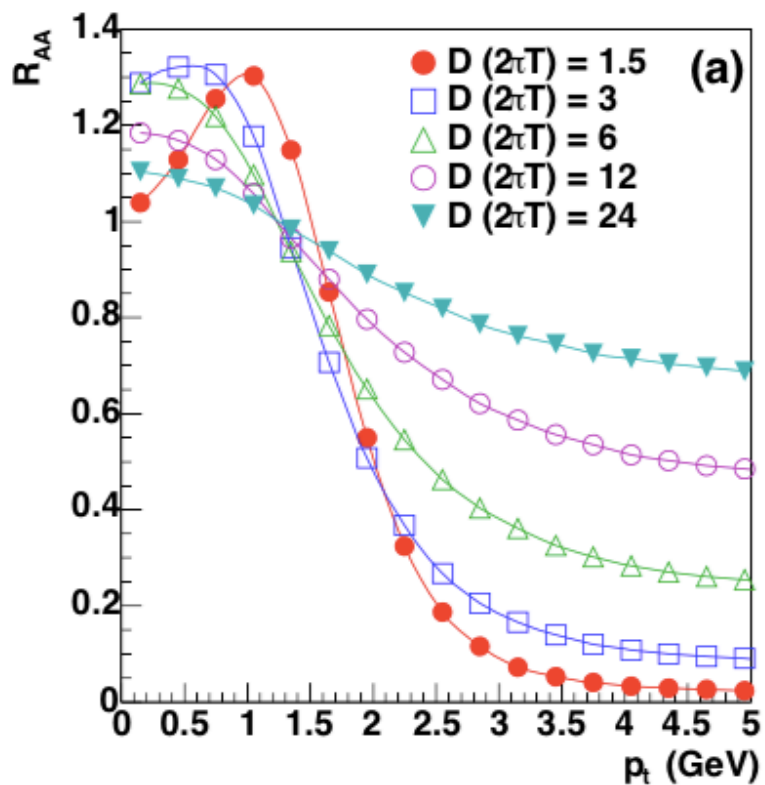
present < previous -> reject present parameters and employ previous parameters



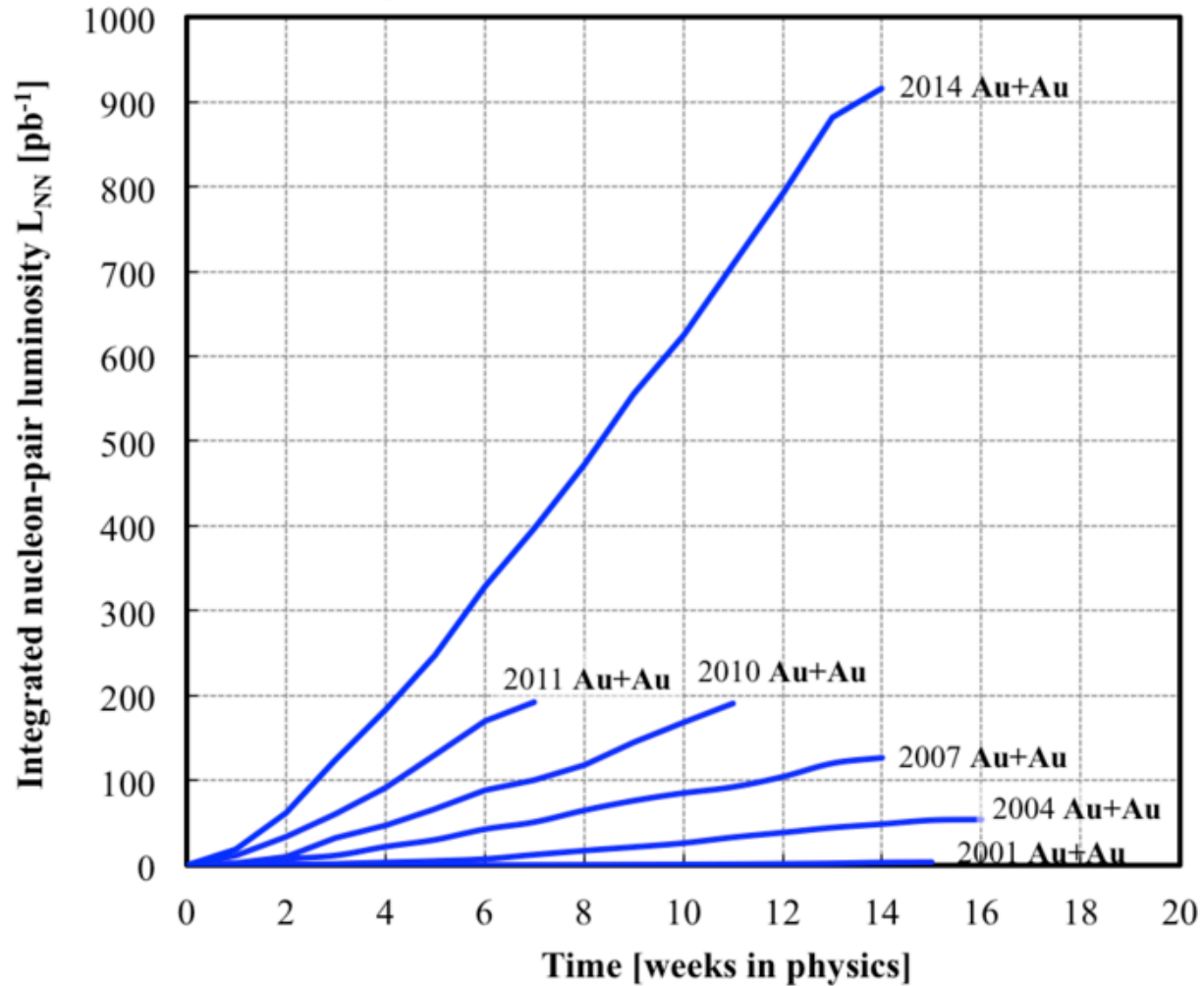
Metropolis-Hasting Algorithm

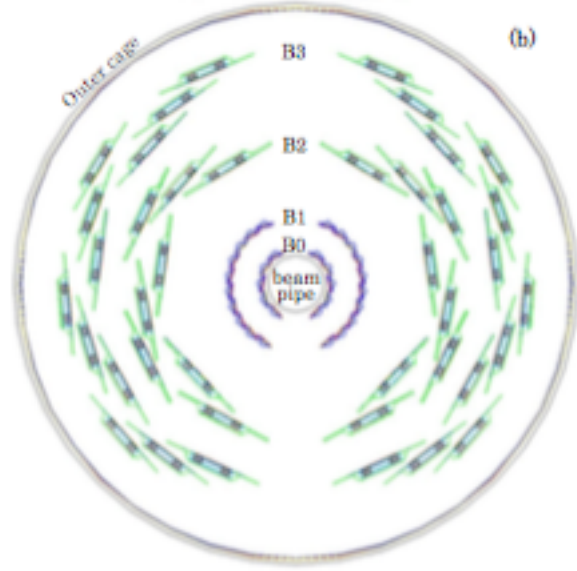
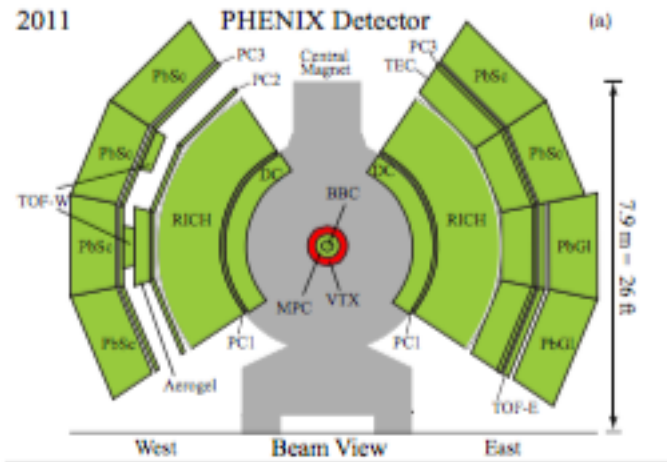


✓ Diffusion constant

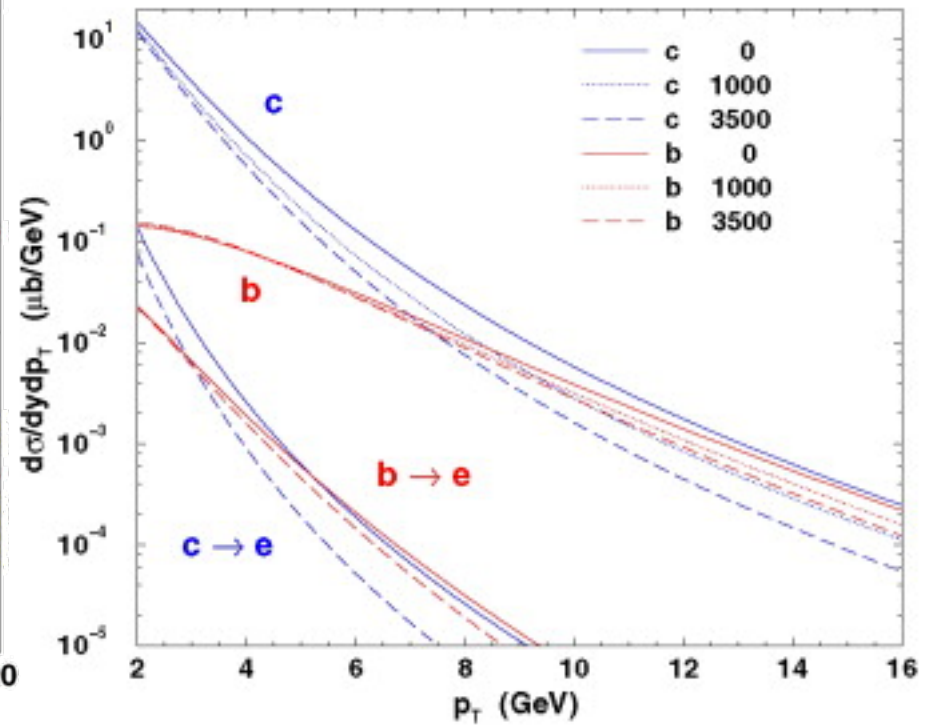
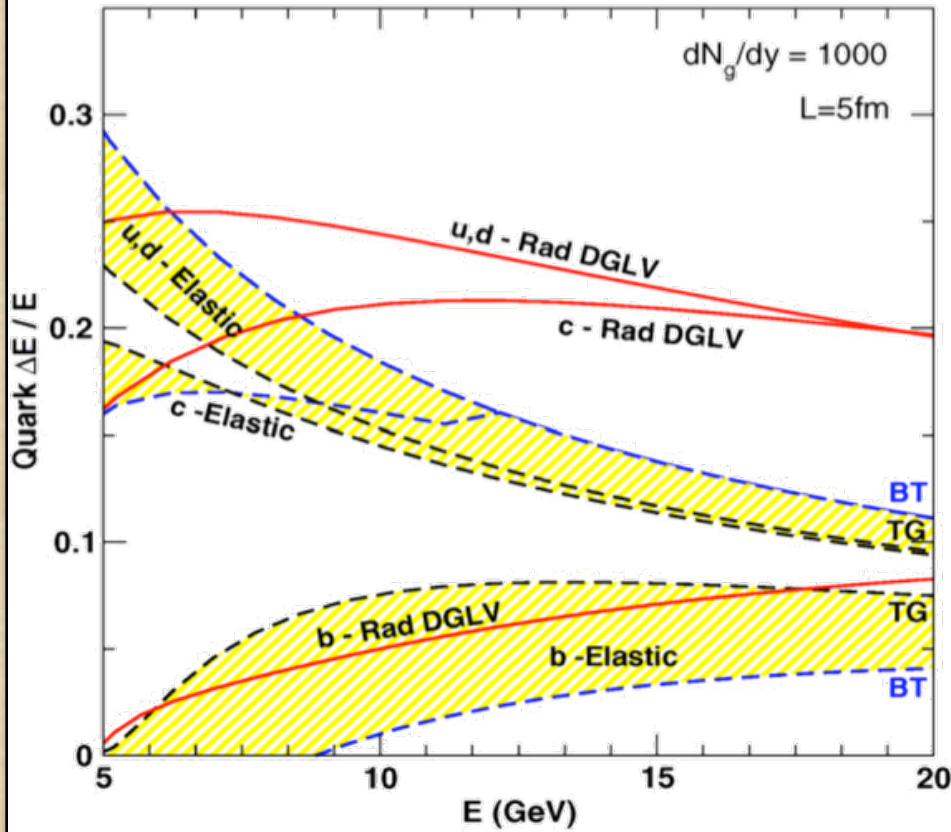


Heavy ion runs - time evolution of Au+Au





✓ Energy loss model



✓ Quark energy loss mechanism in QGP

+ collisional energy loss

- parton elastic scattering
- Brownian motion via Langevin equation

$$\frac{d\vec{p}}{dt} = -\eta_D(p)\vec{p} + \vec{\xi} \quad \begin{array}{l} \eta_D: \text{friction coefficient} \\ \xi: \text{drift force} \end{array}$$

+ radiative energy loss

- Bathe-Heitler for gluon radiation
- Landau-Pomeranchuk-Migdal effect
- > suppression of radiation in high density

$$dP_0 \approx \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{dk_{\perp}^2}{k_{\perp}^2} \times \frac{\lambda_{\text{path}}}{L_{\text{form}}}$$

- Dead-Cone effect

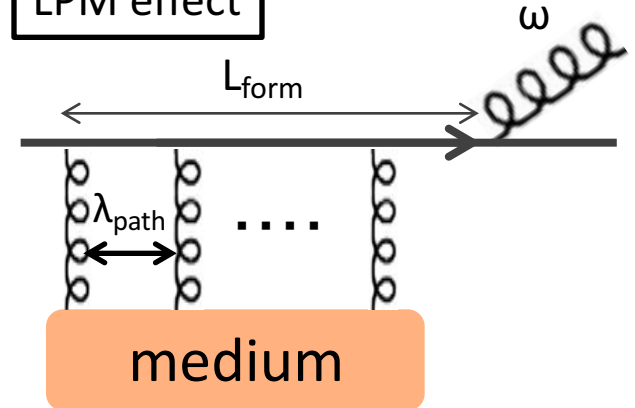
-> strong suppression of small-angle radiation

$$dP = \frac{\alpha_s C_F}{\pi} \frac{d\omega}{\omega} \frac{k_{\perp}^2 dk_{\perp}^2}{(k_{\perp}^2 + \omega^2 \theta_0^2)^2} \quad \theta_0 \equiv \frac{M}{E}$$

mass ordering

$$\Delta E_g > \Delta E_{u,d,s} > (?) \Delta E_c > (?) \Delta E_b$$

LPM effect



λ_{path} : mean free path
 L_{form} : formation length

Dead-Cone effect

