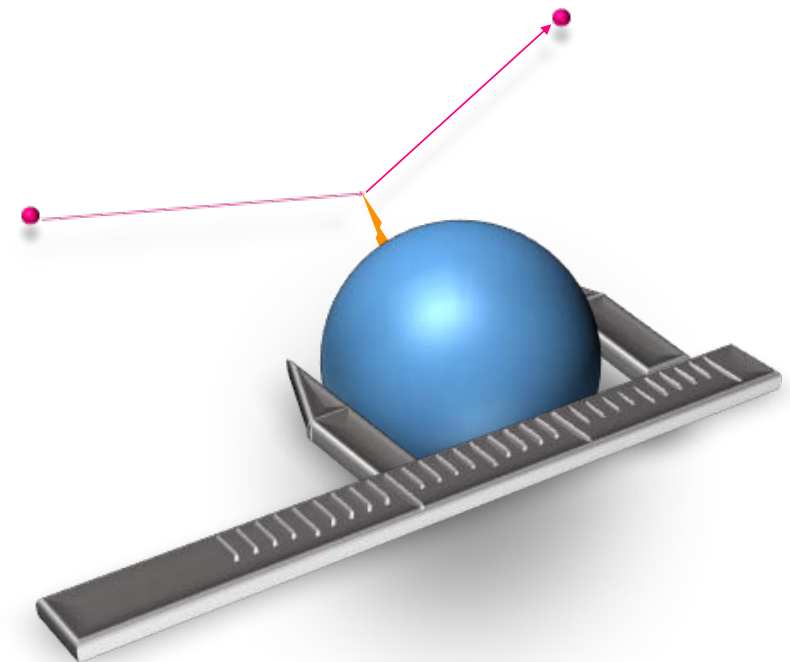


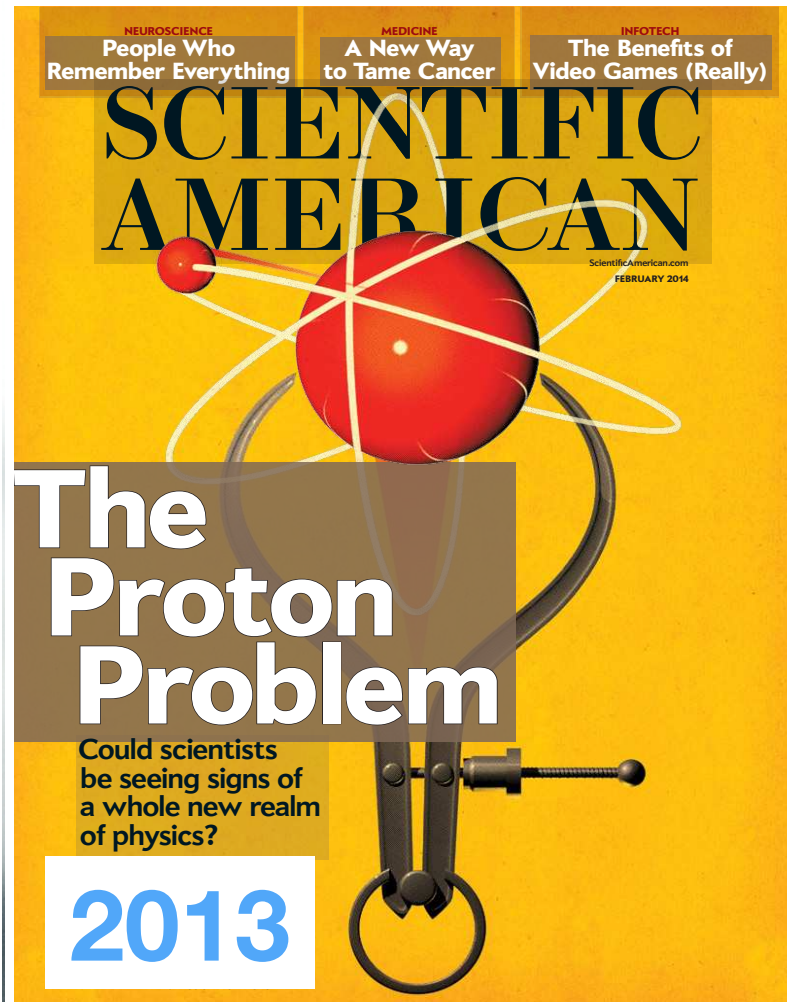
Electron scattering experiment off proton at ultra-low Q^2

Toshimi Suda

**Research Center for Electron-Photon Science,
Tohoku University,
Sendai**



“Proton Radius Puzzle”



many many discussions ..

Data ? Interpretation ?

e-scatt.
(1950~)

μ -hy
(2000~)

Higher order effects ?

hydrogen
(1990~)

QED calculation ?

New Physics (beyond SM ?)

4.0% (1.7 σ)

0.82 0.84 0.86 0.88 0.9 0.92

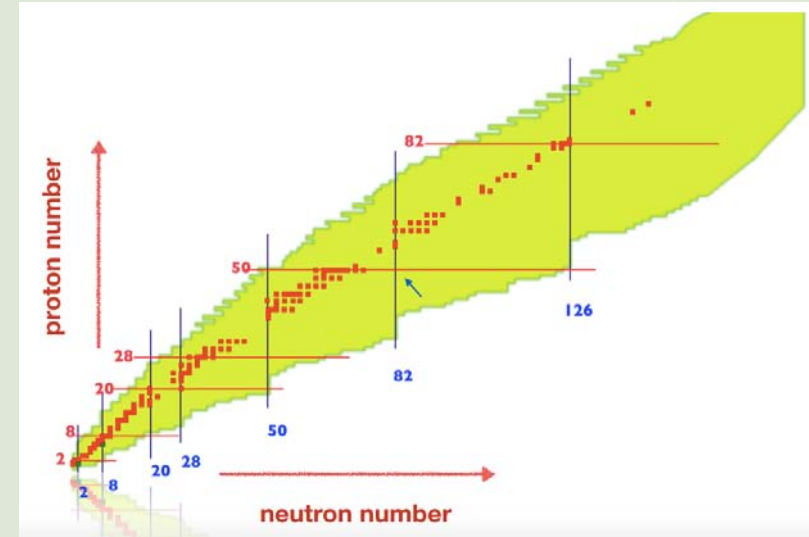
so far, not yet settled (2016)

We are “ Electron Scatterers”.

“classical” elastic electron scattering
to study the charge density distributions
pioneered by R. Hofstadter in 1950s !

$$\frac{d\sigma}{d\Omega} = \frac{d\sigma_{Mott}}{d\Omega} |F_c(q)|^2$$

$$F_c(\vec{q}) = \int \rho(\vec{r}) e^{-i\vec{q}\cdot\vec{r}} d\vec{r}$$



Not for stable nuclei,,,,,

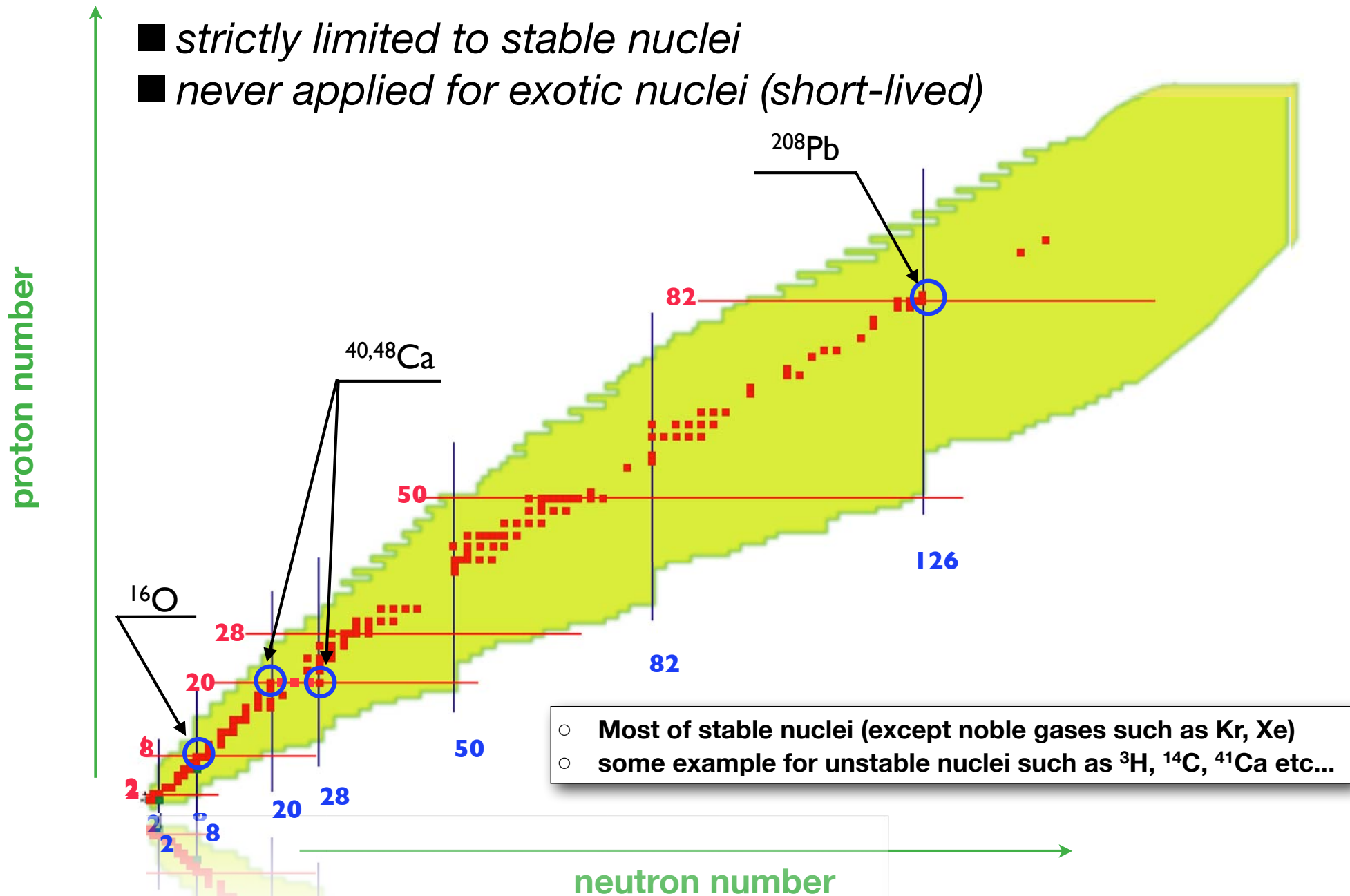
BUT never-yet-performed **Short-Lived Exotic Nuclei !**

➡ “Hofstadter’s experiments” for exotic nuclei

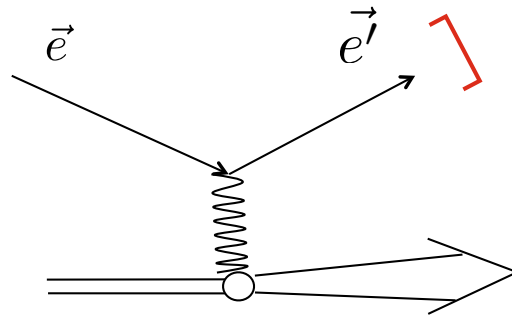
we are currently operating
the **World’s first electron scattering facility**
dedicated for exotic nuclei.

H.deVries, C. deJager and C. deVries
Atomic Data and Nuclear Data Tables 36 (1987)495

- *strictly limited to stable nuclei*
- *never applied for exotic nuclei (short-lived)*



Electron scattering provides direct and unambiguous structure information of atomic nuclei including proton



$$\omega = e - e'$$
$$\vec{q} = \vec{e} - \vec{e}'$$

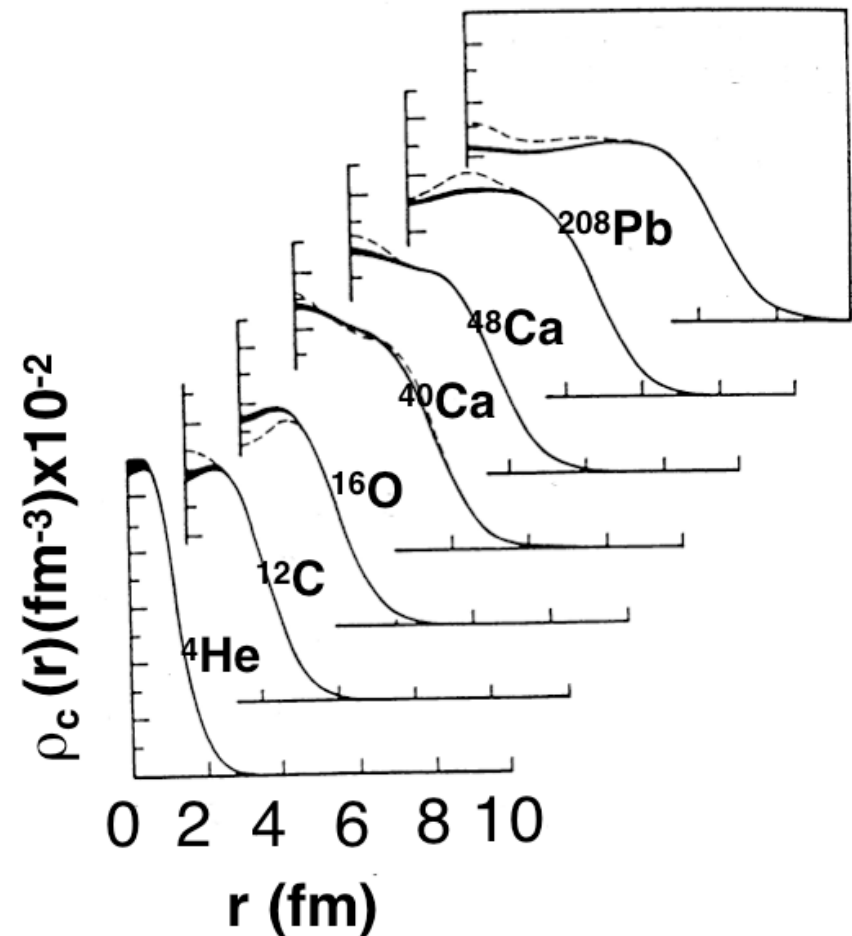
1. *point particle*
2. *electromagnetic interaction*
 - i) *coupling : charge and current => el.mag. structure*
 - ii) *“weak” -> probing whole volume*
perturbation theory
 - iii) *exp. data => structure information*
3. *variable q for fixed ω*

For 0^+ nuclei

$$\frac{d\sigma}{d\Omega} = \frac{d\sigma_{Mott}}{d\Omega} |F_c(q)|^2$$

$$F_c(\vec{q}) = \int \rho(\vec{r}) e^{-i\vec{q}\cdot\vec{r}} d\vec{r}$$

$$\rho_c(\vec{r}) = \sum_{i=1}^Z |\psi_i(\vec{r})|^2$$



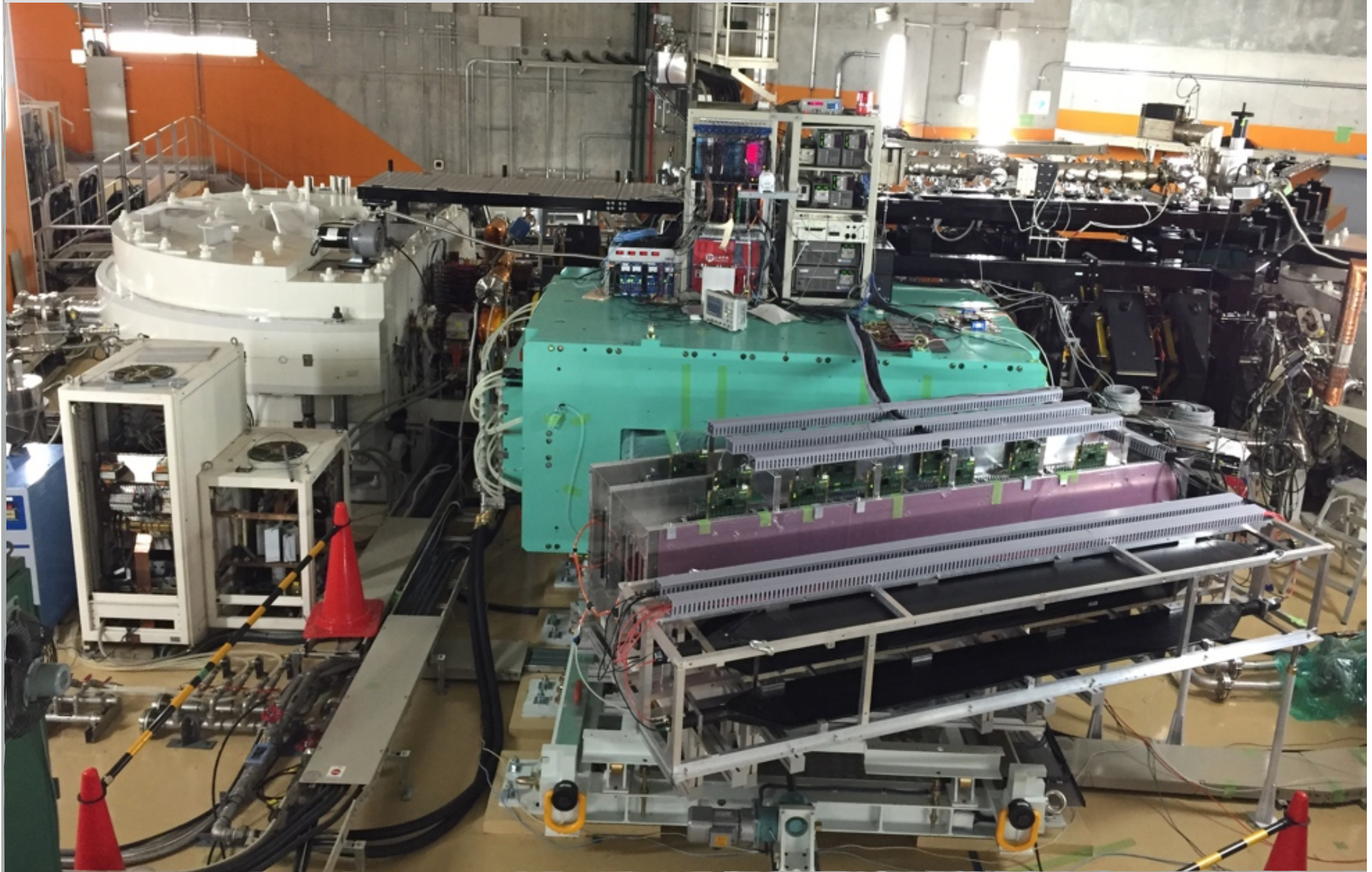
For non- 0^+ nuclei

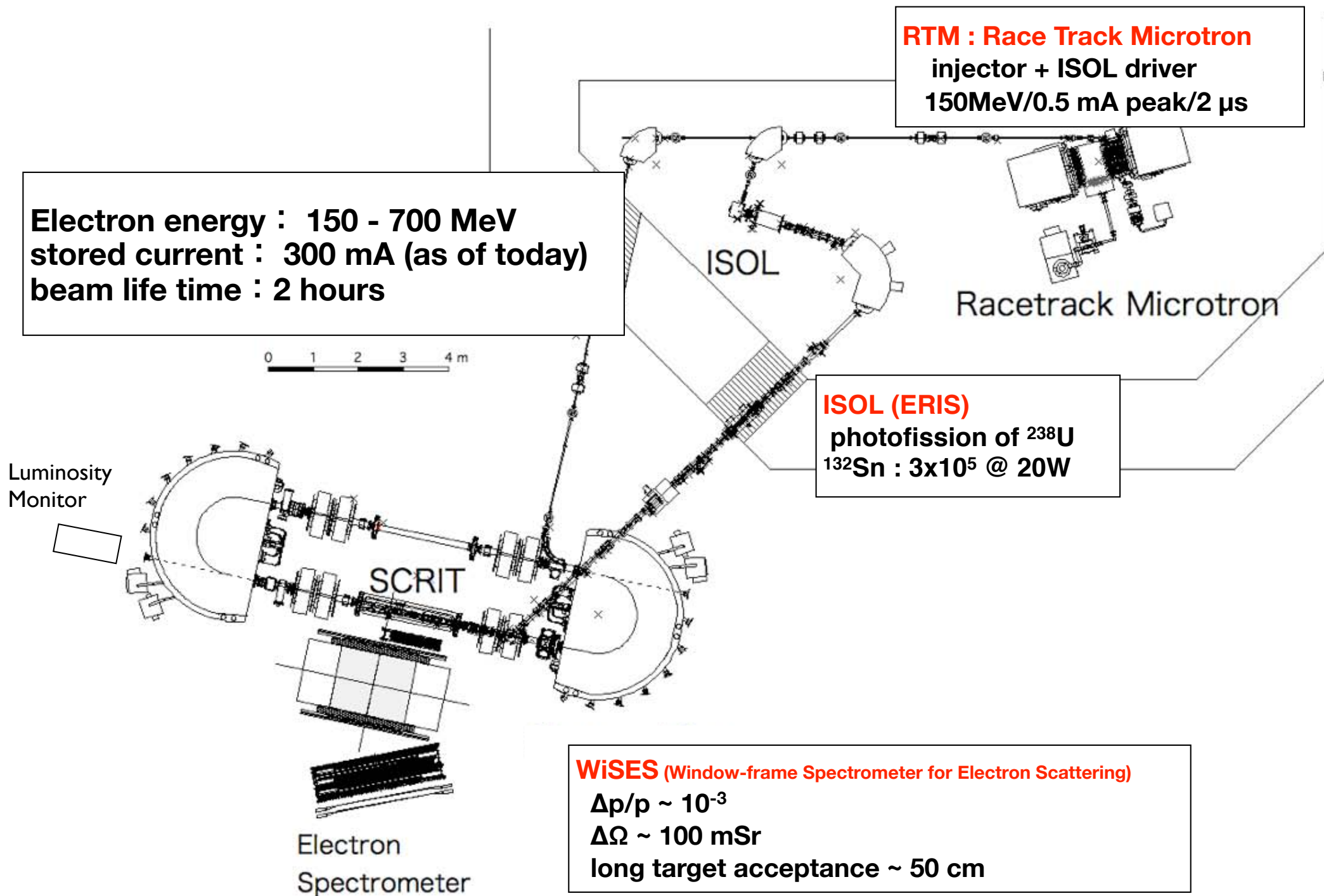
$$\frac{d\sigma}{d\Omega} = \frac{d\sigma_{Mott}}{d\Omega} [\text{Charge} + \text{Magnetic}]$$

SCRIT electron scattering facility

ULQ2@JPARC
Nov. 1, 2016

the world's first facility dedicated for exotic nuclei





Electron energy : 150 - 700 MeV
stored current : 300 mA (as of today)
beam life time : 2 hours

RTM : Race Track Microtron
injector + ISOL driver
150MeV/0.5 mA peak/2 μ s

ISOL (ERIS)
photofission of ^{238}U
 $^{132}\text{Sn} : 3 \times 10^5 @ 20\text{W}$

WiSES (Window-frame Spectrometer for Electron Scattering)
 $\Delta p/p \sim 10^{-3}$
 $\Delta \Omega \sim 100 \text{ mSr}$
long target acceptance $\sim 50 \text{ cm}$

Luminosity Monitor

0 1 2 3 4 m

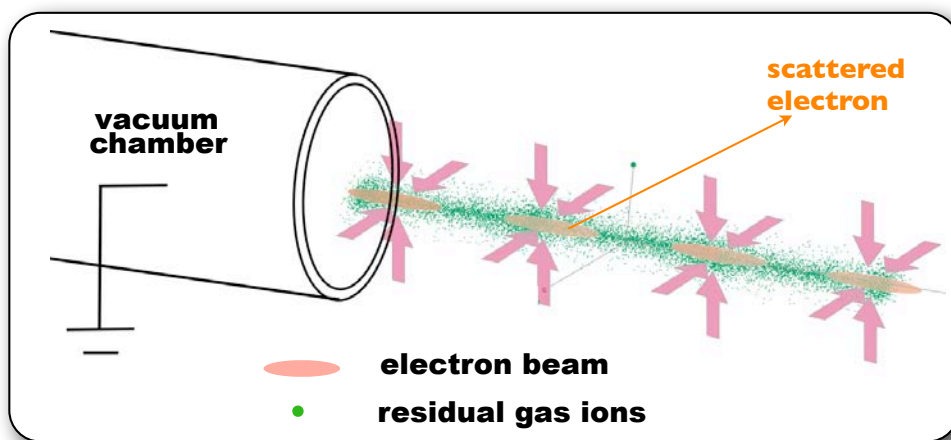
Electron Spectrometer

M. Wakasugi, T. Suda and Y. Yano
Nucl. Instrum. and Method A278 (2004) 216.

Idea

Problematic ion trapping phenomena
@
electron storage ring

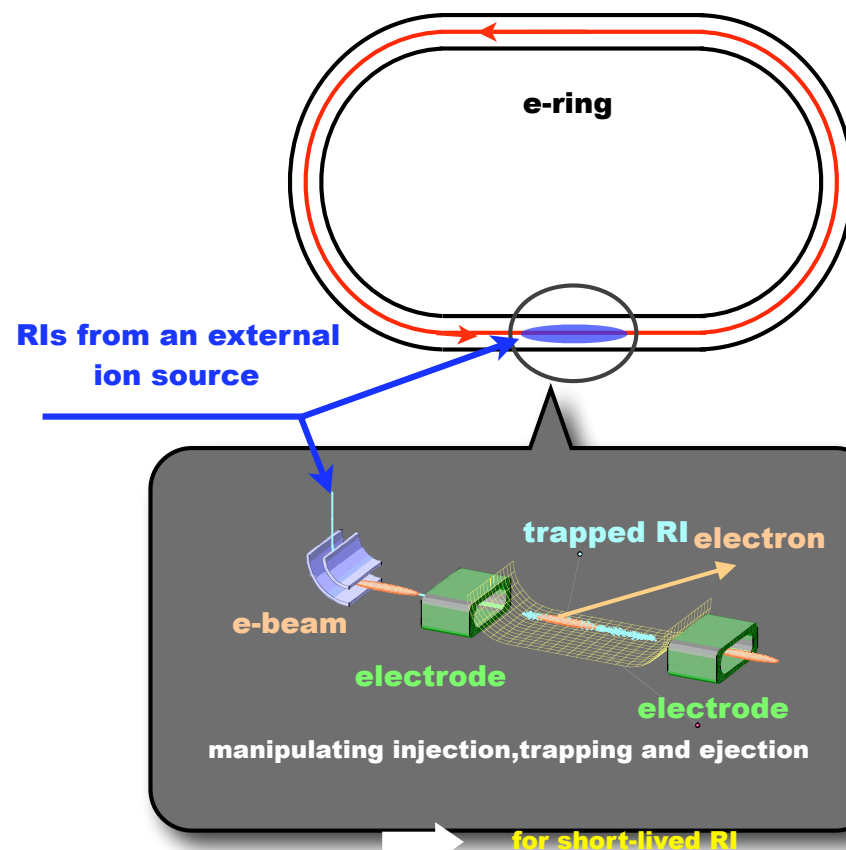
ionized residual gases are trapped
by the circulating electron beam

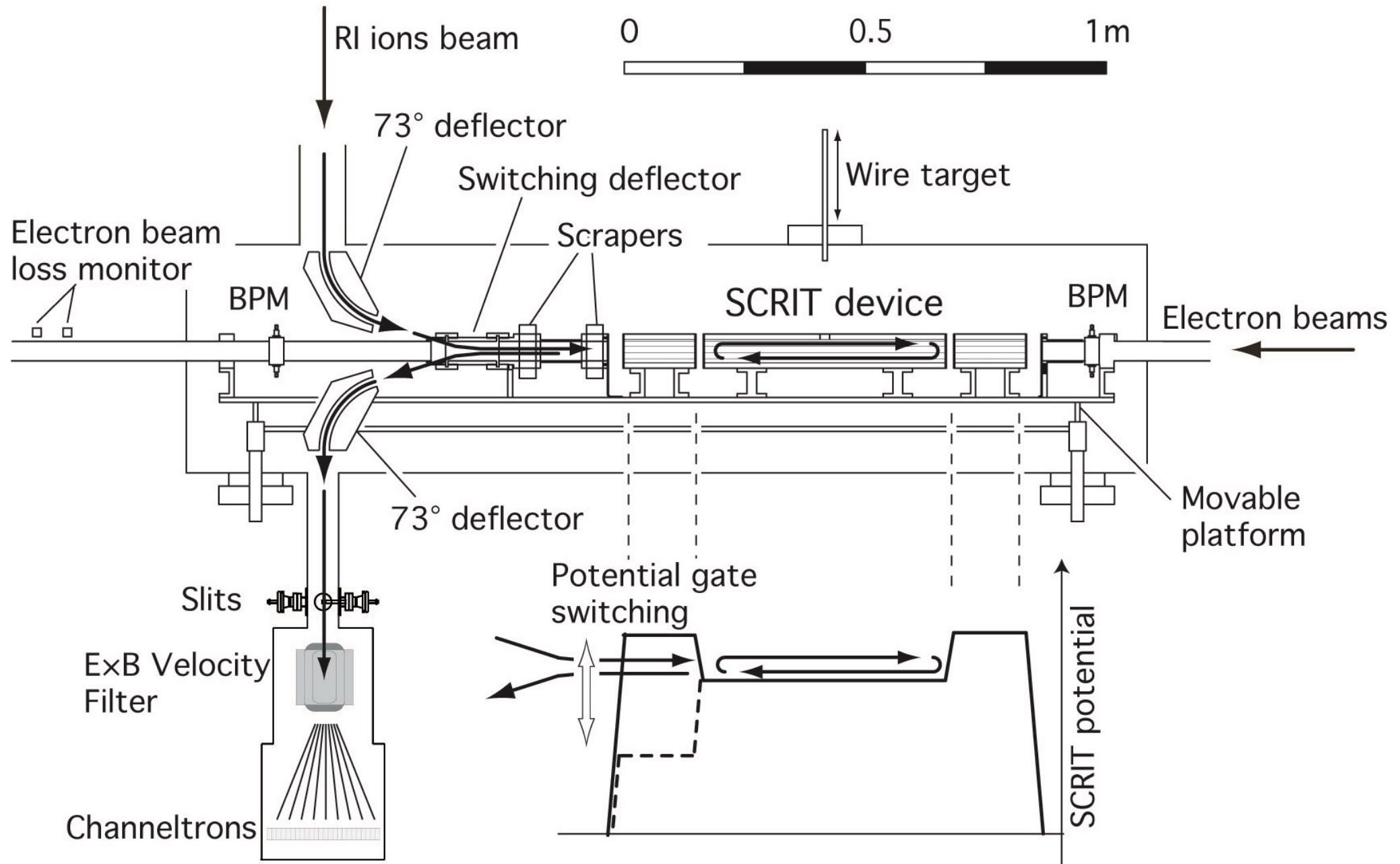


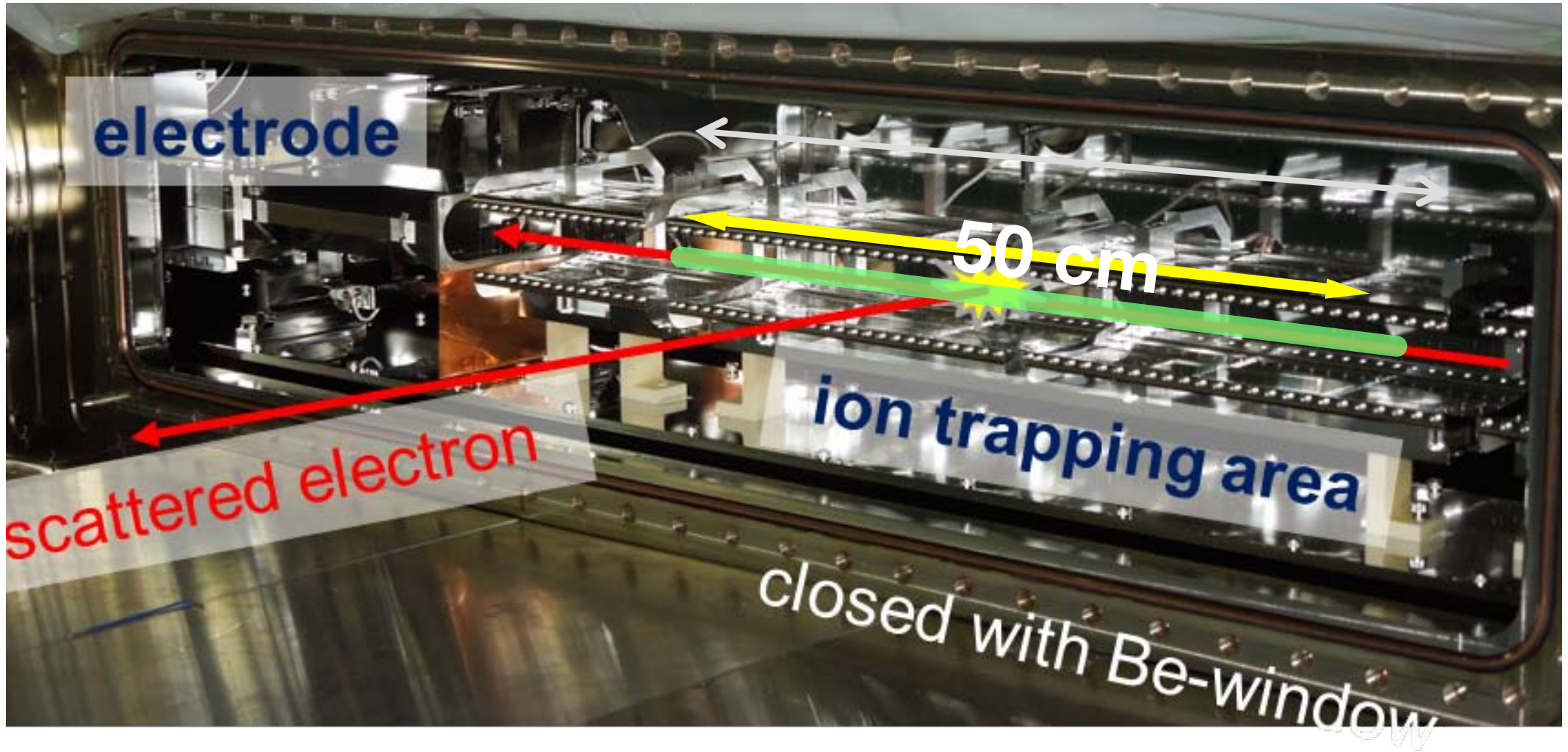
ill problem of e-storage ring

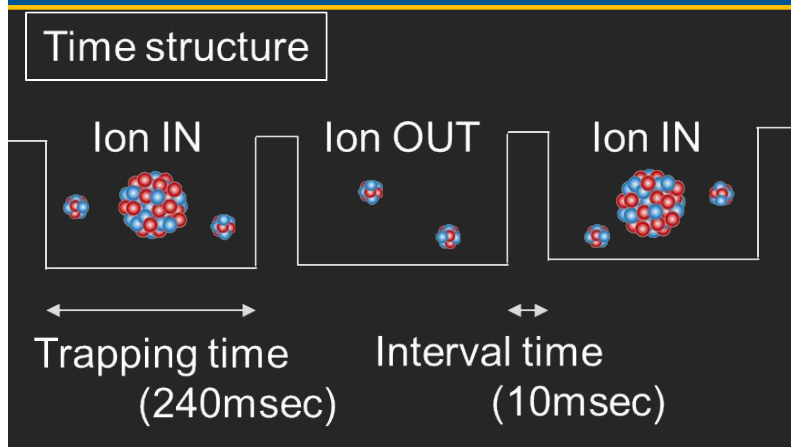
new ion trap for e-RI scattering

trapping RIs on electron beam
(automatic e-scattering off trapped RIs)

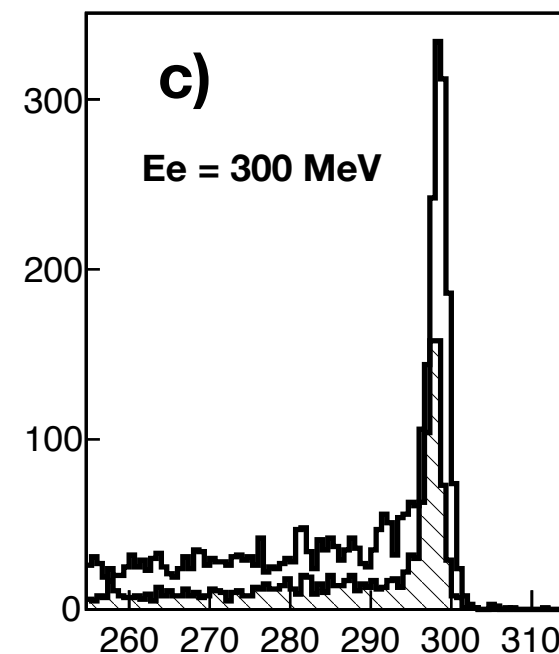
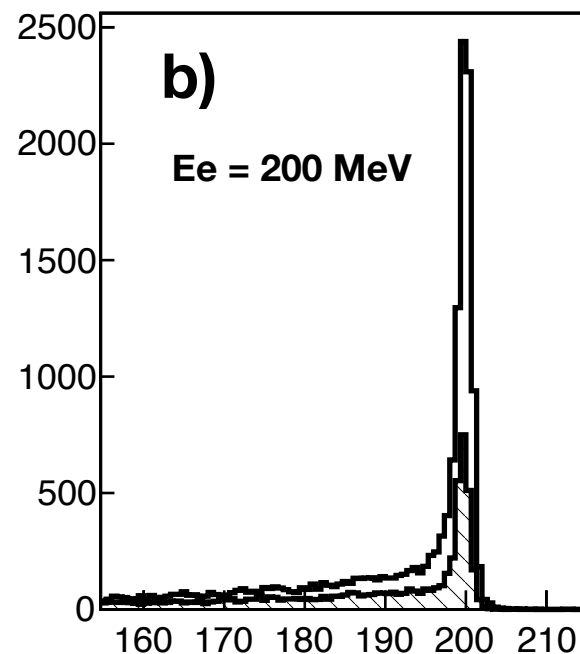
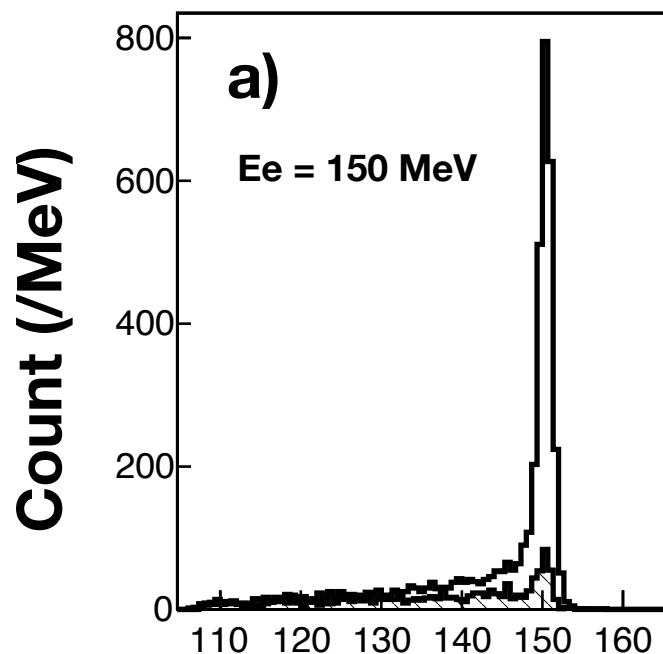








Ion IN - Ion OUT
for comparative measurements

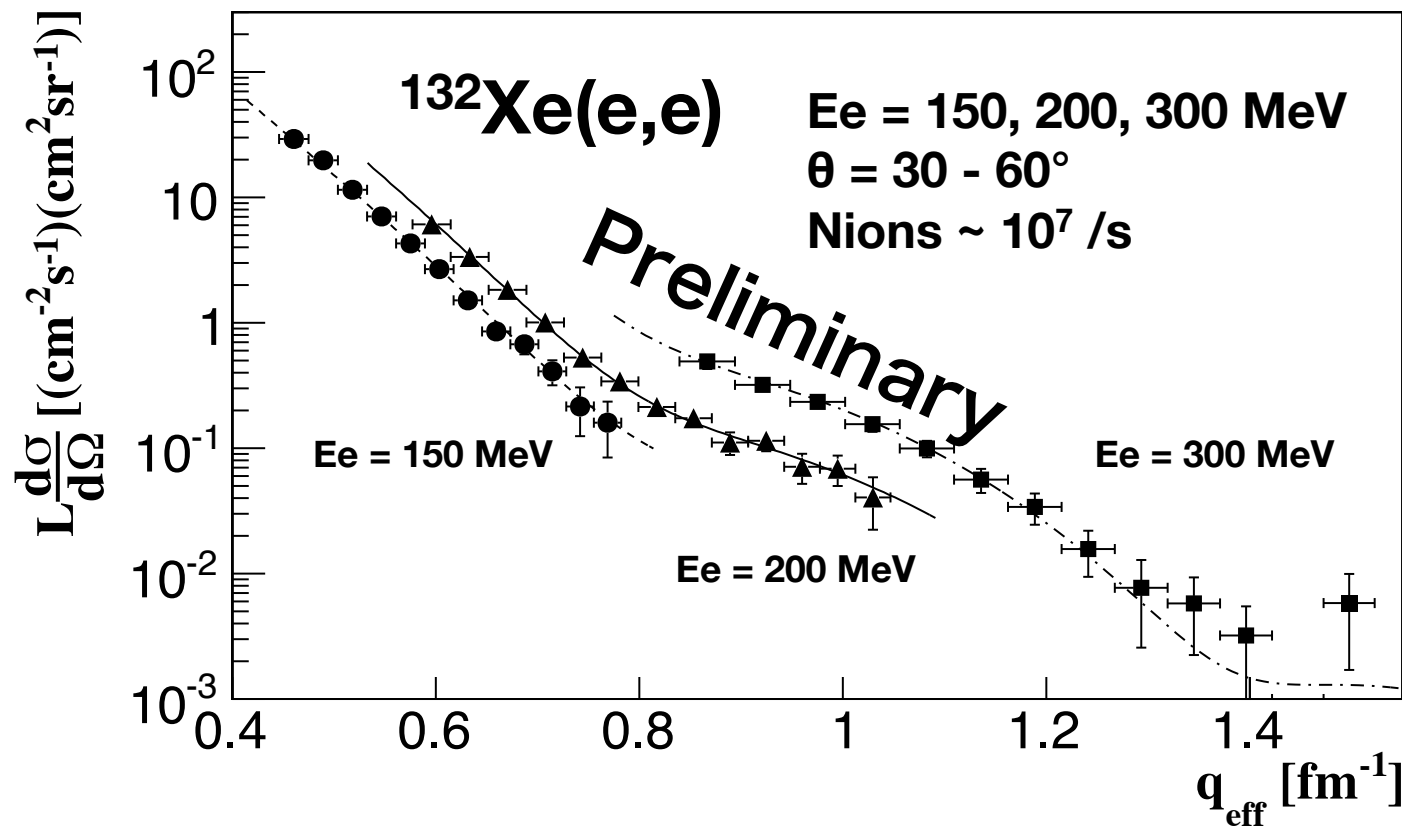
 $^{132}\text{Xe}(e,e')$ 

Scattered electron energy (MeV)

The facility started its full operation,
and the first physic run was carried out since April, 2016.

^{132}Xe is a stable nucleus but has never been targeted.

Luminosity, $10^{27} \text{ cm}^{-2}\text{s}^{-2}$, is achieved **with only $\sim 10^7$ target nuclei**



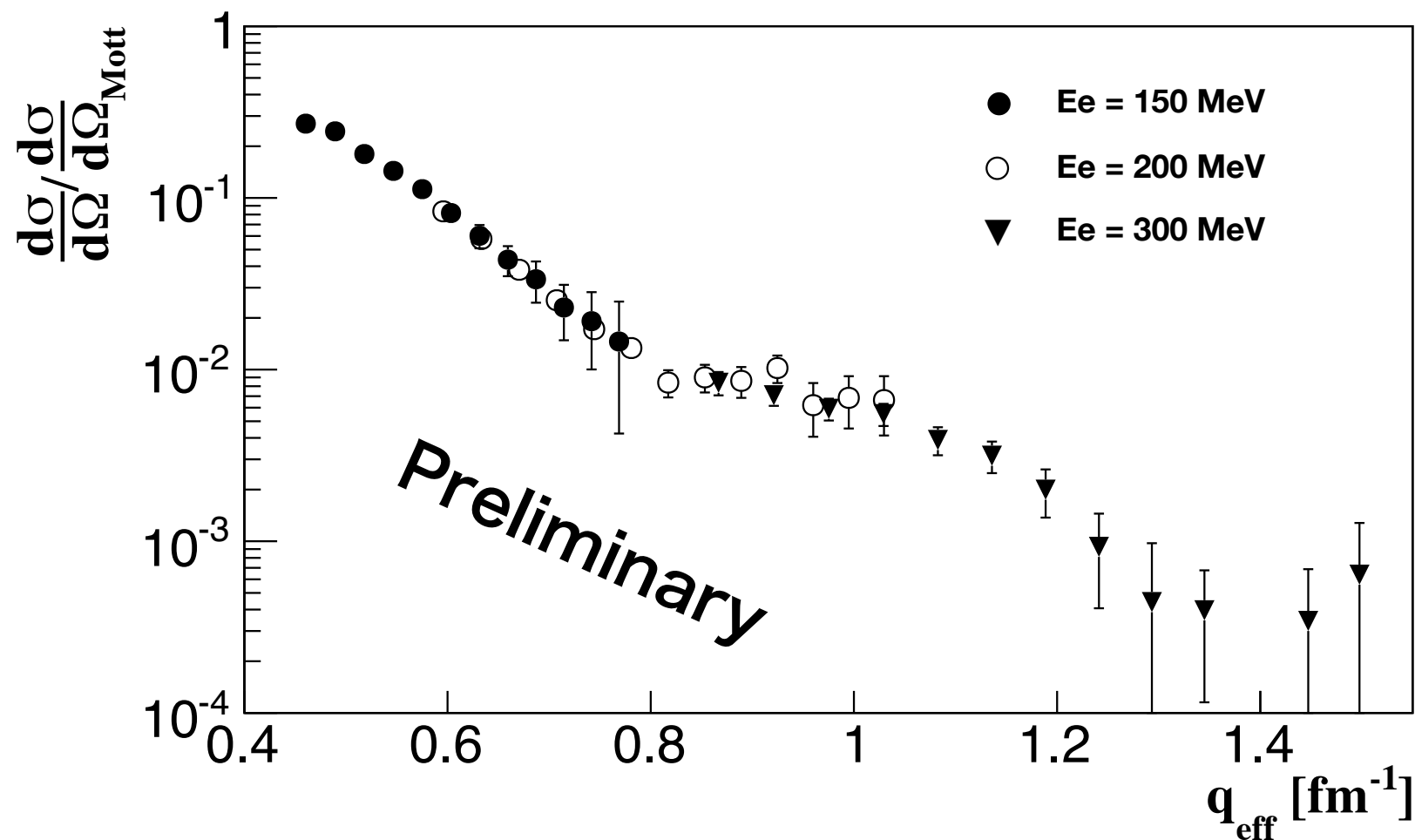
First experiment for exotic nucleus, ^{138}Xe (14 min.), this autumn.
and to be followed by **doubly magic nucleus, ^{132}Sn (50s).**

PWIA

$$\frac{d\sigma}{d\Omega} = \frac{d\sigma_{Mott}}{d\Omega} |F_c(q)|^2$$

DWBA

$$|F_C^{DWBA}|^2 \sim \frac{d\sigma}{d\Omega} / \frac{d\sigma_{Mott}}{d\Omega}$$



	Ee	N_{beam}	$\rho \cdot t$	L
Hofstadter's era (1950s)	150 MeV	~ 1nA (~10 ⁹ /s)	~10 ¹⁹ /cm ²	~10 ²⁸ /cm ² /s
JLAB	6 GeV	~100μA (~10 ¹⁴ /s)	~10 ²² /cm ²	~10 ³⁶ /cm ² /s
SCRIT	150 - 300 MeV	~200 mA (~10 ¹⁸ /s)	~ 10 ⁹ /cm ²	~10 ²⁷ /cm ² /s



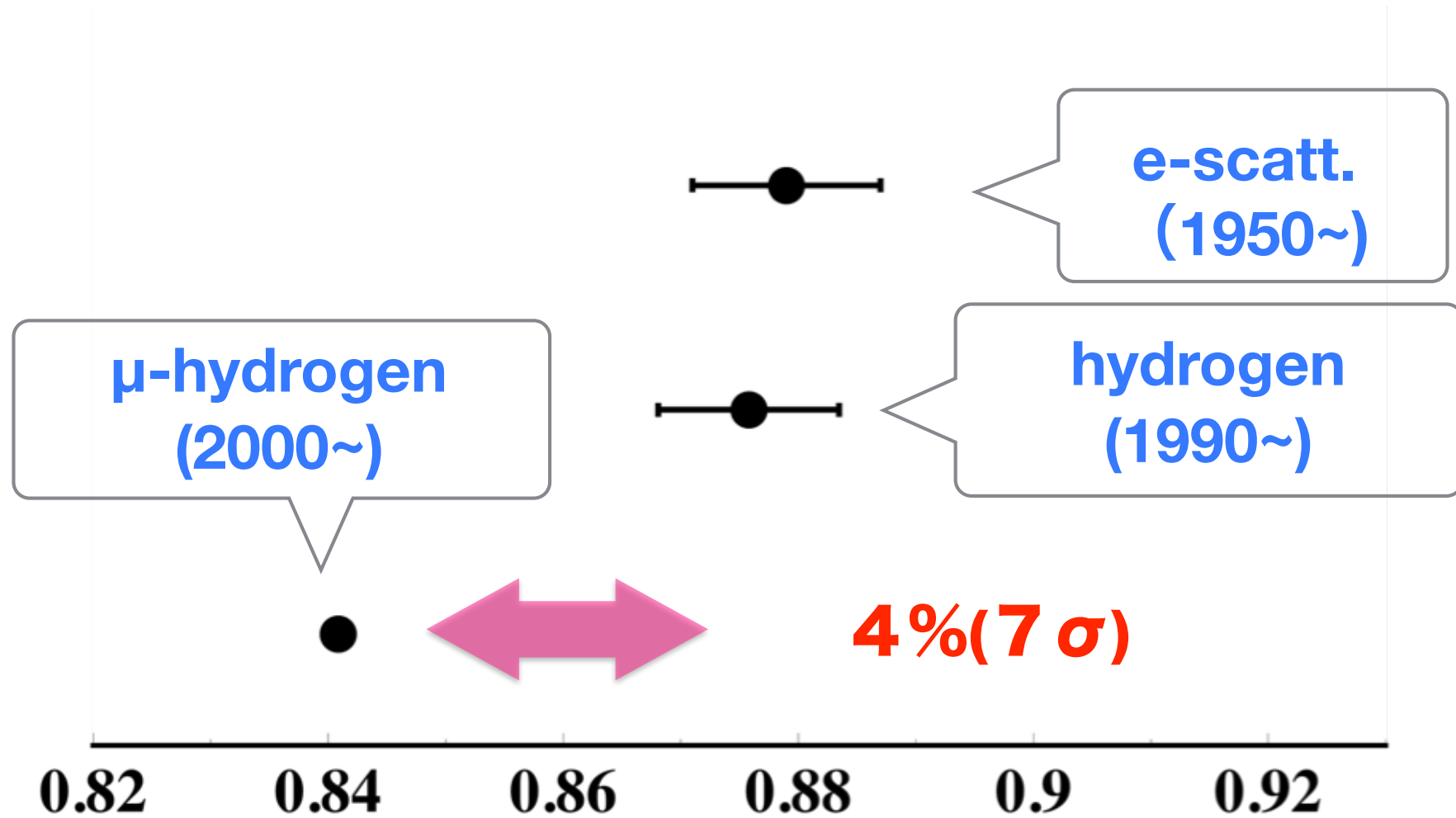
~10⁷ ions are trapped
on the electron beam of ~ 1 mm² cross section

$$\sim 10^7 / \text{mm}^2 \rightarrow 10^9 / \text{cm}^2$$

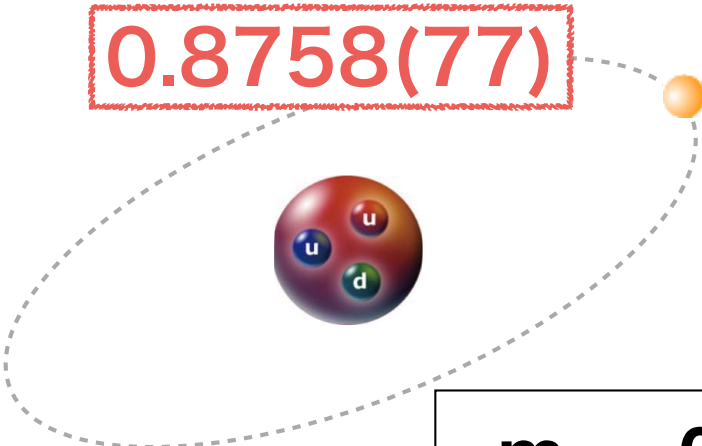
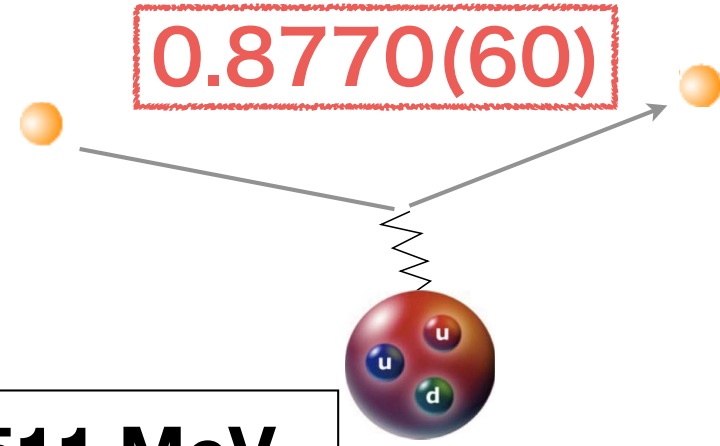
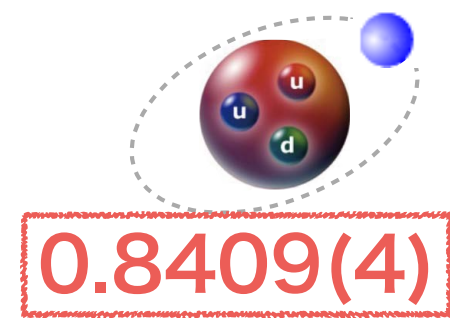

Proton Charge Radius

Proton charge radius puzzle

ULQ2@JPARC
Nov. 1, 2016



Proton Charge Radius (fm)

	Spectroscopy	Scattering
e^-	 <p>0.8758(77)</p>	 <p>0.8770(60)</p>
	<p>$m_e = 0.511 \text{ MeV}$ $m_\mu = 105.6 \text{ MeV}$</p>	
μ^-	 <p>0.8409(4)</p>	 <p>MUSE@PSI</p>

P. Randolph et al., Nature 466 (2010) 213

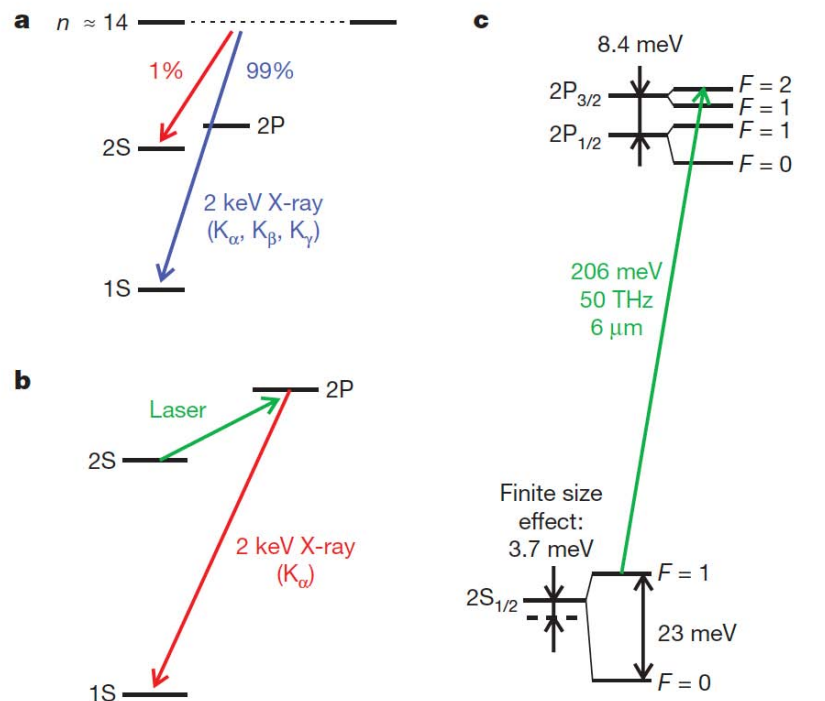
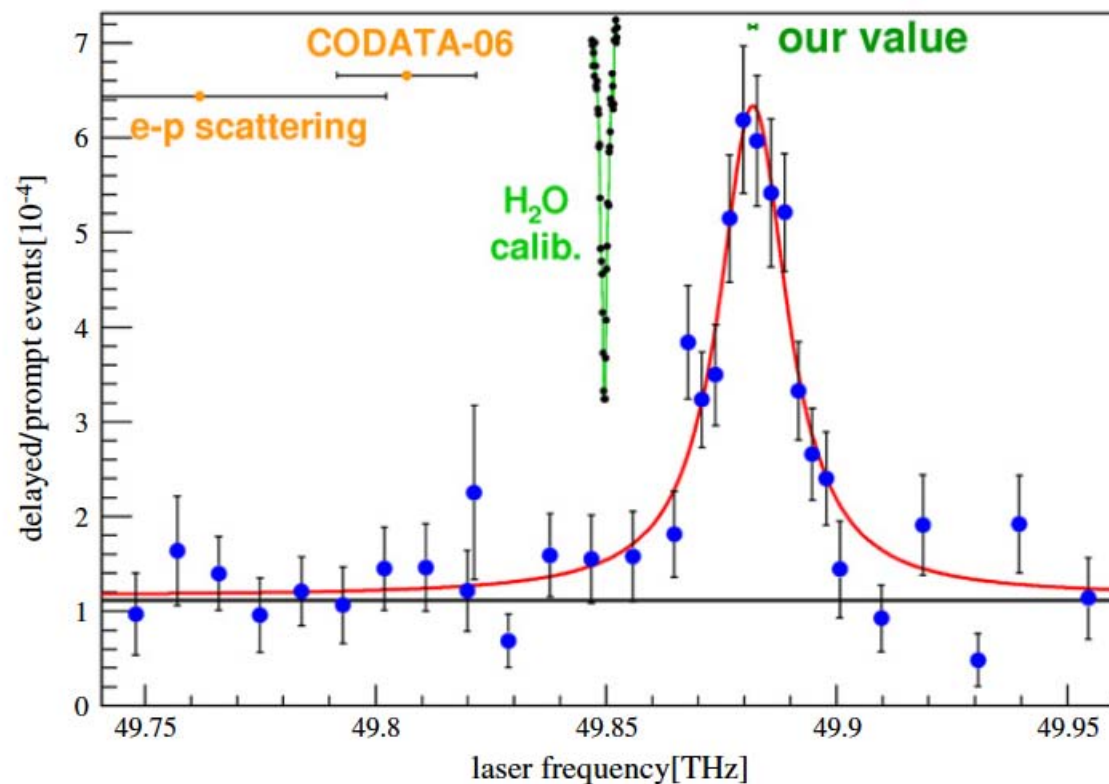


Figure 1 | Energy levels, cascade and experimental principle in muonic hydrogen. **a**, About 99% of the muons proceed directly to the 1S ground state during the muonic cascade, emitting ‘prompt’ K-series X-rays (blue). 1% remain in the metastable 2S state (red). **b**, The $\mu p(2S)$ atoms are illuminated by a laser pulse (green) at ‘delayed’ times. If the laser is on resonance, delayed K_α X-rays are observed (red). **c**, Vacuum polarization dominates the Lamb shift in μp . The proton’s finite size effect on the 2S state is large. The green arrow indicates the observed laser transition at $\lambda = 6 \mu\text{m}$.



$$\Delta E(2S - 2P) = 209.978(5) - 5.226r_p^2 + \dots \text{ meV}$$

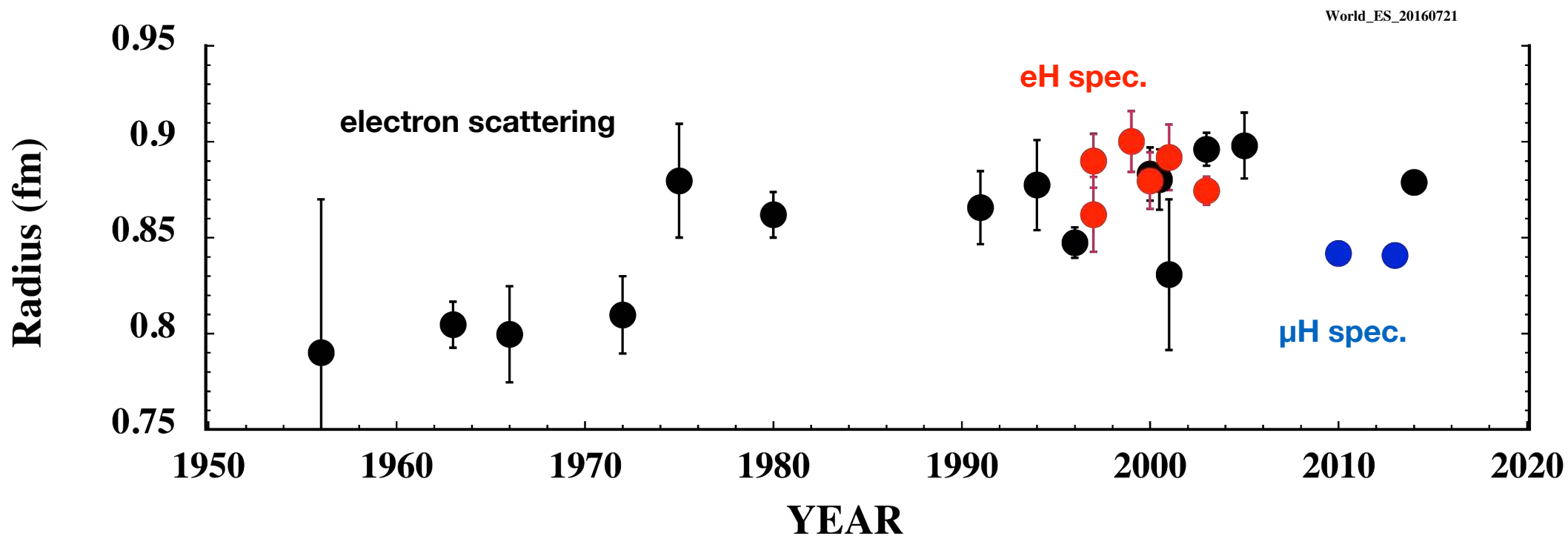
Electron scattering off proton



e+p, e+A elastic scattering
R. Hofstadter
(1961)



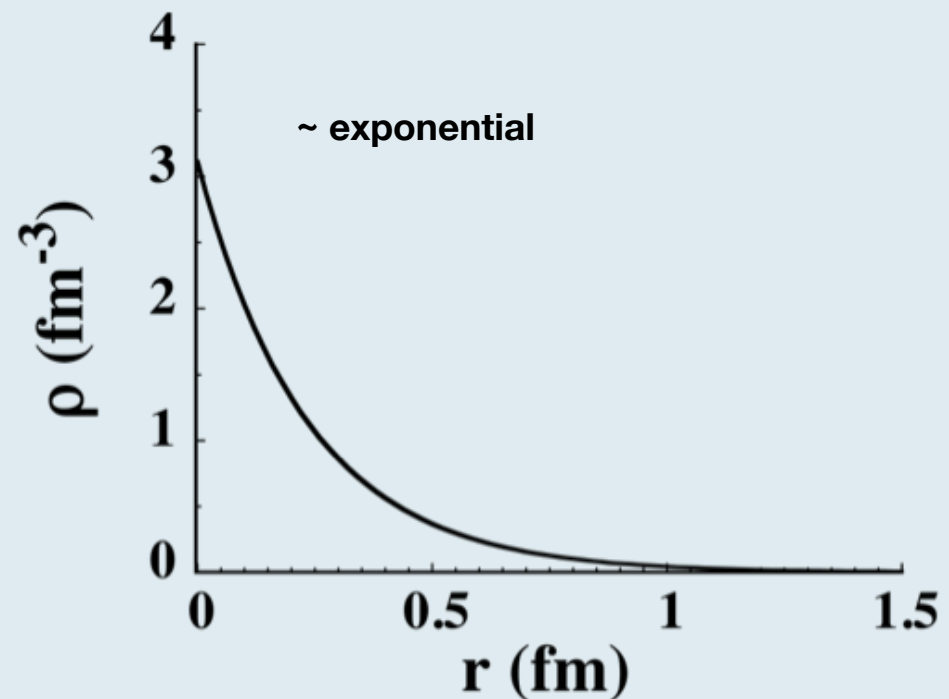
e+p deep inelastic scattering
J. Friedman, H. Kendall and R. Taylor
(1990)



RMS radius

$$\begin{aligned}\langle r^2 \rangle &= \int r^2 \rho(\vec{r}) d\vec{r} \\ &= 4\pi \int r^4 \rho(r) dr\end{aligned}$$

$\rho(r)$



$$G_E(Q^2) = \frac{1}{\left(1 + \frac{Q^2}{\alpha^2}\right)^2}$$

$$\alpha^2 = 0.71(\text{GeV}/c)^2$$

$$G_E(Q^2) \rightarrow \rho(r) \quad Q^2 \ll M_p^2$$

Fourier transformation

$$\rho(r) = \frac{\alpha^3}{8\pi} e^{-\alpha r} \quad (r > 0)$$

$$\langle r^2 \rangle^{1/2} = \frac{2\sqrt{3}}{\alpha}$$

$$\langle r^2 \rangle^{1/2} = 0.81 \text{ fm}$$

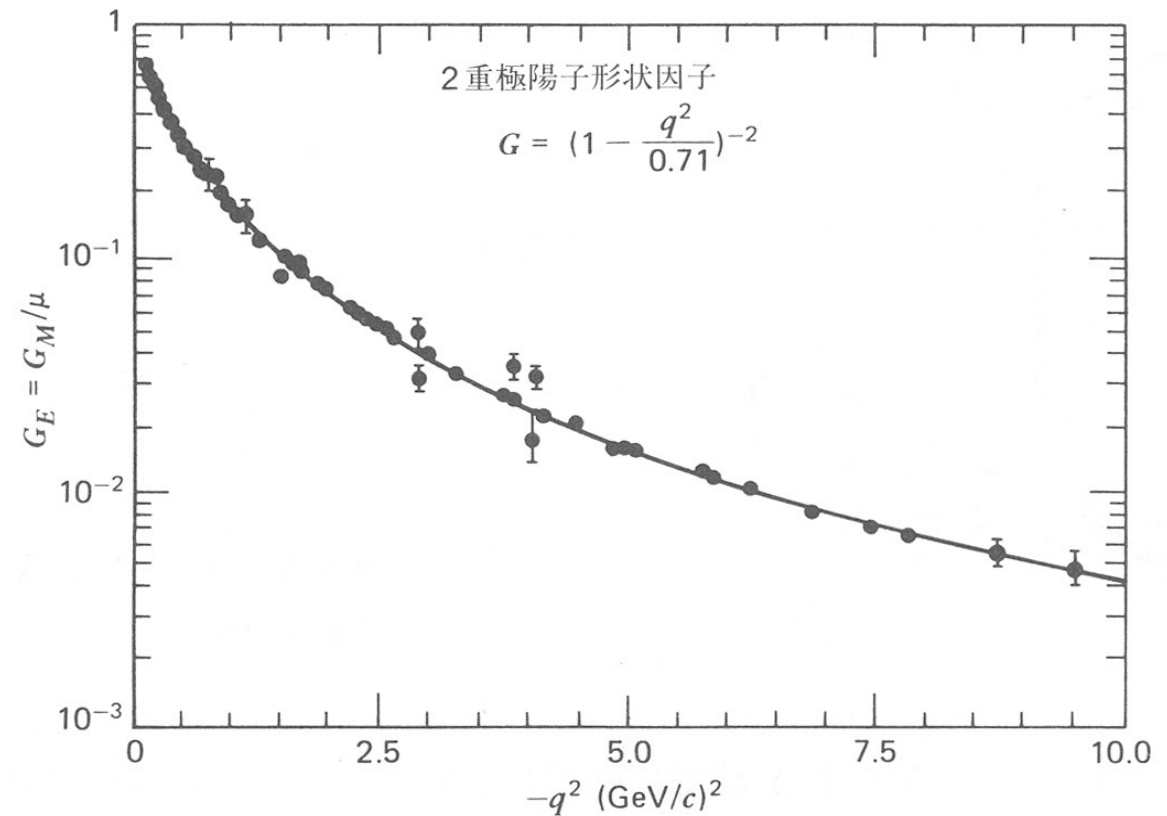
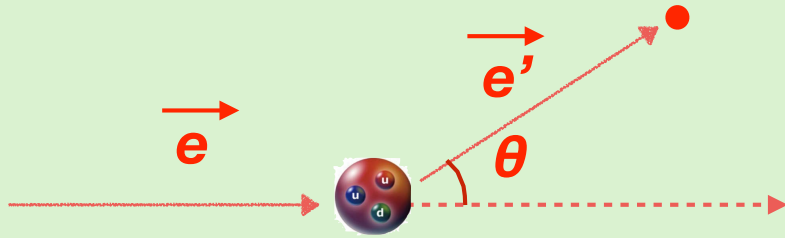


図8・4 q^2 の関数としての陽子形状因子



$$\frac{d\sigma}{d\Omega} = \left(\frac{d\sigma}{d\Omega}\right)_{Mott} \frac{G_E^2(Q^2) + \frac{\tau}{\epsilon} G_M^2(Q^2)}{1 + \tau}$$

$$\left(\frac{d\sigma}{d\Omega}\right)_{Mott} = \frac{z^2 \alpha^2 \cos^2(\theta/2)}{4e^2 \sin^4(\theta/2)} \propto \frac{e^2}{q^4}$$

momentum transfer $\vec{q} = \vec{e} - \vec{e}'$

energy transfer $\omega = e - e'$

4 momentum transfer $Q^2 = q^2 - \omega^2$
 $= 4 e e' \sin^2(\theta/2)$

$$\epsilon = \frac{1}{1 + 2(1 + \tau) \tan^2 \frac{\theta}{2}}$$

$$\tau = \frac{Q^2}{4m_p^2}$$

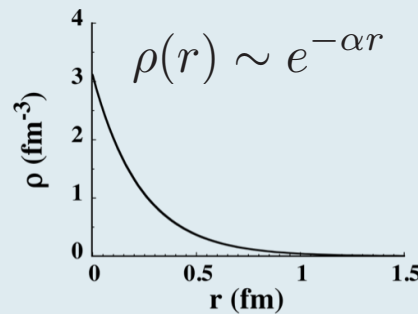
1) high Q^2 : charge density $\rho(r)$

Electric Form Factor G_E



$\rho(r)$

$$\langle r^2 \rangle = \int r^2 \rho(\vec{r}) d^3\vec{r}$$



radius is sensitive to $\rho(r)$ at large distance
(even at $r \sim 4$ fm)

2) low Q^2

$$G_E(Q^2) \sim 1 - \frac{\langle r^2 \rangle^{1/2}}{6} Q^2 + \frac{\langle r^4 \rangle^{1/2}}{120} Q^4 - \dots$$

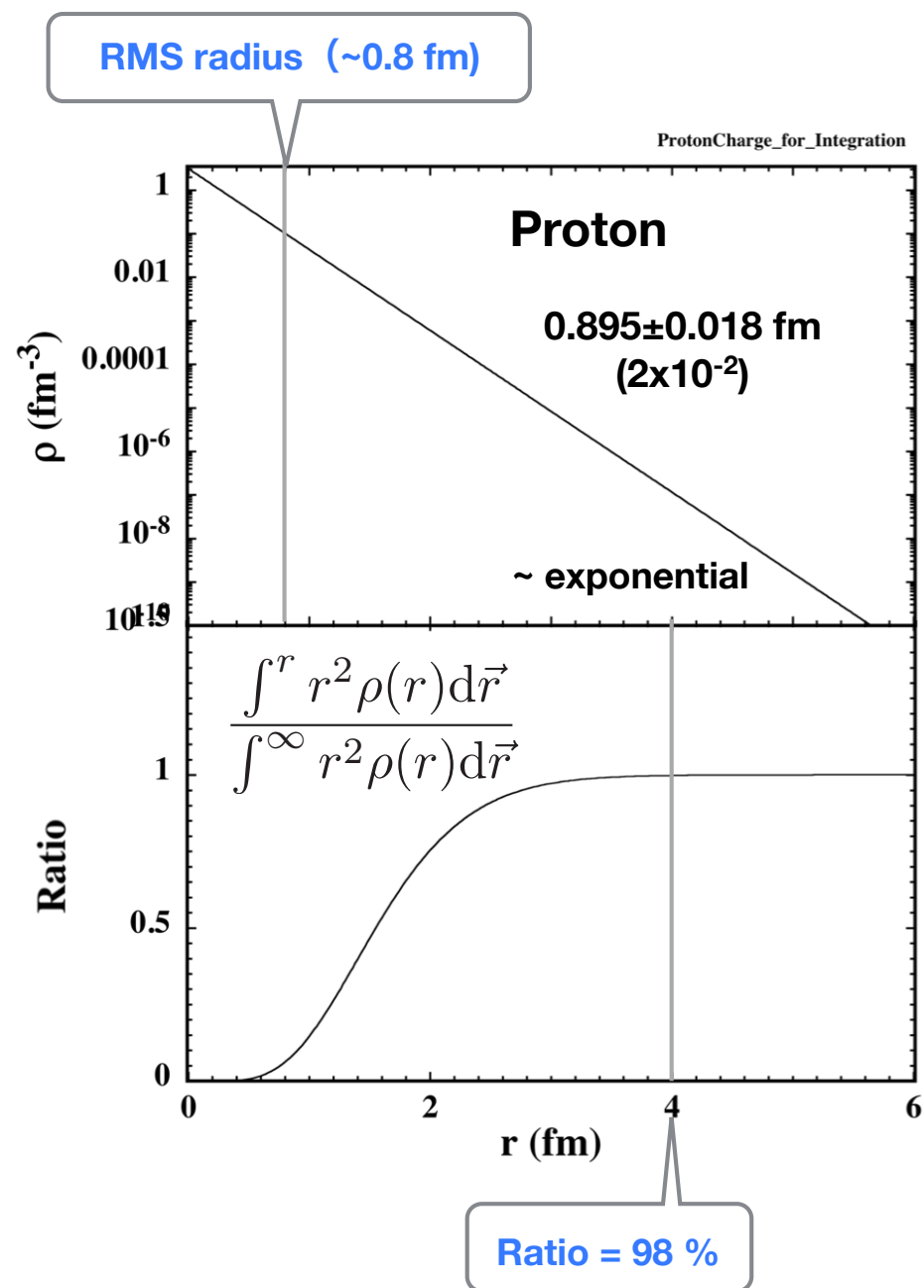
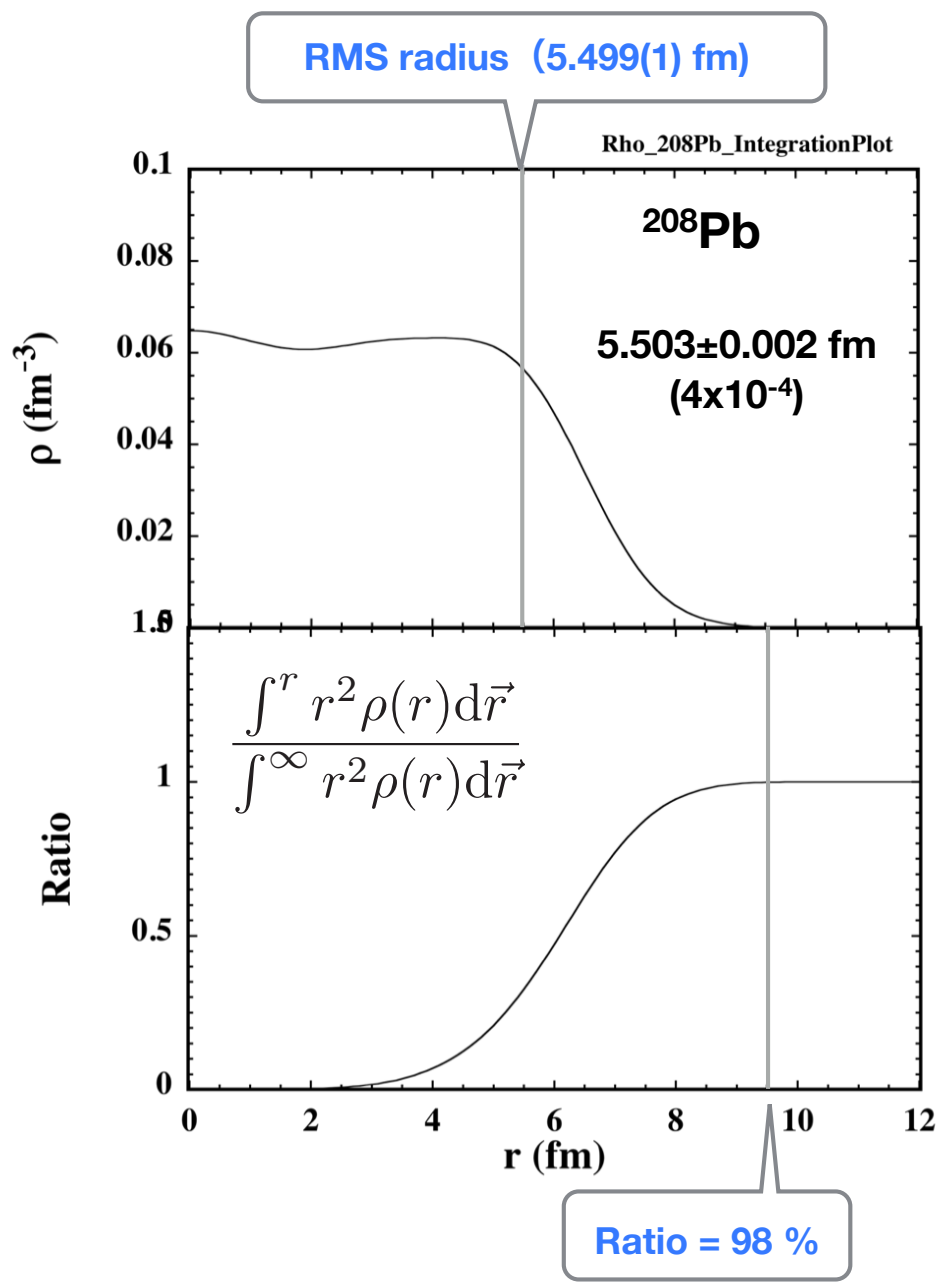
$$\langle r^2 \rangle \equiv -6 \left. \frac{dG_E(Q^2)}{dQ^2} \right|_{Q^2 \rightarrow 0}$$

ill problem : higher order contribution



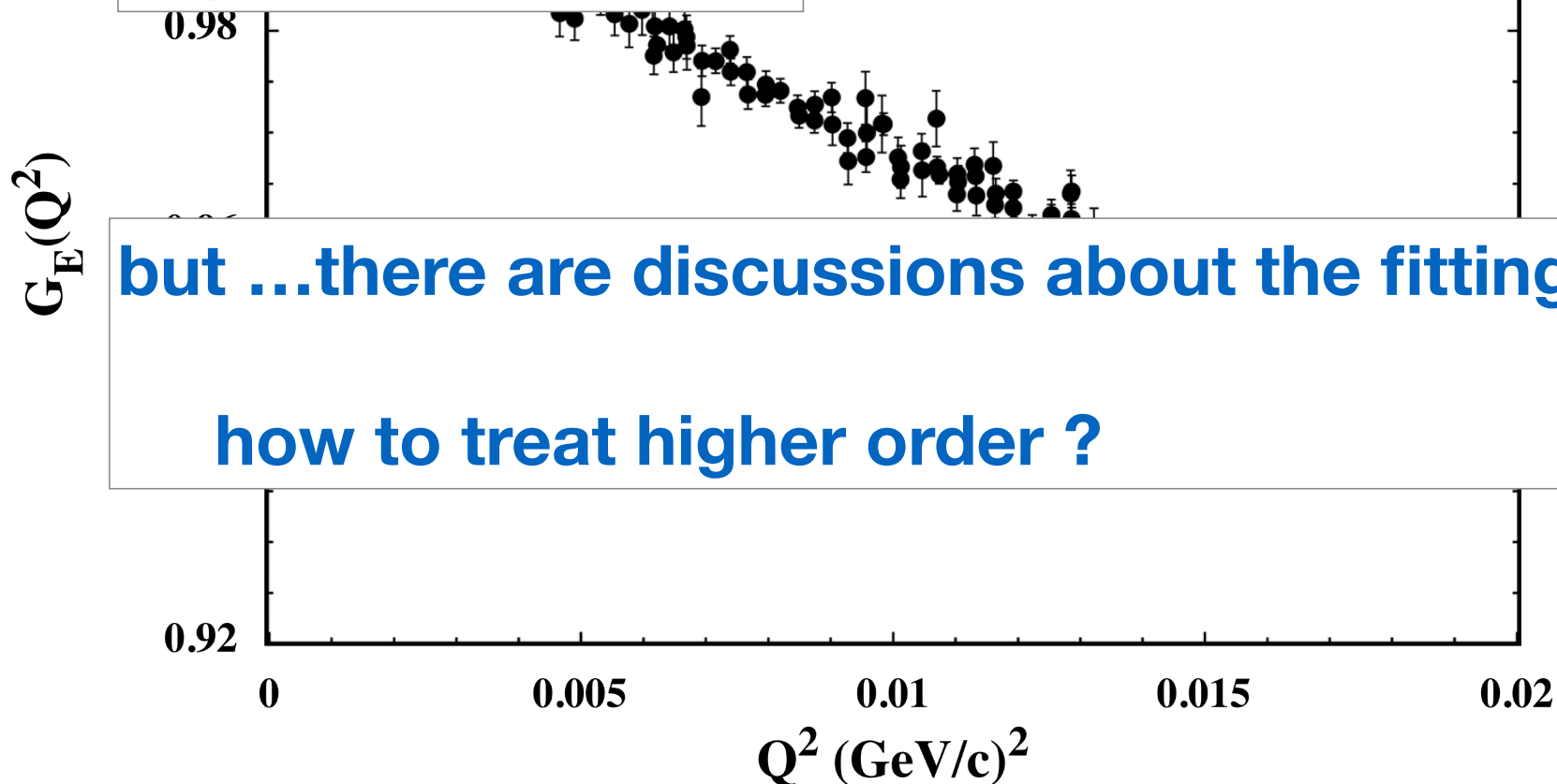
lower Q^2 as possible

Charge radius $\langle r^2 \rangle = \int r^2 \rho(\vec{r}) d\vec{r}$

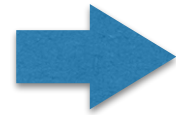


$$G_E(Q^2) \sim 1 - \frac{\langle r^2 \rangle}{6} Q^2 + \frac{\langle r^4 \rangle}{120} Q^4 - \frac{\langle r^6 \rangle}{5040} Q^6 + \dots$$

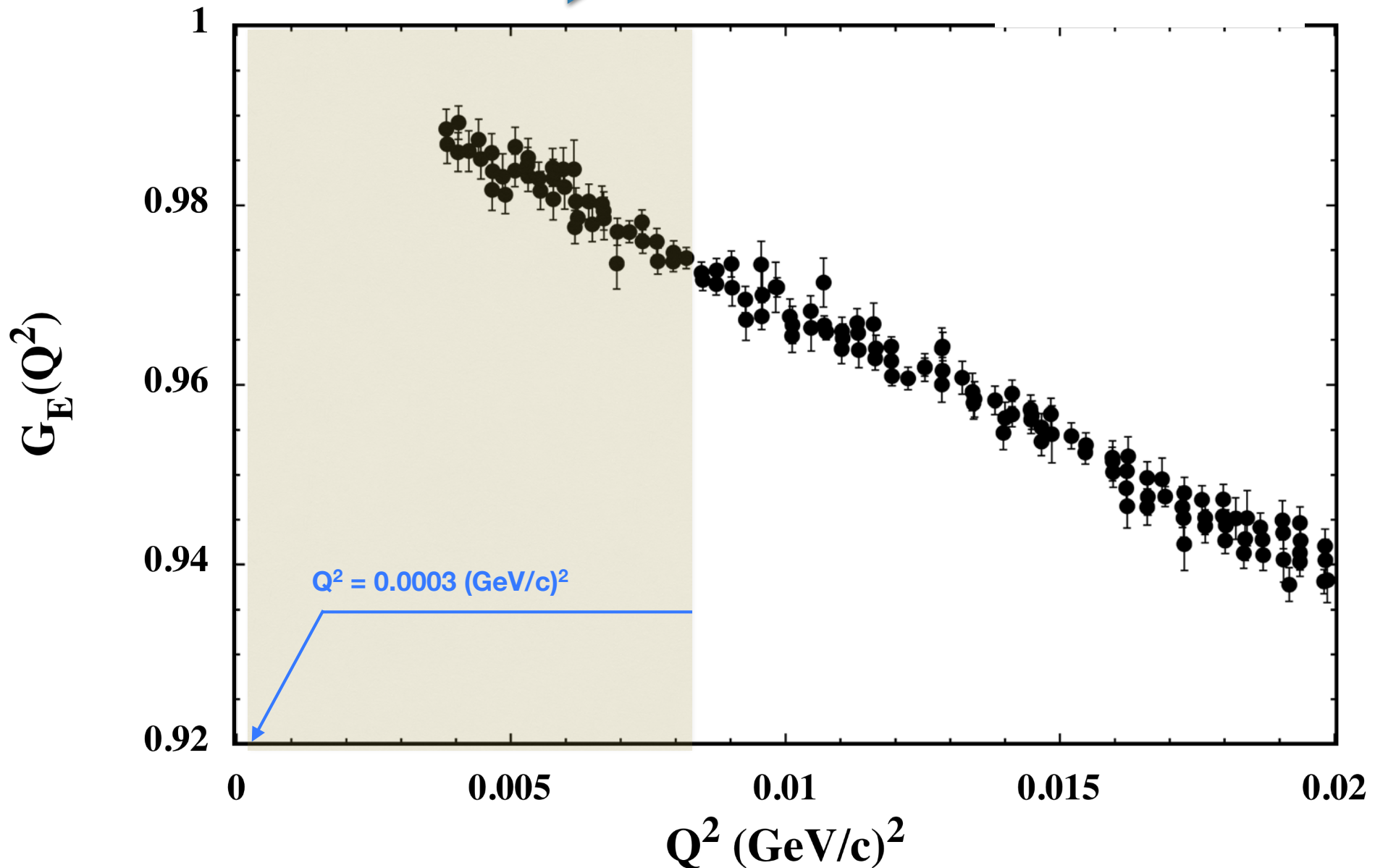
$$\langle r_p \rangle = 0.879 (5) \text{ fm}$$



Reduction of the higher order contribution



$G_E(Q^2)$ at lower Q^2 region



What are we going to do ?

ULQ2@JPARC
Nov. 1, 2016

	Mainz 2014	Tohoku
Q^2_{\min} (GeV/c) ²	0.004	0.0003
E_e (MeV)	180 ~ 850	20 ~ 60
absolute $d\sigma/d\Omega$	X	○
G_E/G_M separation	X	○

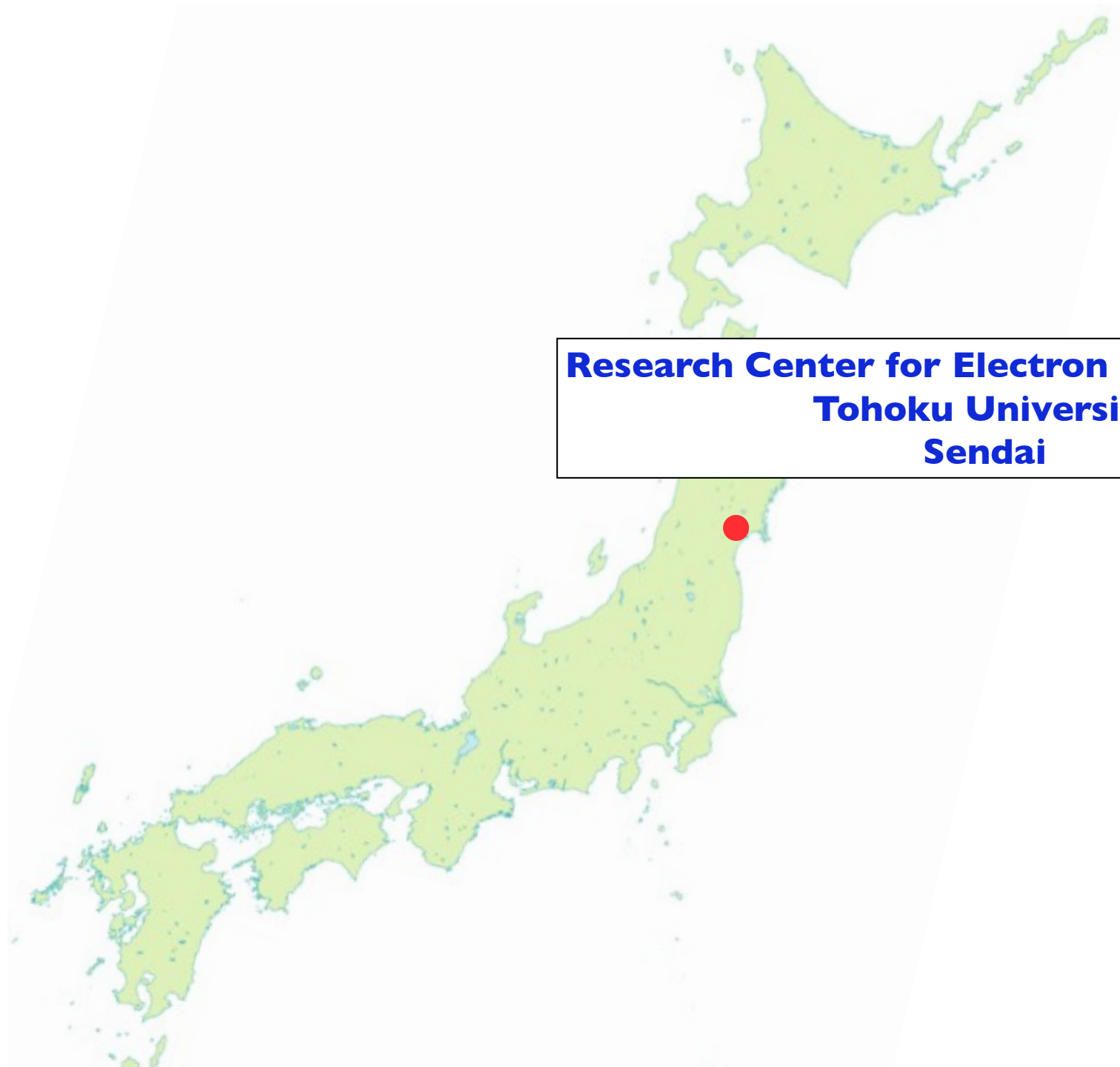
experimental GE separation at ultra-low Q^2

ELPH, Tohoku Univ. : only a electron scattering facility.

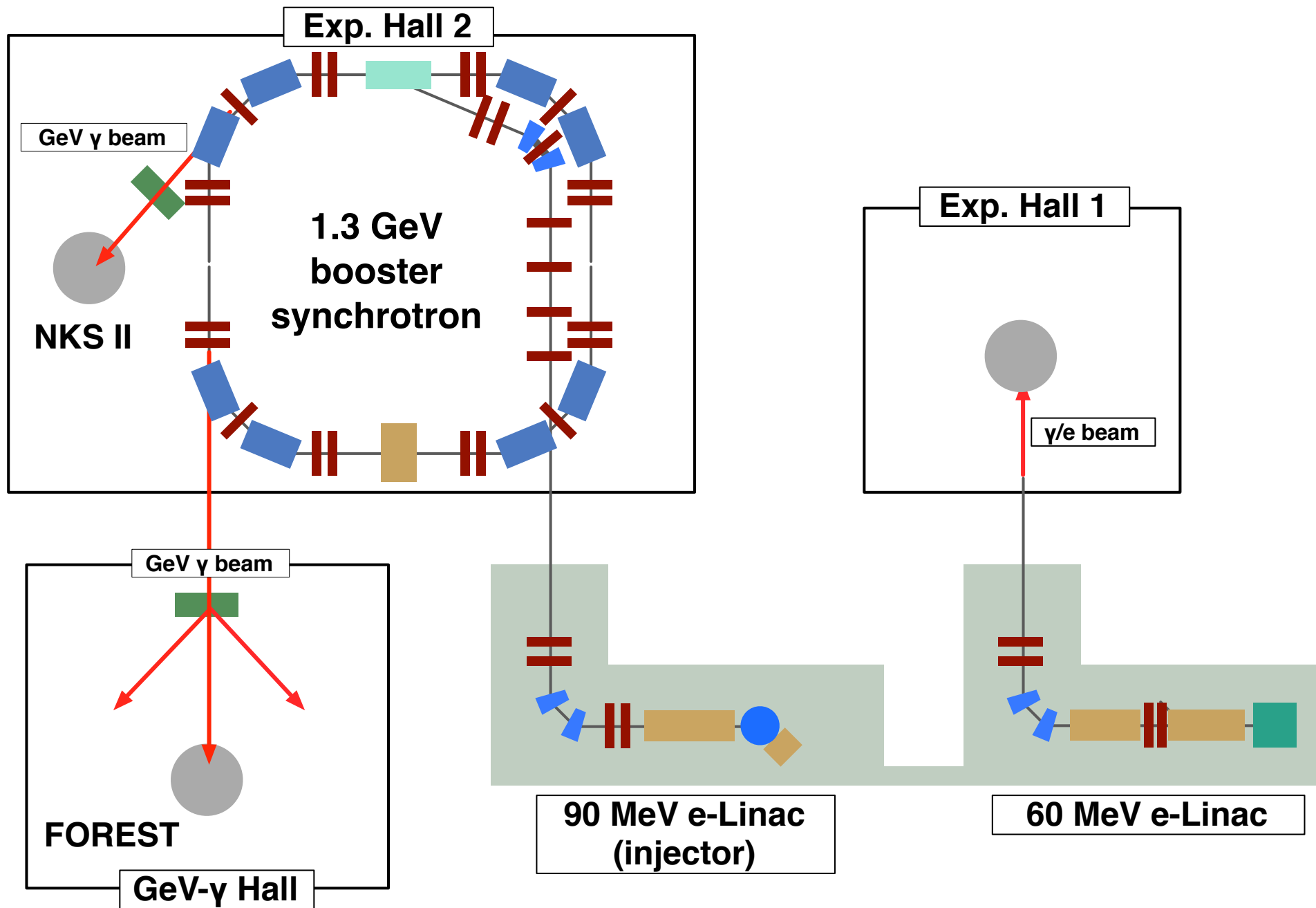
Lab.		E_e	θ	absolute $d\sigma/d\Omega$	G_E, G_M separation
JLAB (USA)	Ultra-forward	1.1 - 2.2 GeV	1 - 4 deg.	○	X
Mainz (Germany)	lower E_e by Bremsstrahlung	195, 330, 490 MeV		X	X
TOHOKU	low E_e	20 - 60 MeV	30 - 150 deg.	○	○

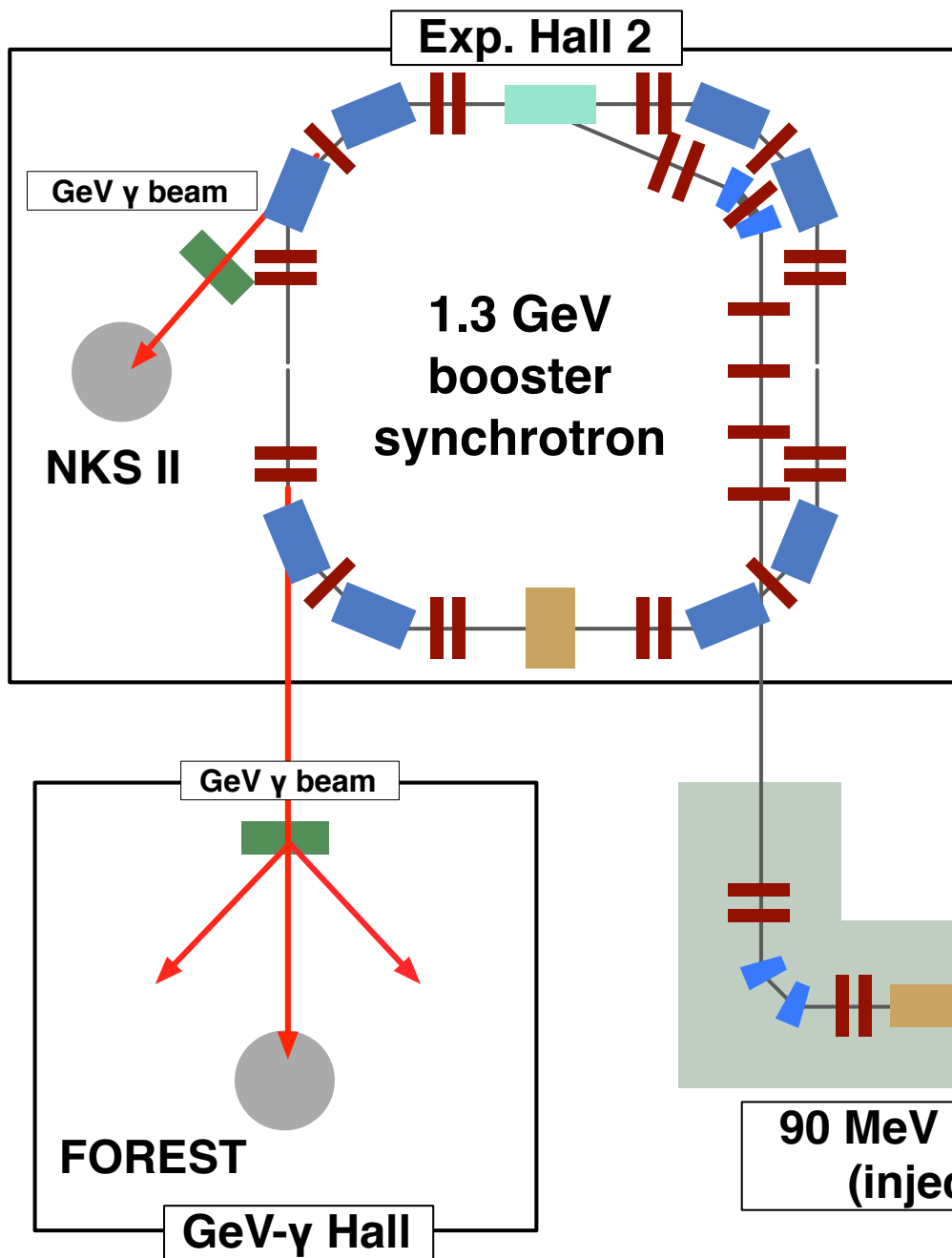
Where are we ?

ULQ2@JPARC
Nov. 1, 2016



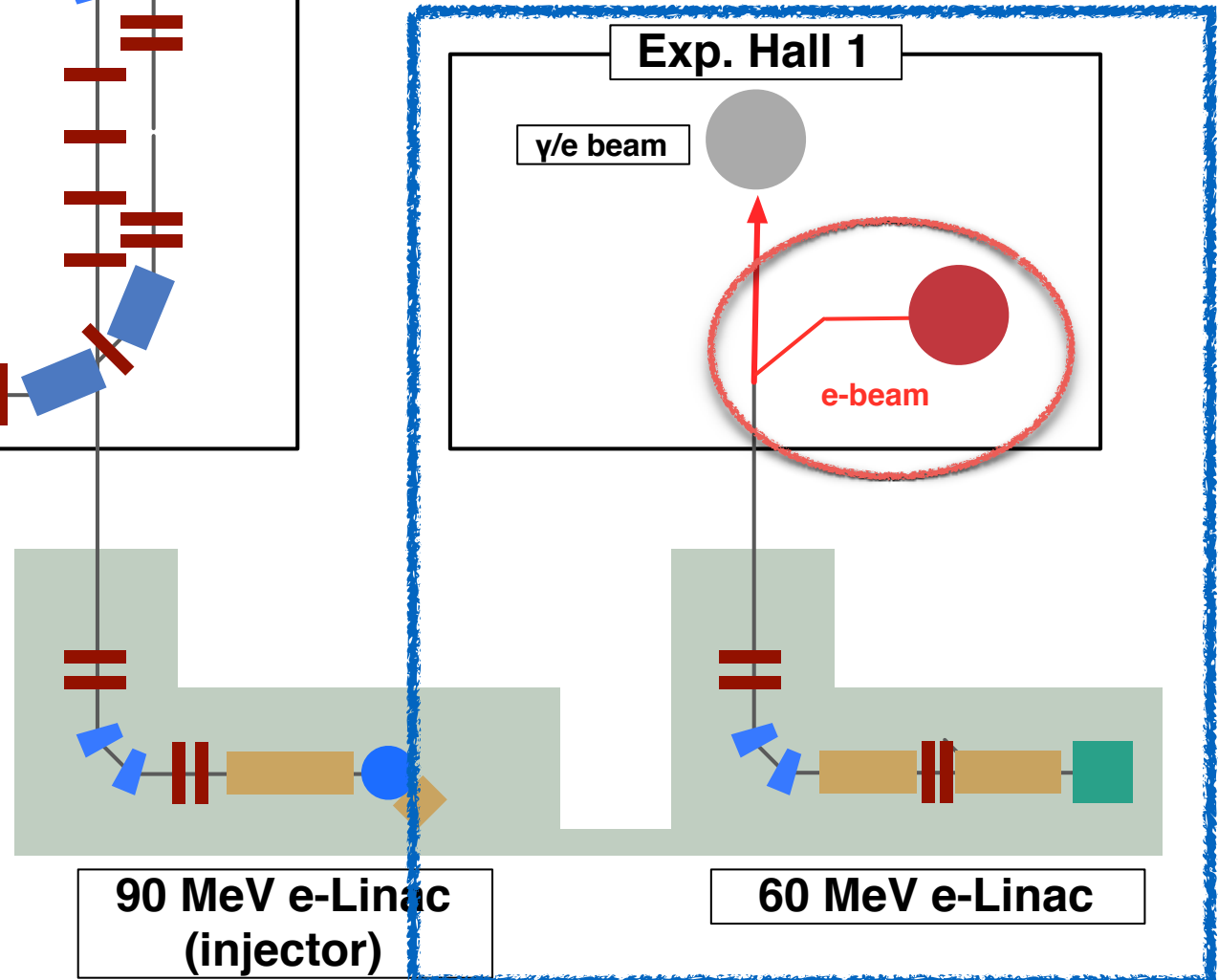
**Research Center for Electron Photon Science
Tohoku University
Sendai**





“OLD” Low-Energy Electron Linac

E_e : 20 ~ 60 MeV variable
 I_e : 0 ~ 150 μ A



Goal of our experiment

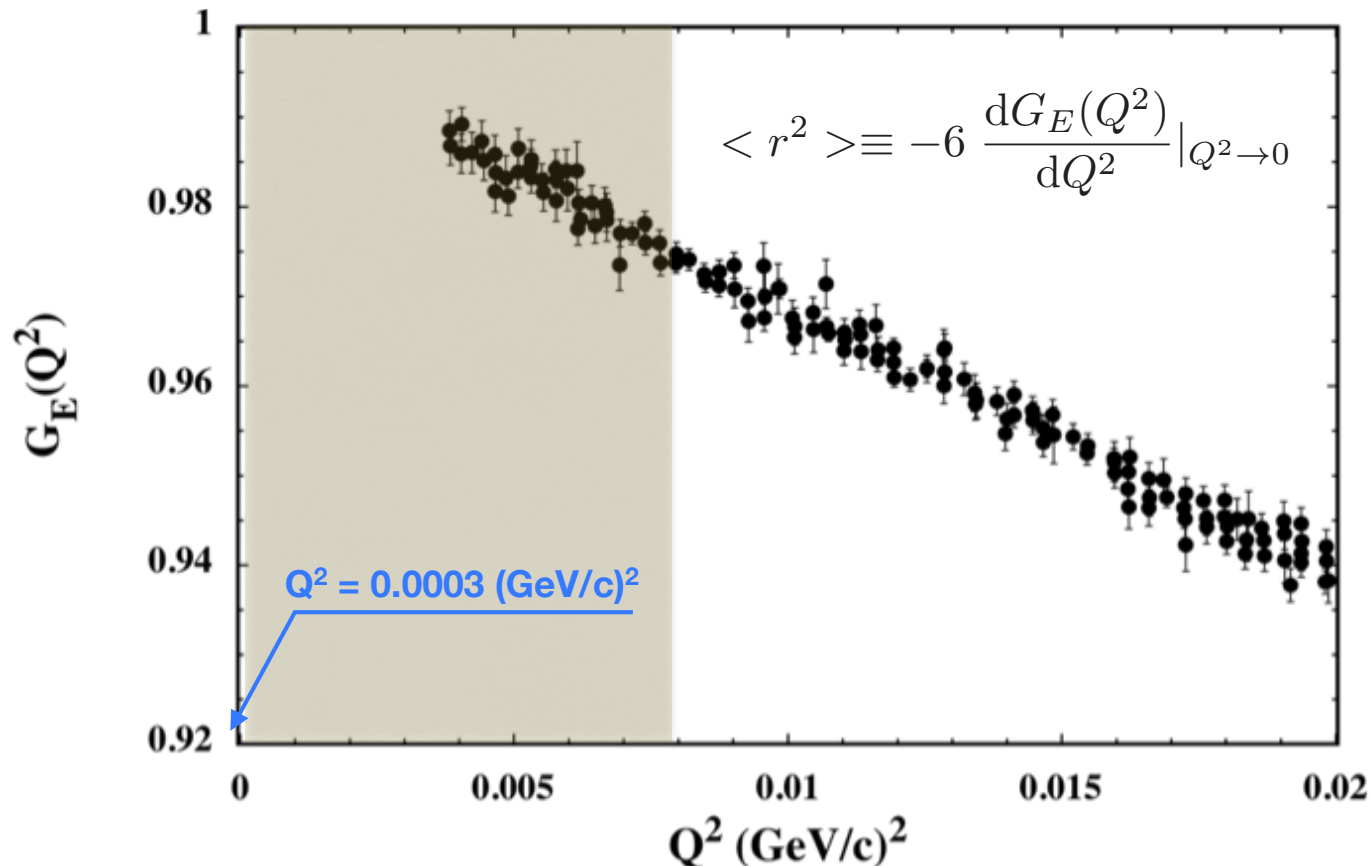
$G_E(Q^2)$ measurements in $0.0003 \leq Q^2 \leq 0.008 \text{ (GeV/c)}^2$

Our experiments

Low energy electron beam ($20 \leq E_e \leq 60 \text{ MeV}$)

Absolute cross section measurement

Rosenbluth separation ($G_E(Q^2)$, $G_M(Q^2)$ separation)

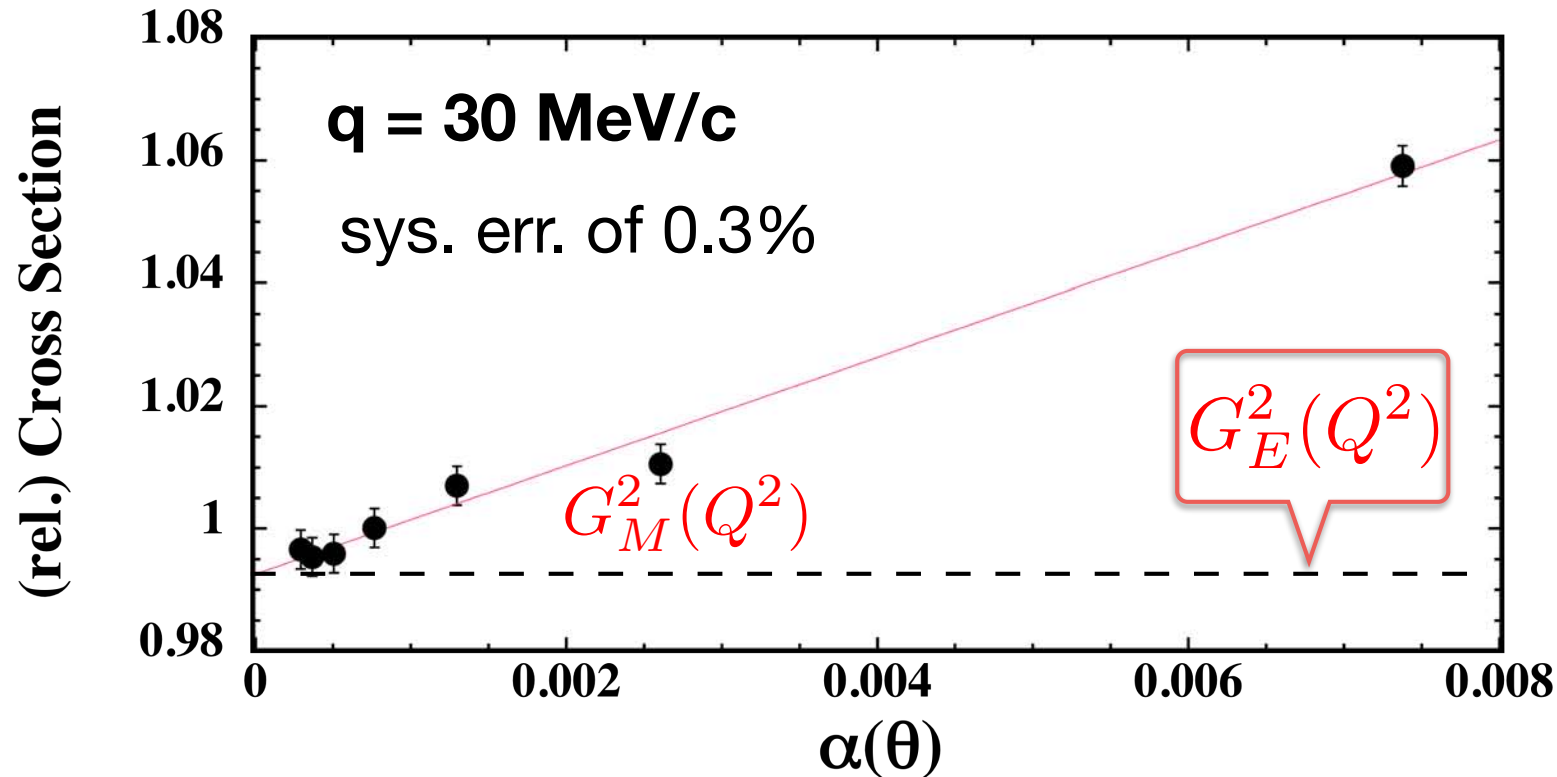


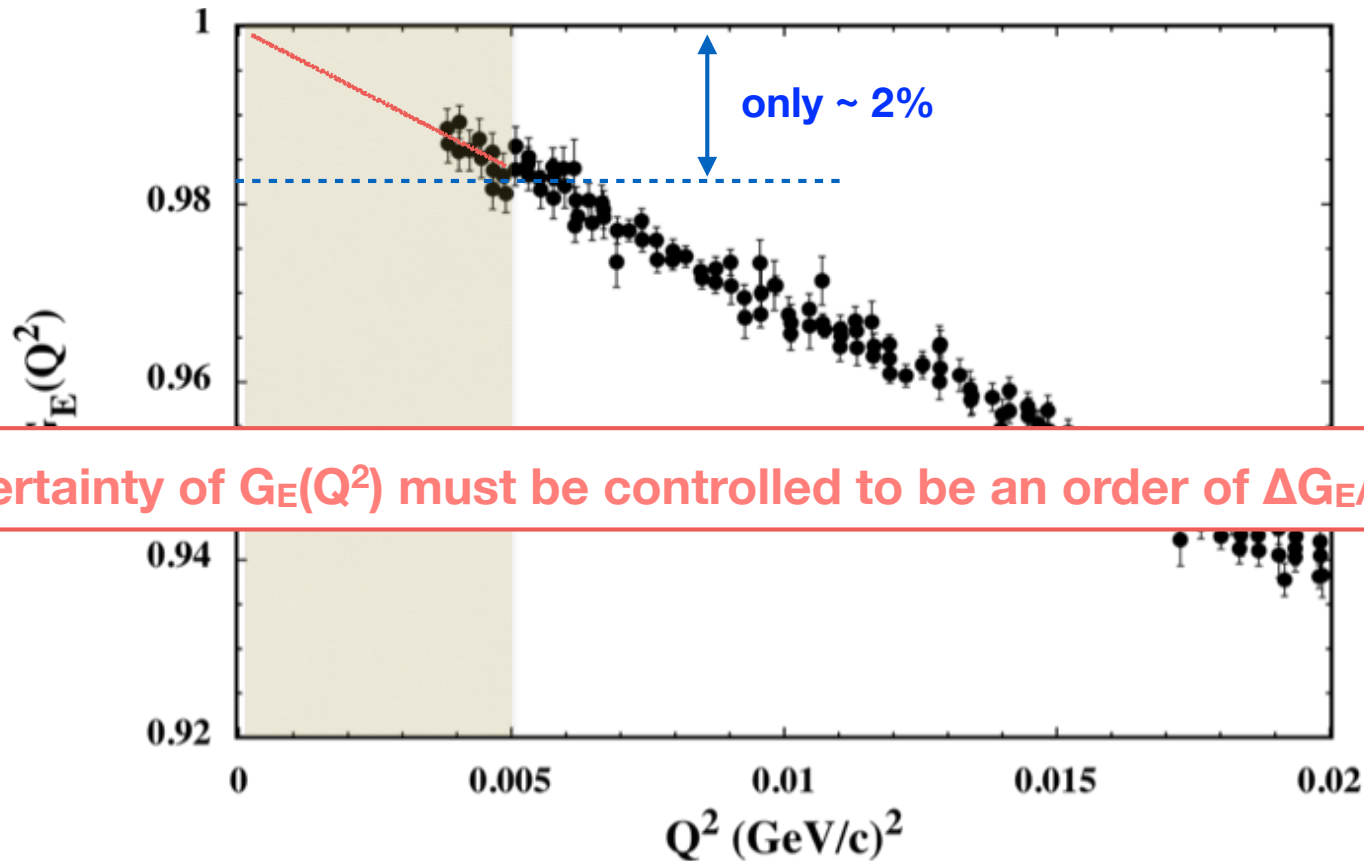
Elastic cross section

$$\frac{d\sigma}{d\Omega} \propto G_E^2(Q^2) + \alpha(\theta) G_M^2(Q^2) \quad Q^2 = 4ee' \sin^2(\theta/2)$$

change $\alpha(\theta)$ under fixed Q^2 \rightarrow different electron beam energies

Rosenbluth separation





Uncertainty of $G_E(Q^2)$ must be controlled to be an order of $\Delta G_E/G_E \sim 10^{-3}$

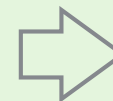
$$\frac{dN_{evt}}{d\Omega} = \frac{d\sigma}{d\Omega} \underbrace{N_{target}}_{\text{target thickness}} \underbrace{N_{beam}}_{\text{beam dose}} \underbrace{\Delta\Omega}_{\text{spectrometer acceptance}}$$

Statistics : at least $> 10^6$ for each (E_e, θ) measurements

Target thickness

Beam dose at various intensities

Acceptance at various scattering angle



accuracy of $\sim 10^{-3}$
not obvious !

Relative measurement for ¹²C(e,e)¹²C and p(e,e)p

$$\frac{dN^{e^{12}C} / d\Omega}{dN^{ep} / d\Omega} = \frac{d\sigma^{e^{12}C} / d\Omega}{d\sigma^{ep} / d\Omega} \cdot \frac{N_{target}^{12C}}{N_{target}^H}$$

$$\frac{dN_{evt}}{d\Omega} = \frac{d\sigma}{d\Omega} N_{target} \boxed{N_{beam} \Delta\Omega}$$

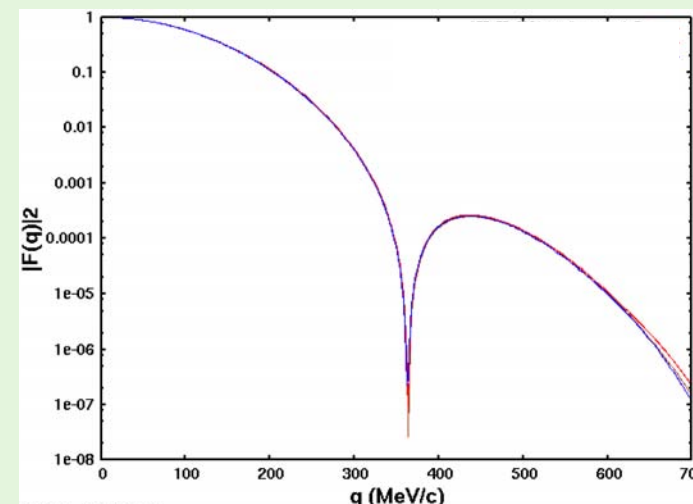
Canceled out in relative measurements

- 1) RMS charge radius (or $\rho(r)$) of ¹²C ??
- 2) ¹²C(e,e)¹²C, p(e,e)p by kinematics ??
- 3) change of C/H ratio by beam irradiation ??

1) ¹²C : “standard” nucleus for (e,e')

μ-Xray
electron scattering

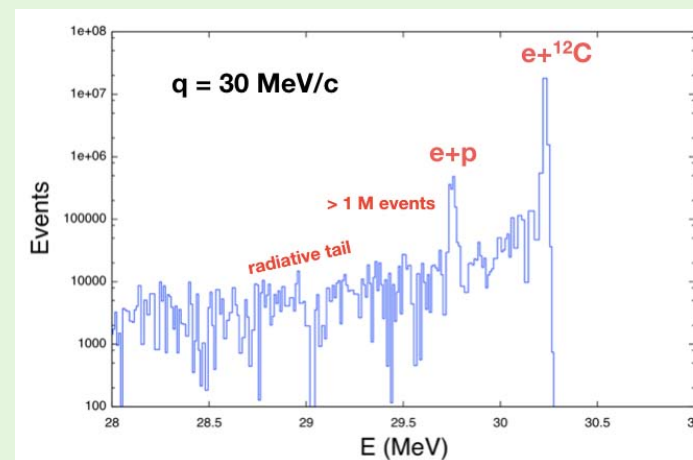
$$\frac{\Delta \langle r_{12C}^2 \rangle^{1/2}}{\langle r_{12C}^2 \rangle^{1/2}} \sim 3 \times 10^{-3}$$



2) ¹²C(e,e)¹²C, p(e,e)p by kinematics

$\Delta E = 0.2 - 4$ MeV
for $q = 20 - 90$ MeV/c

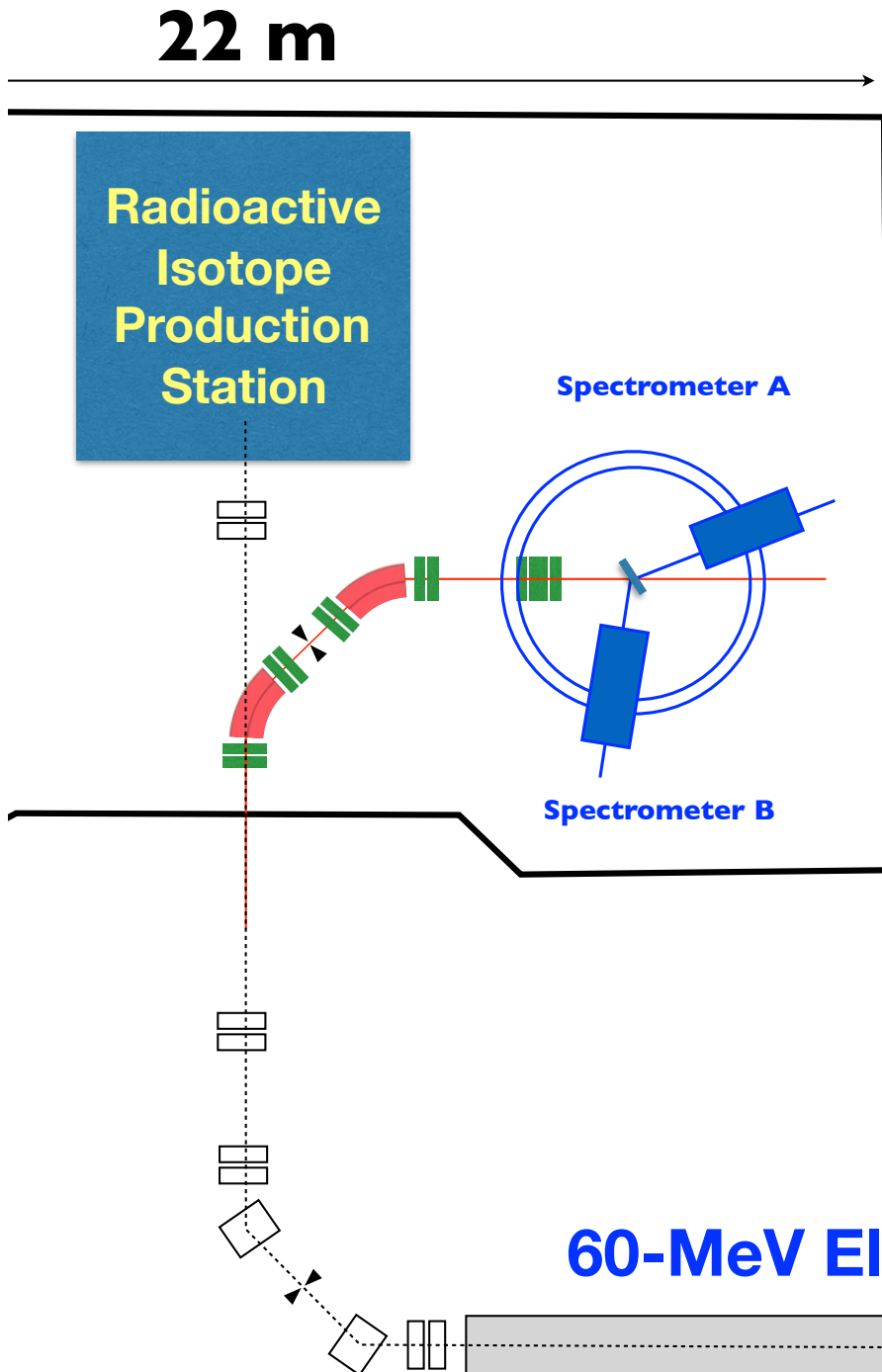
$$\Delta p/p \sim 10^{-3}$$



3) no severe damage of target is expected

large cross section : $\frac{d\sigma}{d\Omega} \propto 1/q^4$

$I_e \sim 1$ nA - 1 μA



$E_e = 20 \sim 60 \text{ MeV}$
 $I_e \sim 1 \text{ nA} - 1 \mu\text{A}$

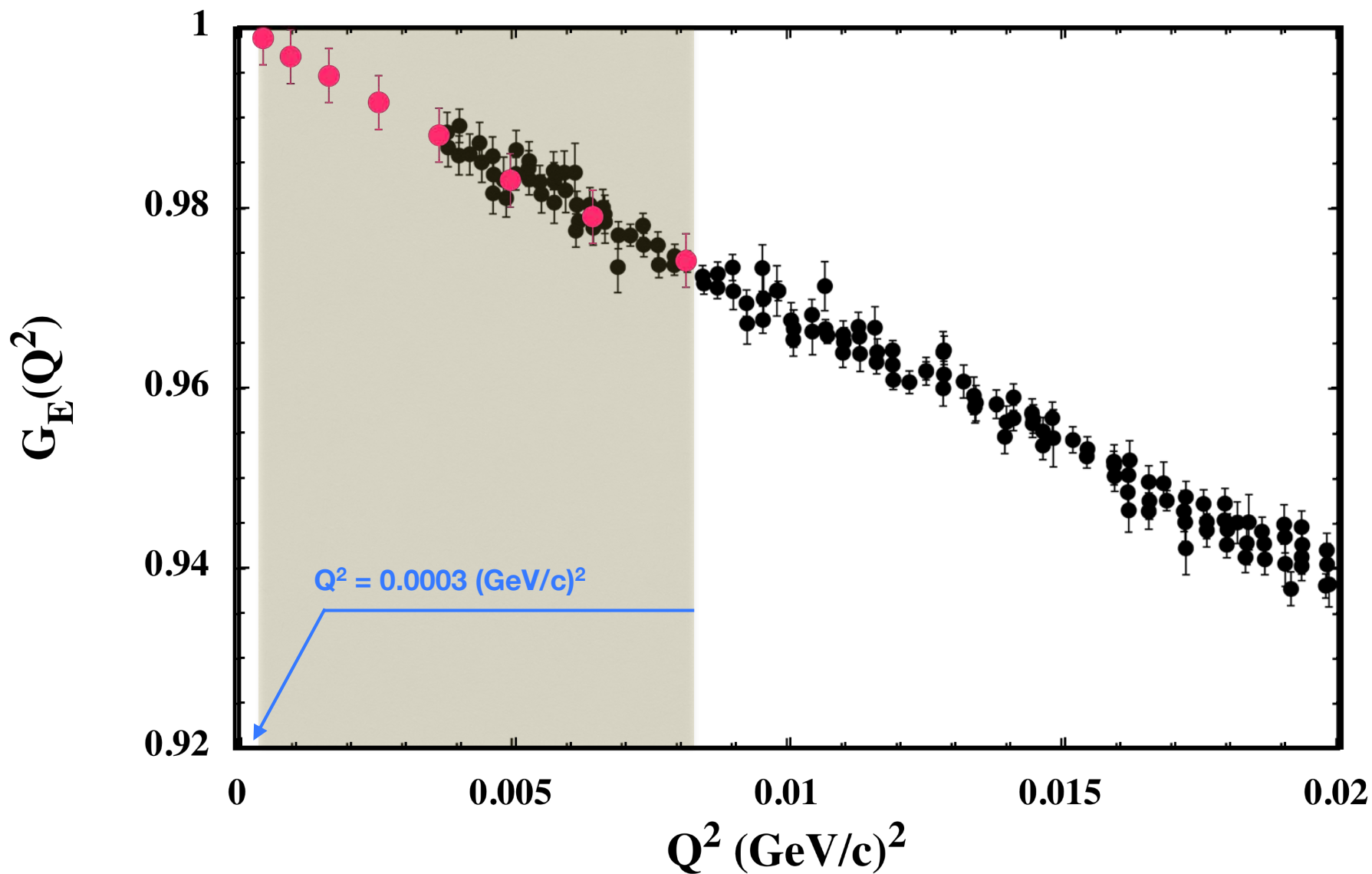
- 1) new beam line
- 2) two magnetic spectrometers
Rosenbluth measurements
Luminosity monitoring

CH_2 target ($\sim 0.1 \text{ mm t}$)
 $\Delta p/p \sim 1 \times 10^{-3}$

Absolute cross section
Rosenbluth separation

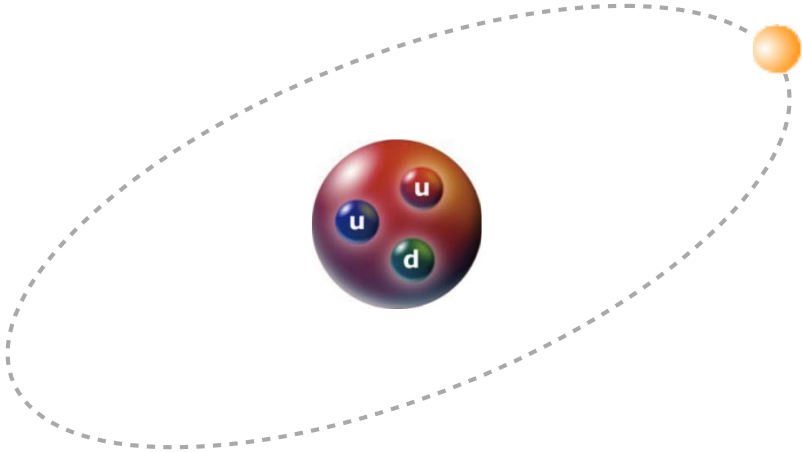
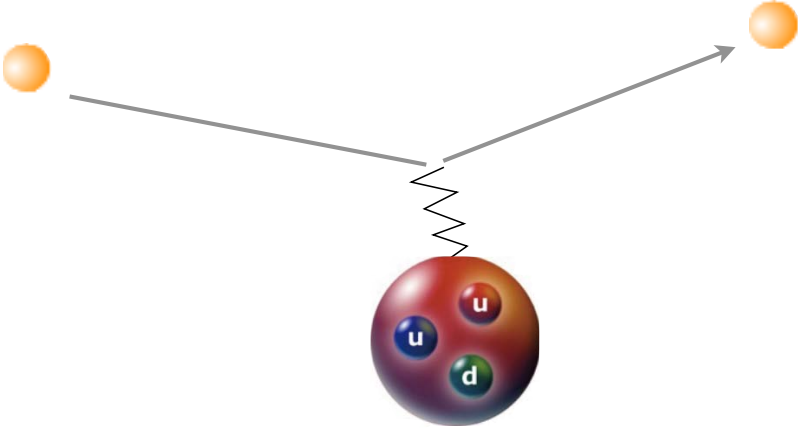
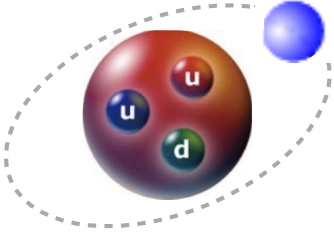


$G_E(Q^2)$



How r_p has been determined ??

ULQ2@JPARC
Nov. 1, 2016

	Spectroscopy	Scattering
e^-	 A diagram showing a central nucleus composed of two red spheres labeled 'u' and one green sphere labeled 'd'. A dashed grey elliptical orbit surrounds the nucleus, with a single orange sphere representing an electron at the top of the orbit.	 A diagram showing an orange sphere (electron) on the left with an arrow pointing towards a central nucleus (two red 'u' spheres and one green 'd' sphere). A zigzag line representing a photon connects the nucleus to another orange sphere on the right, with an arrow pointing away from it, indicating scattering.
μ^-	 A diagram showing a central nucleus (two red 'u' spheres and one green 'd' sphere) with a dashed grey elliptical orbit. A small blue sphere representing a muon is positioned at the top of the orbit.	<p>MUSE exp. @PSI is coming ...</p>

- 1) elastic e+p scattering at ultra-low Q^2 region
- 2) $G_E(Q^2)$ at $0.0003 \leq Q^2 \leq 0.008 \text{ (GeV/c)}^2$
- 3) G_E is extracted by the **Rosenbluth separation**
- 4) **absolute cross section measurement**
relative to $^{12}\text{C}(e,e)^{12}\text{C}$: sys. err. $\sim 3 \times 10^{-3}$
- 5) $E_e = 20 - 60 \text{ MeV}$, $\theta = 30 - 150^\circ$
- 6) constructing of new beam line, and spectrometers
- 7) the experiments will start in 2019